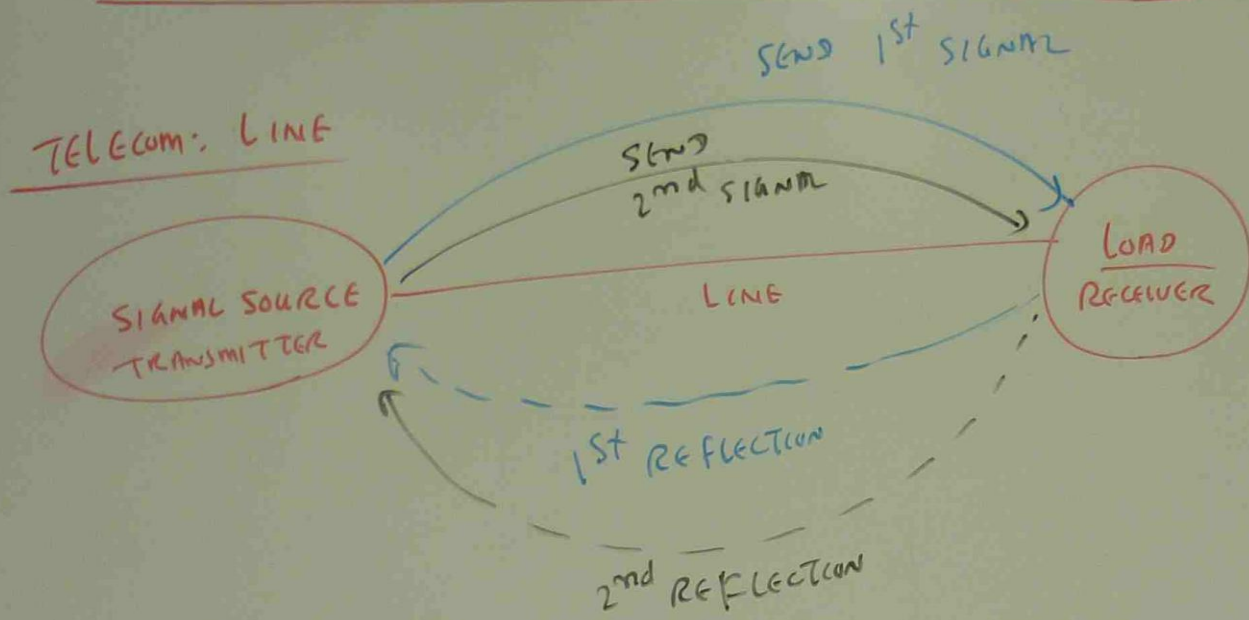


APPLICATION OF REFLECTION AND OSCILLATION FUNCTIONS IN POWER ENGINEERING



V_s = SOURCE VOLTAGE
 Z_0 = LINE IMPEDANCE
 Z_s = SOURCE IMPEDANCE
 Z_L = LOAD IMPEDANCE

V_+ = SOURCE TO LOAD VOLTAGE

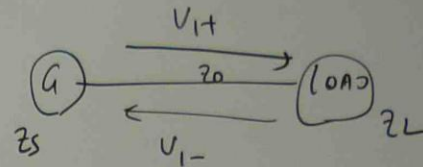
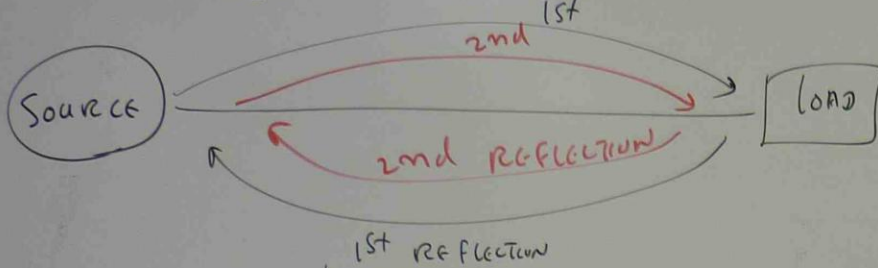
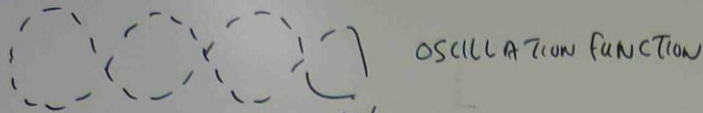
V_- = REFLECTED VOLTAGE

