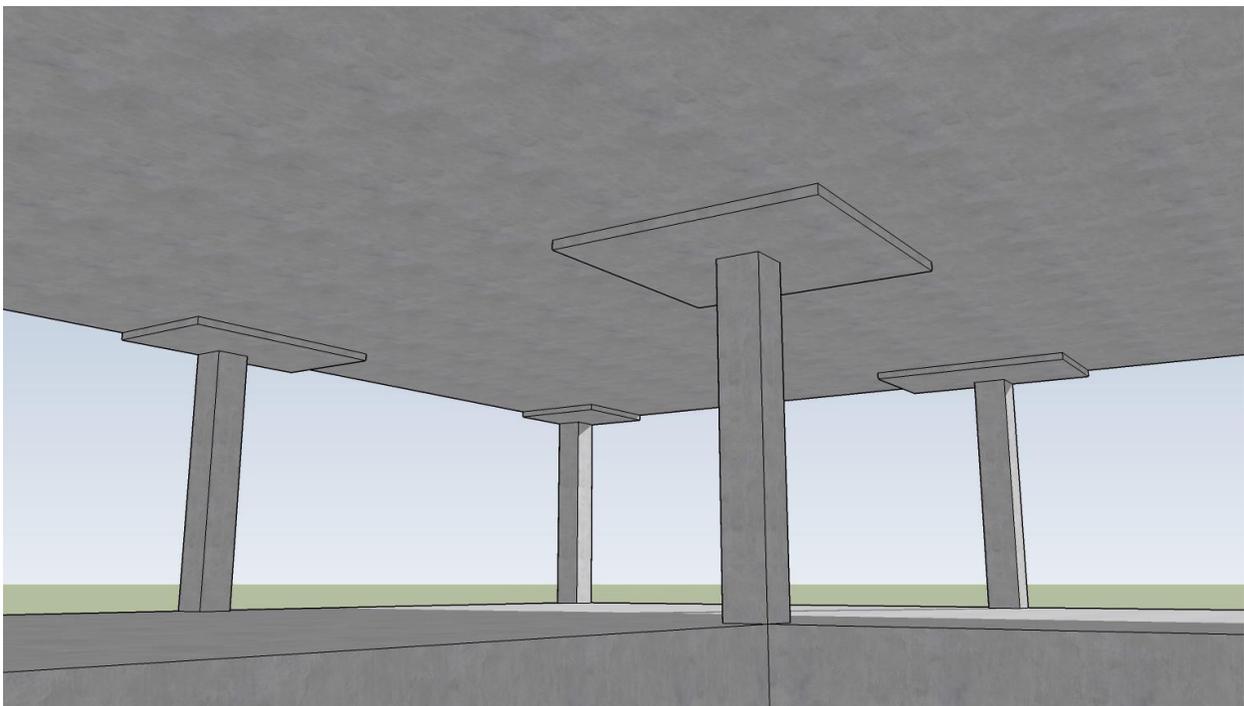
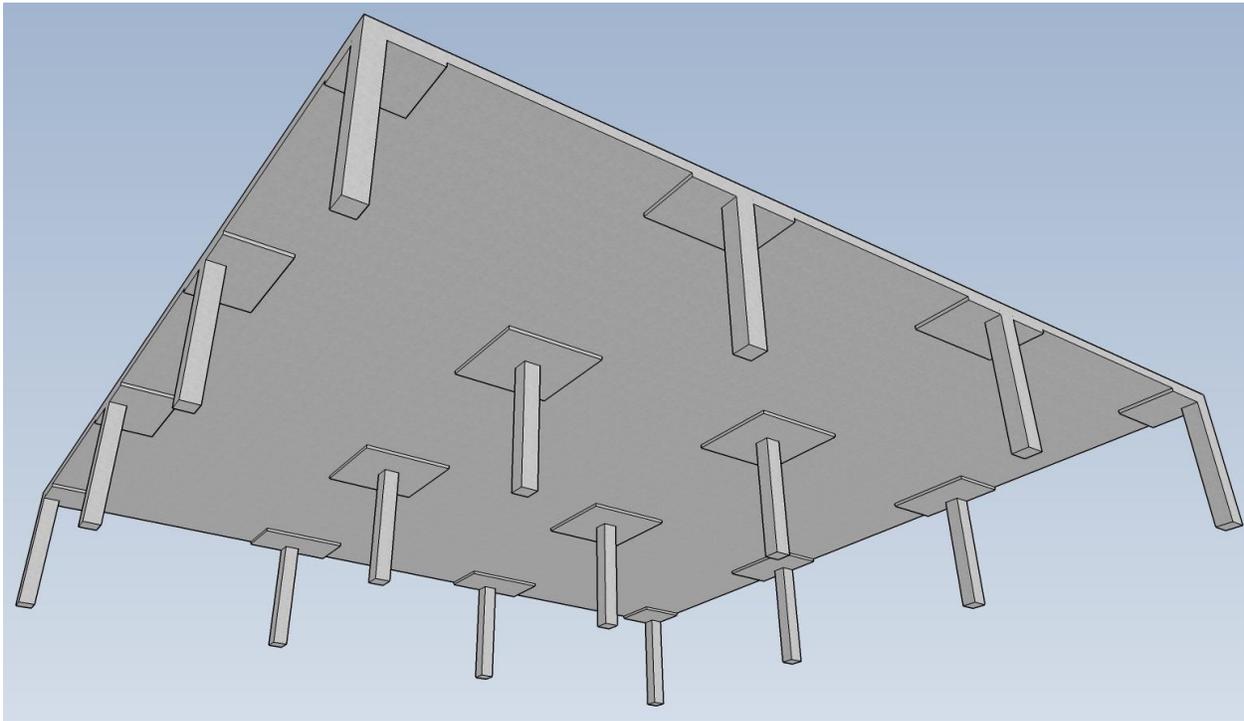