1st REFLECTION AT LOAD = $V_t = V_+ + V_-$

$V_+ = V_s \times \frac{Z_0}{Z_0 + Z_s}$

$V_- = V_+ \times \left(\frac{Z_L - Z_0}{Z_L + Z_0} \right)$

G047



Z_L = LOAD IMPEDANCE
 Z_0 = LINE IMPEDANCE
 Z_S = SOURCE IMPEDANCE

1st REFLECTION AT LOAD

$$V_t = V_{1+} + V_{1-}$$

$$V_{1+} = V_s \frac{Z_0}{Z_0 + Z_S}$$

$$V_{1-} = V_{1+} \times \Gamma_L \leftarrow \frac{Z_L - Z_0}{Z_L + Z_0}$$

2nd REFLECTION AT SOURCE $\Rightarrow V_t = V_{1+} + V_{1-} + V_{2+}$

$$V_{2+} = V_{1-} \times \Gamma_S \leftarrow \frac{Z_S - Z_0}{Z_S + Z_0}$$

3rd REFLECTION AT LOAD \Rightarrow

$$V_t = V_{1+} + V_{1-} + V_{2+} + V_{2-}$$

$$V_{2-} = V_{2+} \times \Gamma_L \leftarrow \frac{Z_L - Z_0}{Z_L + Z_0}$$

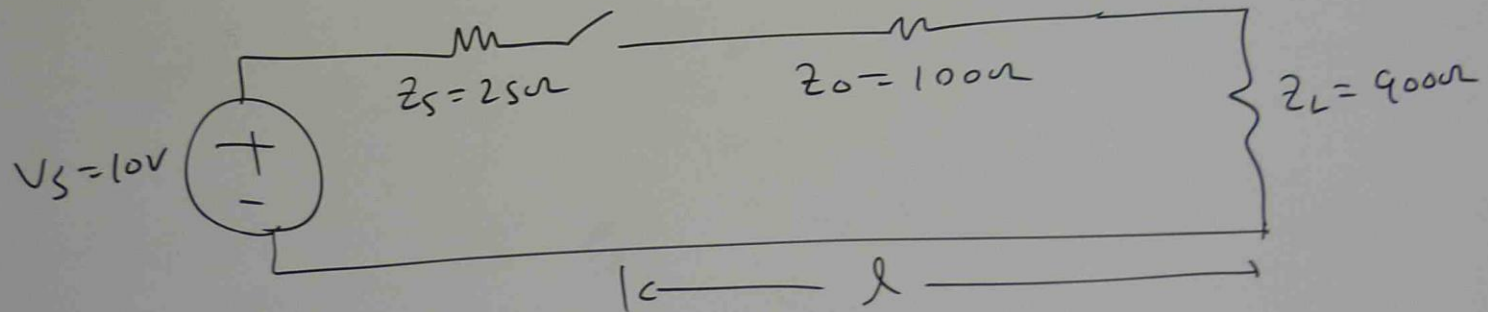
Ex

A 10V DC SOURCE WITH AN INTERNAL RESISTANCE OF 25Ω IS CONNECTED TO A TRANSMISSION LINE OF LENGTH "L" HAVING AN IMPEDANCE OF 100Ω BY SWITCH. THE TRANSMISSION LINE IS TERMINATED WITH A 900Ω RESISTOR. T = AMOUNT OF TIME REQUIRED FOR SIGNAL TO TRAVEL THE LENGTH OF THE LINE. CALCULATE (a) THE VOLTAGE WHEN THE SWITCH IS CLOSED AT $T=0$