Two-Way Flat Slab (Concrete Floor with Drop Panels) System Analysis and Design



Two-Way Flat Slab (Concrete Floor with Drop Panels) System Analysis and Design

Design the concrete floor slab system shown below for an intermediate floor considering partition weight = 20 psf, and unfactored live load = 60 psf. The lateral loads are independently resisted by shear walls. The use of flat plate system will be checked. If the use of flat plate is not adequate, the use of flat slab system with drop panels will be investigated. Flat slab concrete floor system is similar to the flat plate system. The only exception is that the flat slab uses drop panels (thickened portions around the columns) to increase the nominal shear strength of the concrete at the critical section around the columns. The Equivalent Frame Method (EFM) shown in ACI 318 is used in this example. The hand solution from EFM is also used for a detailed comparison with the model results of [spSlab](#) engineering software program.

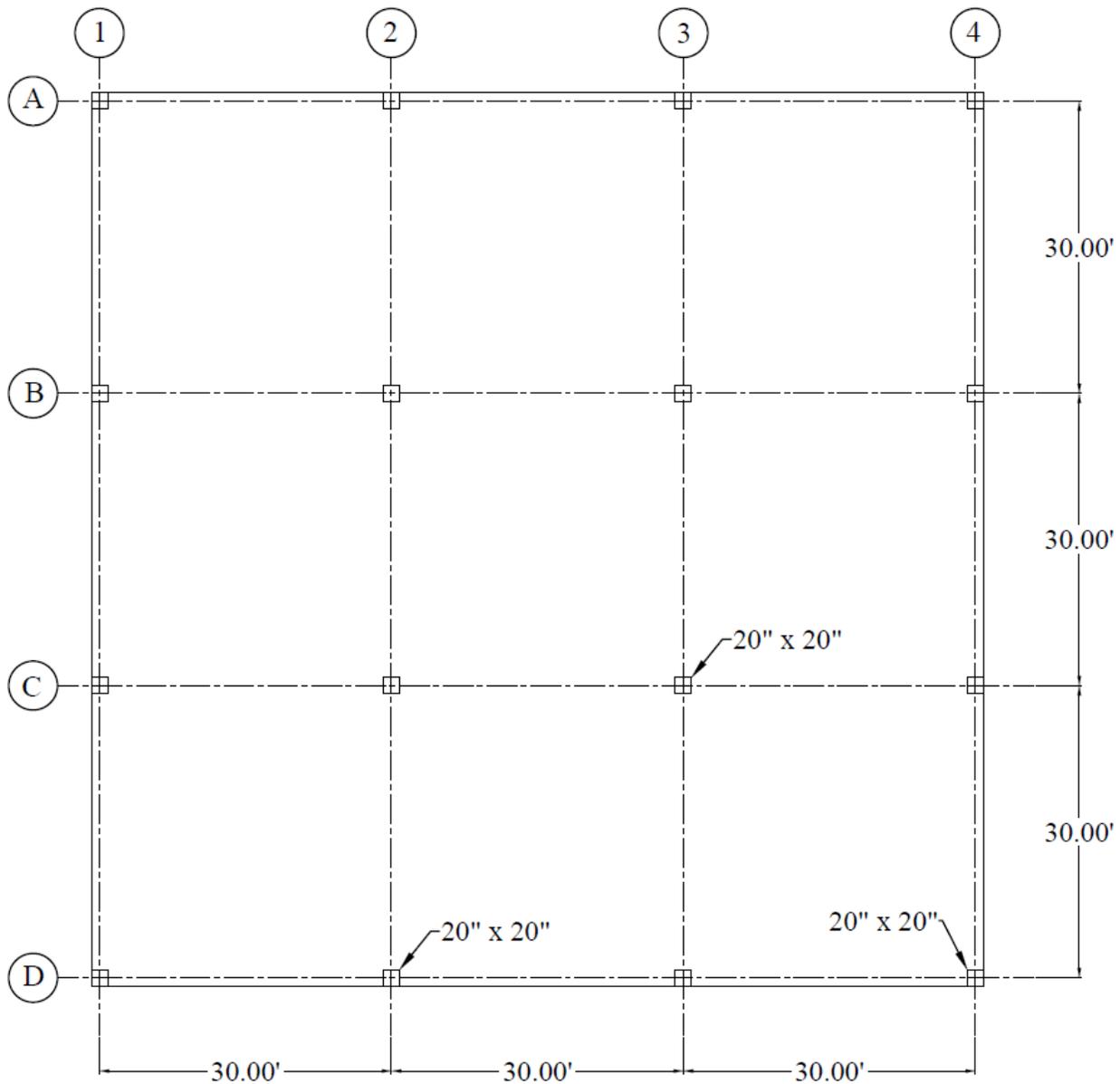


Figure 1 - Two-Way Flat Concrete Floor System

Contents

| | |
|--|----|
| 1. Preliminary member sizing | 1 |
| 2. Flexural Analysis and Design..... | 10 |
| 2.1. Equivalent Frame Method (EFM)..... | 10 |
| 2.1.1. Limitations for use of equivalent frame method..... | 11 |
| 2.1.2. Frame members of equivalent frame | 11 |
| 2.1.3. Equivalent frame analysis | 14 |
| 2.1.4. Factored moments used for Design | 16 |
| 2.1.5. Factored moments in slab-beam strip..... | 18 |
| 2.1.6. Flexural reinforcement requirements..... | 19 |
| 2.1.7. Factored moments in columns..... | 22 |
| 3. Design of Columns by spColumn | 24 |
| 3.1. Determination of factored loads..... | 24 |
| 3.2. Moment Interaction Diagram | 26 |
| 4. Shear Strength | 29 |
| 4.1. One-Way (Beam action) Shear Strength | 29 |
| 4.1.1. At distance d from the supporting column | 29 |
| 4.1.2. At the face of the drop panel | 30 |
| 4.2. Two-Way (Punching) Shear Strength | 31 |
| 4.2.1. Around the columns faces | 31 |
| 4.2.2. Around drop panels | 34 |
| 5. Serviceability Requirements (Deflection Check) | 37 |
| 5.1. Immediate (Instantaneous) Deflections..... | 37 |
| 5.2. Time-Dependent (Long-Term) Deflections (Δ_{lt})..... | 49 |
| 6. spSlab Software Program Model Solution | 50 |
| 7. Summary and Comparison of Design Results..... | 71 |
| 8. Conclusions & Observations | 74 |
| 8.1. One-Way Shear Distribution to Slab Strips | 74 |
| 8.2. Two-Way Concrete Slab Analysis Methods | 77 |

Code

Building Code Requirements for Structural Concrete (ACI 318-14) and Commentary (ACI 318R-14)

Reference

Concrete Floor Systems (Guide to Estimating and Economizing), Second Edition, 2002 David A. Fanella

Notes on ACI 318-11 Building Code Requirements for Structural Concrete, Twelfth Edition, 2013 Portland Cement Association.