(b) FIRST REFLECTION AT LOAD

(c) SECOND REFLECTION AT SOURCE

(d) THIRD REFLECTION AT LOAD



(a) VOLTAGE AT $t=0$

$$\begin{aligned} V_{1+} &= V_S \times \frac{Z_0}{Z_0 + Z_S} \\ &= 10 \times \frac{100}{100 + 25} = 8V \end{aligned}$$

$$(b) V_{1(-)} = V_{1(+)} \Gamma_L$$

$$= 8 \times \frac{Z_L - Z_0}{Z_L + Z_0}$$

$$= 8 \times \frac{900 - 100}{900 + 100}$$

$$= 8 \times \frac{800}{1000} = 6.4 V$$

FIRST REFLECTION
AT LOAD

$$V_L(t) = V_{1(+)} + V_{1(-)}$$

$$= 8 + 6.4$$

$$= 14.4 V$$

$$(c) V_{2+} = V_{(-)} \times \Gamma_S$$

$$= 6.4 \times \frac{Z_S - Z_0}{Z_S + Z_0}$$

$$= 6.4 \times \frac{25 - 100}{25 + 100}$$

$$= -3.84 V$$

$$\text{2nd reflection AT SOURCE} = V_{1(+)} + V_{1(-)} + V_{2(+)}$$

$$= 8 + 6.4 + (-3.84)$$

$$= 10.56 V$$

$$(d) V_{2(-)} = V_{2(+)} \Gamma_L$$

$$= (-3.84) \times \frac{Z_L - Z_0}{Z_L + Z_0}$$

$$= -3.84 \times \frac{900 - 100}{900 + 100}$$

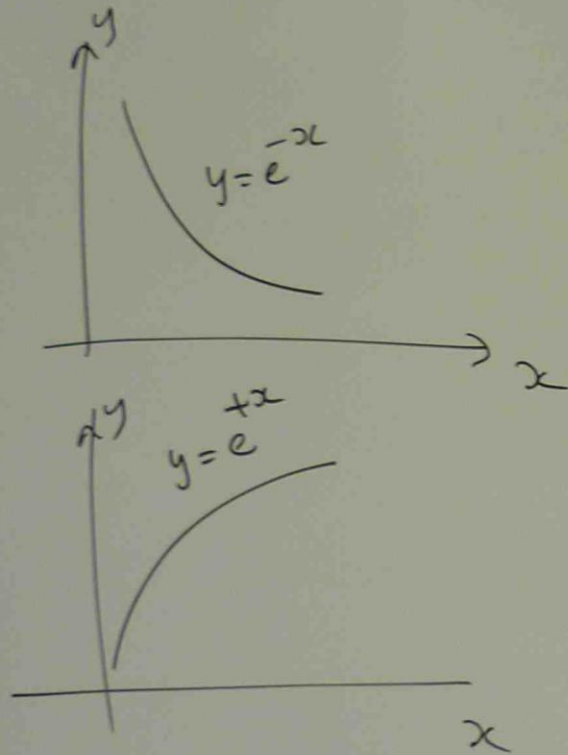
$$= -3.072 V$$

$$\text{3rd reflection AT LOAD} = V_{1(+)} + V_{1(-)} + V_{2(+)} + V_{2(-)}$$

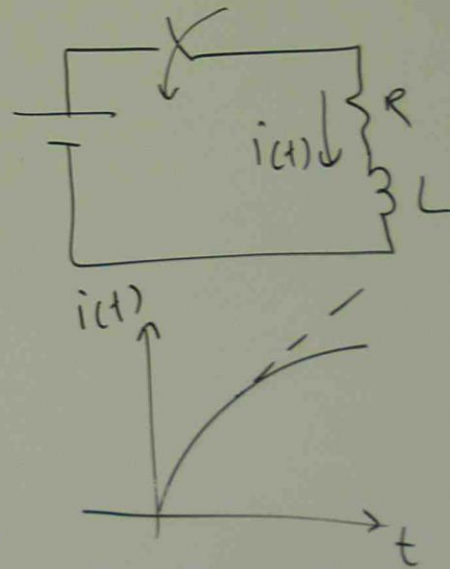
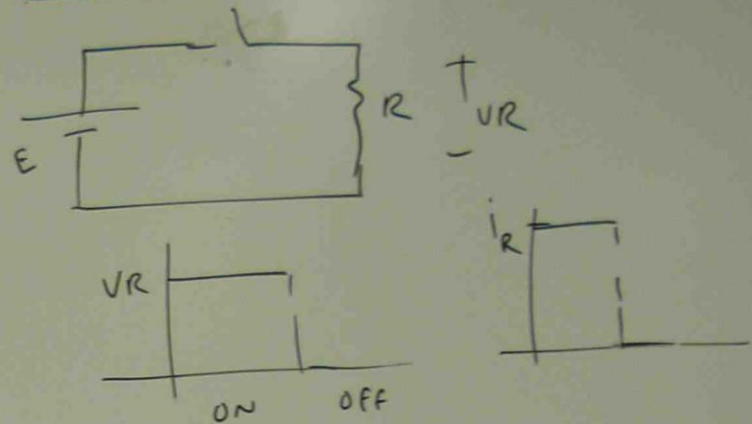
$$= 8 + 6.4 + (-3.84) + (-3.072)$$

$$= 7.488 V$$

APPLICATION OF EXPONENTIAL FUNCTION IN POWER ENGINEERING CALCULATIONS

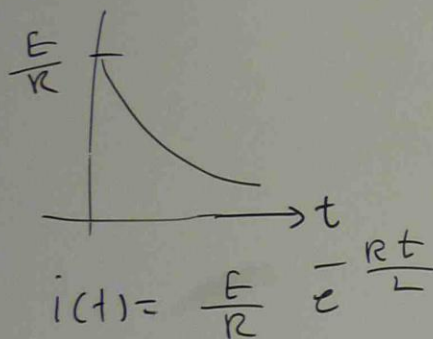
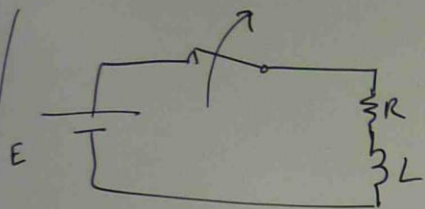


PURE RESISTANCE



$$i(t) = \frac{V}{R} \left(1 - e^{-\frac{Rt}{L}} \right)$$

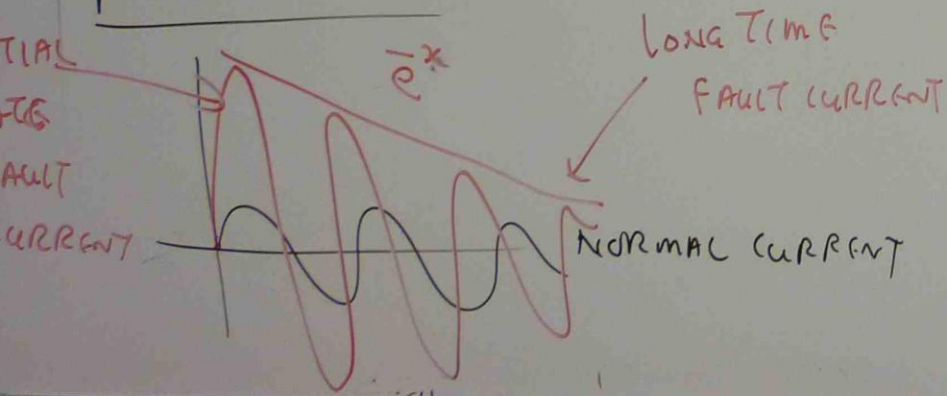
INITIAL
STATE
FACTORS
CONSIDERED



TRANSIENT CIRCUIT CALCULATION

USES EXPONENTIAL FUNCTION

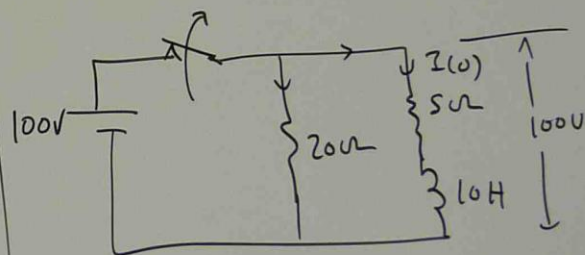
POWER LINE FAULT



EX

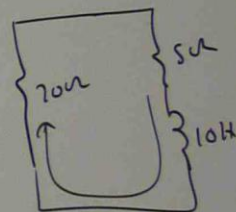
A COIL OF 10 H INDUCTANCE AND 5 OHM RESISTANCE IS CONNECTED IN PARALLEL WITH A 20 OHM RESISTOR ACROSS A 100 V DC SUPPLY WHICH IS SUDDENLY DISCONNECTED.