Simplified Design of Reinforced Concrete Buildings, Fourth Edition, 2011 Mahmoud E. Kamara and Lawrence C. Novak

Control of Deflection in Concrete Structures (ACI 435R-95)

Design Data

Story Height = 13 ft (provided by architectural drawings)

Superimposed Dead Load, $SDL = 20$ psf for framed partitions, wood studs, 2 x 2, plastered 2 sides

ASCE/SEI 7-10 (Table C3-1)

Live Load, $LL = 60$ psf

ASCE/SEI 7-10 (Table 4-1)

50 psf is considered by inspection of Table 4-1 for Office Buildings – Offices (2/3 of the floor area)

80 psf is considered by inspection of Table 4-1 for Office Buildings – Corridors (1/3 of the floor area)

$LL = 2/3 \times 50 + 1/3 \times 80 = 60$ psf

$f_c' = 5000$ psi (for slab)

$f_c' = 6000$ psi (for columns)

$f_y = 60,000$ psi

Solution

1. Preliminary member sizing

For Flat Plate (without Drop Panels)

a. Slab minimum thickness – Deflection

ACI 318-14 (8.3.1.1)

In lieu of detailed calculation for deflections, ACI 318 Code gives minimum slab thickness for two-way construction without interior beams in **Table 8.3.1.1**.

For this flat plate slab systems the minimum slab thicknesses per **ACI 318-14** are:

$$\text{Exterior Panels: } h_s = \frac{l_n}{30} = \frac{340}{30} = 11.33 \text{ in.}$$

ACI 318-14 (Table 8.3.1.1)

But not less than 5 in.

ACI 318-14 (8.3.1.1(a))

$$\text{Interior Panels: } h_s = \frac{l_n}{33} = \frac{340}{33} = 10.3 \text{ in.}$$

ACI 318-14 (Table 8.3.1.1)

But not less than 5 in.

ACI 318-14 (8.3.1.1(a))

Where l_n = length of clear span in the long direction = $30 \times 12 - 20 = 340$ in.

Try 11 in. slab for all panels (self-weight = $150 \text{ pcf} \times 11 \text{ in.} / 12 = 137.5 \text{ psf}$)

b. Slab shear strength – one way shear

At a preliminary check level, the use of average effective depth would be sufficient. However, after determining the final depth of the slab, the exact effective depth will be used in flexural, shear and deflection calculations. Evaluate the average effective depth (Figure 2):

$$d_1 = h_s - c_{clear} - d_b - \frac{d_b}{2} = 11 - 0.75 - 0.75 - \frac{0.75}{2} = 9.13 \text{ in.}$$

$$d_2 = h_s - c_{clear} - \frac{d_b}{2} = 11 - 0.75 - \frac{0.75}{2} = 9.88 \text{ in.}$$

$$d_{avg} = \frac{d_1 + d_2}{2} = \frac{9.13 + 9.88}{2} = 9.51 \text{ in.}$$

Where:

$c_{clear} = 3/4$ in. for # 6 steel bar

ACI 318-14 (Table 20.6.1.3.1)

$d_b = 0.75$ in. for # 6 steel bar

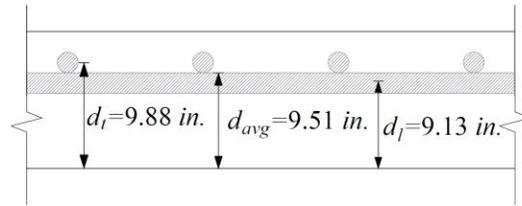


Figure 2 - Two-Way Flat Concrete Floor System

Factored dead load, $q_{Du} = 1.2 \times (137.5 + 20) = 189 \text{ psf}$

Factored live load, $q_{Lu} = 1.6 \times 60 = 96 \text{ psf}$

ACI 318-14 (5.3.1)

Total factored load, $q_u = 189 + 96 = 285 \text{ psf}$

Check the adequacy of slab thickness for beam action (one-way shear)

ACI 318-14 (22.5)

at an interior column:

Consider a 12-in. wide strip. The critical section for one-way shear is located at a distance d , from the face of support (see Figure 3):

$$\text{Tributary area for one-way shear is } A_{Tributary} = \left[\frac{30}{2} - \frac{20}{2 \times 12} - \frac{9.51}{12} \right] \times \frac{12}{12} = 13.37 \text{ ft}^2$$

$$V_u = q_u \times A_{Tributary} = 0.285 \times 13.37 = 3.81 \text{ kips}$$

$$V_c = 2\lambda\sqrt{f'_c}b_w d$$

ACI 318-14 (Eq. 22.5.5.1)