- FIND (a) INITIAL RATE OF CHANGE OF CURRENT AFTER SWITCHING
 (b) THE VOLTAGE ACROSS 20 OHM RESISTOR INITIALLY AFTER 0.3 S
 (c) THE VOLTAGE ACROSS THE SWITCH CONTACTS AT THE INSTANCE OF SEPARATION
 (d) THE RATE AT WHICH THE COIL IS LOSING STORED ENERGY 0.3 SEC AFTER SWITCHING.



$$I(0) = \frac{100}{5} = 20\text{ A}$$

OFF THE SWITCH



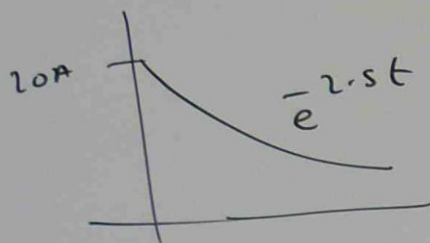
$$i(t) = i(0) e^{-\frac{Rt}{L}}$$

$$R = 20 + 5 = 25 \Omega$$

$$L = 10 \text{ H}$$

$$i(1) = 20 e^{-\frac{25t}{10}}$$

$$= 20 e^{-2.5t}$$



(a)

$$\frac{di(t)}{dt} = \frac{d}{dt} (20 e^{-2.5t})$$

$$= 20 (-2.5) e^{-2.5t}$$

$$= -50 e^{-2.5t}$$

(b)

$$V_{20\Omega}(t) = i(t) \times 20 \Omega$$

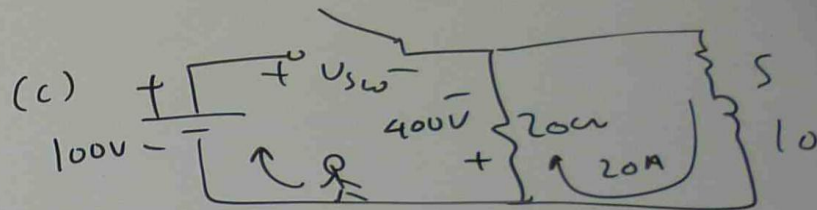
$$= 20 e^{-2.5t} \times 20$$

$$= 400 e^{-2.5t}$$

$$V_{20\Omega}(0.3) = 400 \times e^{-2.5 \times 0.3}$$

$$= 400 \times e^{-0.75}$$

$$= 188 \text{ V}$$



(c)

$$V_{20\Omega}(0) = 20 \times 20 = 400 \text{ V}$$

$$(-100) + V_{sw} + (-400) = 0$$

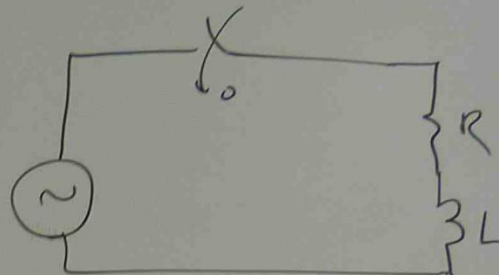
$$V_{sw} = 500 \text{ V}$$

(d)

$$\text{Stored Energy} = L \frac{di(t)}{dt} \times i(t)$$

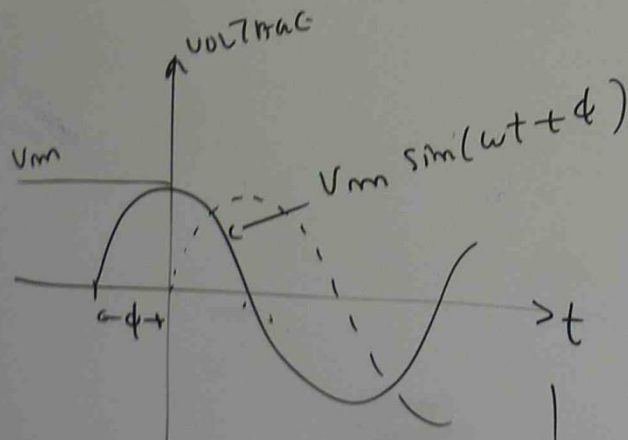
$$10 \times (-50 e^{-2.5t}) \times 20 e^{-2.5t} = -10000 e^{-5t}$$