Where $\lambda = 1$ for normal weight concrete, more information can be found in “[Concrete Type Classification Based on Unit Density](#)” technical article.

$$\phi V_c = 0.75 \times 2 \times 1.0 \times \sqrt{5000} \times 12 \times \frac{9.51}{1000} = 12.09 \text{ kips} > V_u$$

Slab thickness of 11 in. is adequate for one-way shear.

c. **Slab shear strength – two-way shear**

Check the adequacy of slab thickness for punching shear (two-way shear) at an interior column (Figure 4):

$$\text{Tributary area for two-way shear is } A_{\text{Tributary}} = (30 \times 30) - \left(\frac{20 + 9.51}{12} \right)^2 = 894 \text{ ft}^2$$

$$V_u = q_u \times A_{\text{Tributary}} = 0.285 \times 894 = 254.78 \text{ kips}$$

$$V_c = 4\lambda\sqrt{f'_c}b_w d \text{ (For square interior column)}$$

ACI 318-14 (Table 22.6.5.2(a))

$$V_c = 4 \times \sqrt{5000} \times (4 \times (20 + 9.51)) \times \frac{9.51}{1000} = 317 \text{ kips}$$

$$\phi V_c = 0.75 \times 317 = 237.8 \text{ kips} < V_u$$

Slab thickness of 11 in. is not adequate for two-way shear. It is good to mention that the factored shear (V_u) used in the preliminary check does not include the effect of the unbalanced moment at supports. Including this effect will lead to an increase of V_u value as shown later in section 4.2.

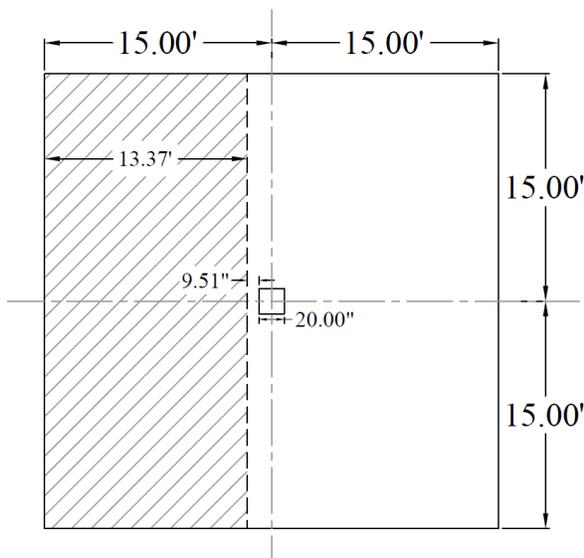


Figure 3 – Critical Section for One-Way Shear

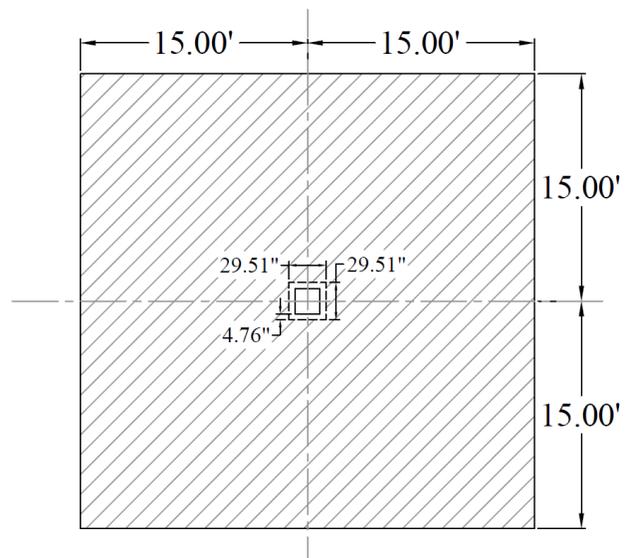


Figure 4 – Critical Section for Two-Way Shear

In this case, four options could be used: 1) to increase the slab thickness, 2) to increase columns cross sectional dimensions or cut the spacing between columns (reducing span lengths), however, this option is assumed to be not

permissible in this example due to architectural limitations, 3) to use headed shear reinforcement, or 4) to use drop panels. In this example, the latter option will be used to achieve better understanding for the design of two-way slab with drop panels often called flat slab.