TRANSIENT / EXPONENTIAL FUNCTION IN AC CIRCUITS



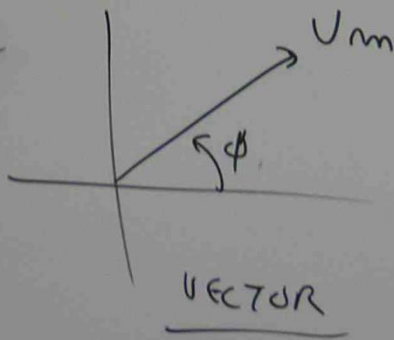
$$V = V_m \sin(\omega t + \phi)$$

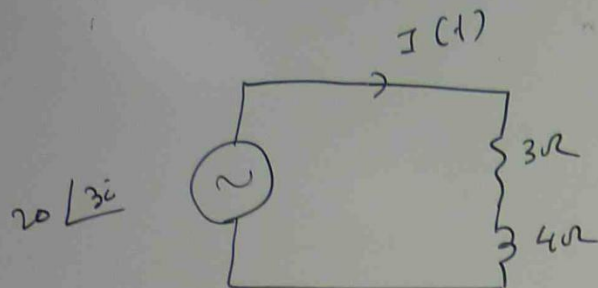
TIME DOMAIN REPRESENTATION



$$V = \frac{V_m}{\sqrt{2}} \angle \phi$$

FREQUENCY DOMAIN REPRESENTATION





FIND THE CURRENT IN

(a) FREQUENCY DOMAIN REPRESENTATION

(b) TIME DOMAIN REPRESENTATION

FREQUENCY = 50 Hz

$$I = \frac{V}{Z} = \frac{20 \angle 30^\circ}{3 + j4} = \frac{20 \angle 30^\circ}{\sqrt{3^2 + 4^2} \angle \tan^{-1} 4/3}$$

$$= \frac{20 \angle 30^\circ}{5 \angle 53.2^\circ} = 4 \angle -23.2^\circ$$

(a) FREQUENCY
DOMAIN
CURRENT

(b) TIME DOMAIN CURRENT

$$I(t) = I_m \sin(\omega t + \phi)$$

$$= 2 \times 4 \sin(2\pi f t + (-23.2^\circ))$$

$$= 1.4142 \times 4 \sin(2 \times 3.1416 \times 50 t - 23.2^\circ)$$

$$= 5.62 \sin(314 t - 23.2^\circ)$$

(b) TIME DOMAIN CURRENT

$$I(t) = I_m \sin(\omega t + \phi)$$

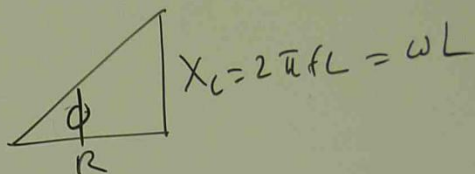
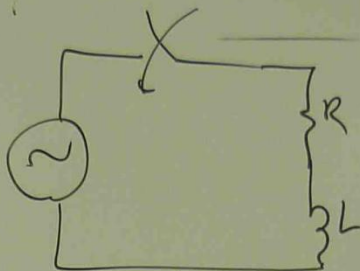
$$= 2 \times 4 \sin(2\pi f t + (-23.2))$$

$$= 1.4142 \times 4 \sin(2 \times 3.1416 \times 50 t - 23.2)$$

$$= 5.62 \sin(314 t - 23.2)$$

$$\tan^{-1} 4/3$$

$$3.2$$



$$\hat{i}(t) = \frac{V_m}{\sqrt{R^2 + \omega^2 L^2}} \left(\sin(\omega t - \phi) + \sin \phi e^{-\frac{Rt}{L}} \right)$$

$$\phi = \tan^{-1} \frac{\omega L}{R}$$

PURE RESISTANCE