Check the drop panel dimensional limitations as follows:

- 1) The drop panel shall project below the slab at least one-fourth of the adjacent slab thickness.

ACI 318-14 (8.2.4(a))

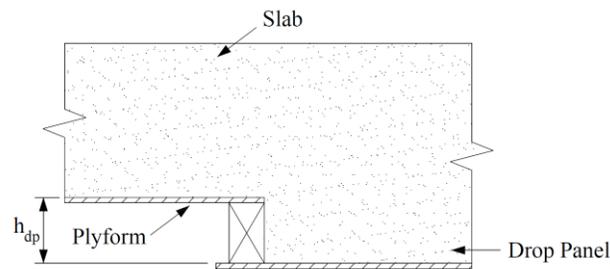
Since the slab thickness (h_s) is 10 in. (see page 6), the thickness of the drop panel should be at least:

$$h_{dp,min} = 0.25 \times h_s = 0.25 \times 10 = 2.5 \text{ in.}$$

Drop panel dimensions are also controlled by formwork considerations. The following Figure shows the standard lumber dimensions that are used when forming drop panels. Using other depths will unnecessarily increase formwork costs.

For nominal lumber size (2x), $h_{dp} = 4.25 \text{ in.} > h_{dp,min} = 2.5 \text{ in.}$

The total thickness including the slab and the drop panel (h) = $h_s + h_{dp} = 10 + 4.25 = 14.25 \text{ in.}$



| Nominal Lumber Size, in. | Actual Lumber Size, in. | Plyform Thickness, in. | h_{dp} , in. |
|--------------------------|-------------------------|------------------------|----------------|
| 2x | 1 1/2 | 3/4 | 2 1/4 |
| 4x | 3 1/2 | 3/4 | 4 1/4 |
| 6x | 5 1/2 | 3/4 | 6 1/4 |
| 8x | 7 1/4 | 3/4 | 8 |

Figure 5 – Drop Panel Formwork Details

- 2) The drop panel shall extend in each direction from the centerline of support a distance not less than one-sixth the span length measured from center-to-center of supports in that direction.

ACI 318-14 (8.2.4(b))

$$L_{1,dp} = \frac{1}{6} \times L_1 + \frac{1}{6} \times L_1 = \frac{1}{6} \times 30 + \frac{1}{6} \times 30 = 5 \text{ ft}$$

$$L_{2,dp} = \frac{1}{6} \times L_2 + \frac{1}{6} \times L_2 = \frac{1}{6} \times 30 + \frac{1}{6} \times 30 = 5 \text{ ft}$$

Based on the previous discussion, Figure 6 shows the dimensions of the selected drop panels around interior, edge (exterior), and corner columns.

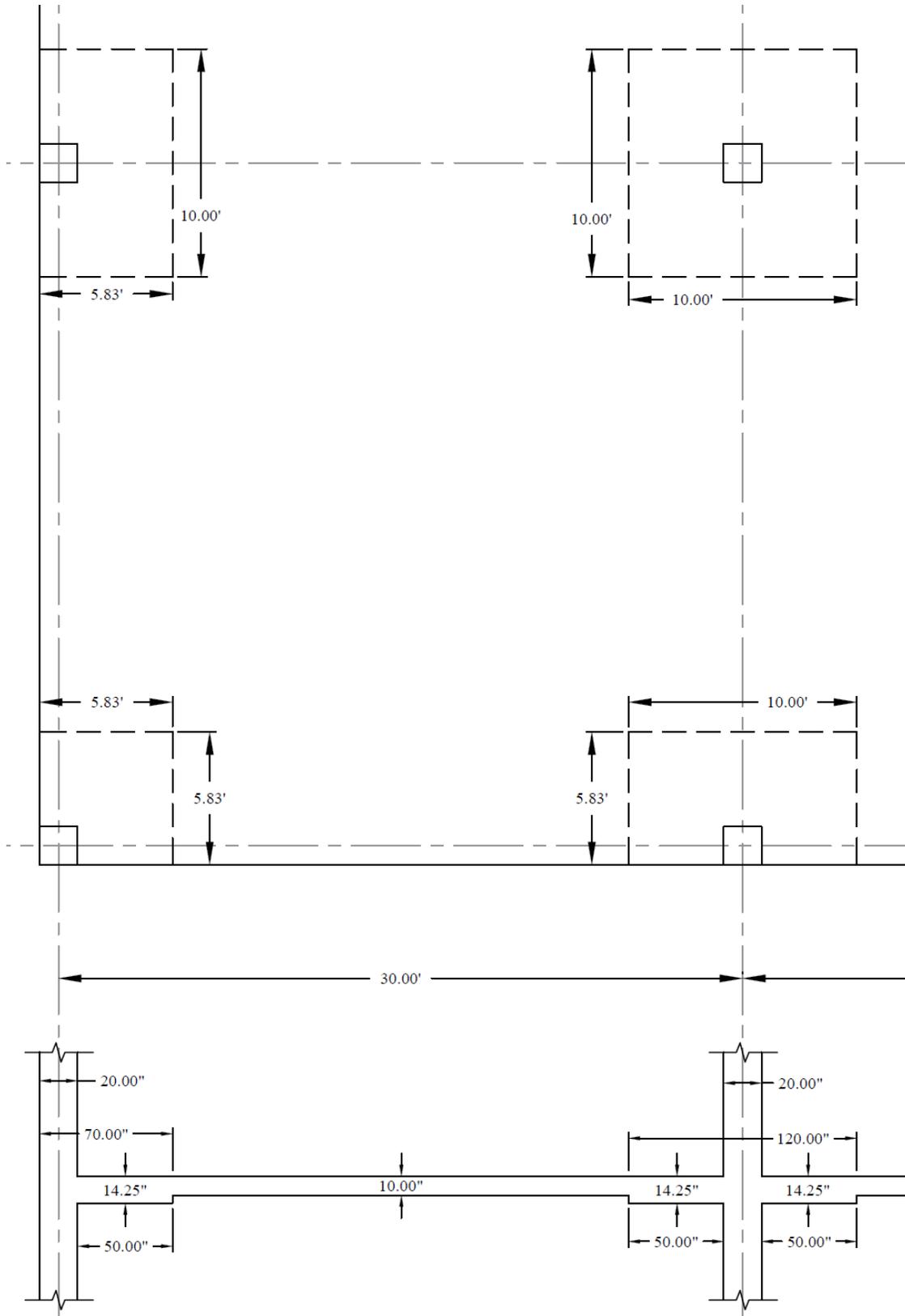


Figure 6 – Drop Panels Dimensions

For Flat Slab (with Drop Panels)

For slabs with changes in thickness and subjected to bending in two directions, it is necessary to check shear at multiple sections as defined in the **ACI 319-14**. The critical sections shall be located with respect to:

- 1) Edges or corners of columns. **ACI 318-14 (22.6.4.1(a))**
- 2) Changes in slab thickness, such as edges of drop panels. **ACI 318-14 (22.6.4.1(b))**

a. **Slab minimum thickness – Deflection** **ACI 318-14 (8.3.1.1)**

In lieu of detailed calculation for deflections, ACI 318 Code gives minimum slab thickness for two-way construction without interior beams in **Table 8.3.1.1**.

For this flat plate slab systems the minimum slab thicknesses per **ACI 318-14** are:

Exterior Panels: $h_s = \frac{l_n}{33} = \frac{340}{33} = 10.30 \text{ in.}$ **ACI 318-14 (Table 8.3.1.1)**

But not less than 4 in. **ACI 318-14 (8.3.1.1(b))**

Interior Panels: $h_s = \frac{l_n}{36} = \frac{340}{36} = 9.44 \text{ in.}$ **ACI 318-14 (Table 8.3.1.1)**

But not less than 4 in. **ACI 318-14 (8.3.1.1(b))**

Where l_n = length of clear span in the long direction = $30 \times 12 - 20 = 340 \text{ in.}$

Try 10 in. slab for all panels

Self-weight for slab section without drop panel = $150 \text{ pcf} \times 10 \text{ in.} / 12 = 125 \text{ psf}$

Self-weight for slab section with drop panel = $150 \text{ pcf} \times 14.25 \text{ in.} / 12 = 178 \text{ psf}$

b. **Slab shear strength – one way shear**

For critical section at distance d from the edge of the column (slab section with drop panel):

Evaluate the average effective depth:

$$d_l = h_s - c_{clear} - d_b - \frac{d_b}{2} = 14.25 - 0.75 - 0.75 - \frac{0.75}{2} = 12.38 \text{ in.}$$

$$d_t = h_s - c_{clear} - \frac{d_b}{2} = 14.25 - 0.75 - \frac{0.75}{2} = 13.13 \text{ in.}$$

$$d_{avg} = \frac{d_l + d_t}{2} = \frac{12.38 + 13.13}{2} = 12.75 \text{ in.}$$

Where:

$c_{clear} = 3/4 \text{ in.}$ for # 6 steel bar **ACI 318-14 (Table 20.6.1.3.1)**

$d_b = 0.75 \text{ in.}$ for # 6 steel bar

$$\text{Factored dead load} \rightarrow q_{Du} = 1.2 \times (178 + 20) = 237.6 \text{ psf}$$

$$\text{Factored live load} \rightarrow q_{Lu} = 1.6 \times 60 = 96 \text{ psf}$$

ACI 318-14 (5.3.1)

$$\text{Total factored load} \rightarrow q_u = 237.6 + 96 = 333.6 \text{ psf}$$

Check the adequacy of slab thickness for beam action (one-way shear) from the edge of the interior column

ACI 318-14 (22.5)

Consider a 12-in. wide strip. The critical section for one-way shear is located at a distance d , from the edge of the column (see Figure 7)

$$\text{Tributary area for one-way shear is } A_{Tributary} = \left[\frac{30}{2} - \frac{20}{2 \times 12} - \frac{12.75}{12} \right] \times \frac{12}{12} = 13.10 \text{ ft}^2$$

$$V_u = q_u \times A_{Tributary} = 0.334 \times 13.10 = 4.37 \text{ kips}$$

$$V_c = 2\lambda \sqrt{f'_c} b_w d$$

ACI 318-14 (Eq. 22.5.5.1)

Where $\lambda = 1$ for normal weight concrete

$$\phi V_c = 0.75 \times 2 \times 1.0 \times \sqrt{5000} \times 12 \times \frac{12.75}{1000} = 16.23 \text{ kips} > V_u$$

Slab thickness of 14.25 in. is adequate for one-way shear for the first critical section (from the edge of the column).

For critical section at the edge of the drop panel (slab section without drop panel):

Evaluate the average effective depth:

$$d_l = h_s - c_{clear} - d_b - \frac{d_b}{2} = 10 - 0.75 - 0.75 - \frac{0.75}{2} = 8.13 \text{ in.}$$

$$d_i = h_s - c_{clear} - \frac{d_b}{2} = 10 - 0.75 - \frac{0.75}{2} = 8.88 \text{ in.}$$

$$d_{avg} = \frac{d_l + d_i}{2} = \frac{8.13 + 8.88}{2} = 8.51 \text{ in.}$$

Where:

$$c_{clear} = 3/4 \text{ in. for \# 6 steel bar}$$

ACI 318-14 (Table 20.6.1.3.1)

$$d_b = 0.75 \text{ in. for \# 6 steel bar}$$

$$\text{Factored dead load} \rightarrow q_{Du} = 1.2 \times (125 + 20) = 174 \text{ psf}$$

$$\text{Factored live load} \rightarrow q_{Lu} = 1.6 \times 60 = 96 \text{ psf}$$

ACI 318-14 (5.3.1)

$$\text{Total factored load} \rightarrow q_u = 174 + 96 = 270 \text{ psf}$$

Check the adequacy of slab thickness for beam action (one-way shear) from the edge of the interior drop panel ACI 318-14 (22.5)

Consider a 12-in. wide strip. The critical section for one-way shear is located at the face of support (see Figure 7)

$$\text{Tributary area for one-way shear is } A_{Tributary} = \left[\frac{30}{2} - \frac{10}{2} \right] \times \frac{12}{12} = 10.00 \text{ ft}^2$$

$$V_u = q_u \times A_{Tributary} = 0.270 \times 10.00 = 2.70 \text{ kips}$$

$$V_c = 2\lambda\sqrt{f'_c} b_w d \quad \text{ACI 318-14 (Eq. 22.5.5.1)}$$

Where $\lambda = 1$ for normal weight concrete

$$\phi V_c = 0.75 \times 2 \times 1.0 \times \sqrt{5000} \times 12 \times \frac{8.51}{1000} = 10.82 \text{ kips} > V_u$$

Slab thickness of 10 in. is adequate for one-way shear for the second critical section (from the edge of the drop panel).

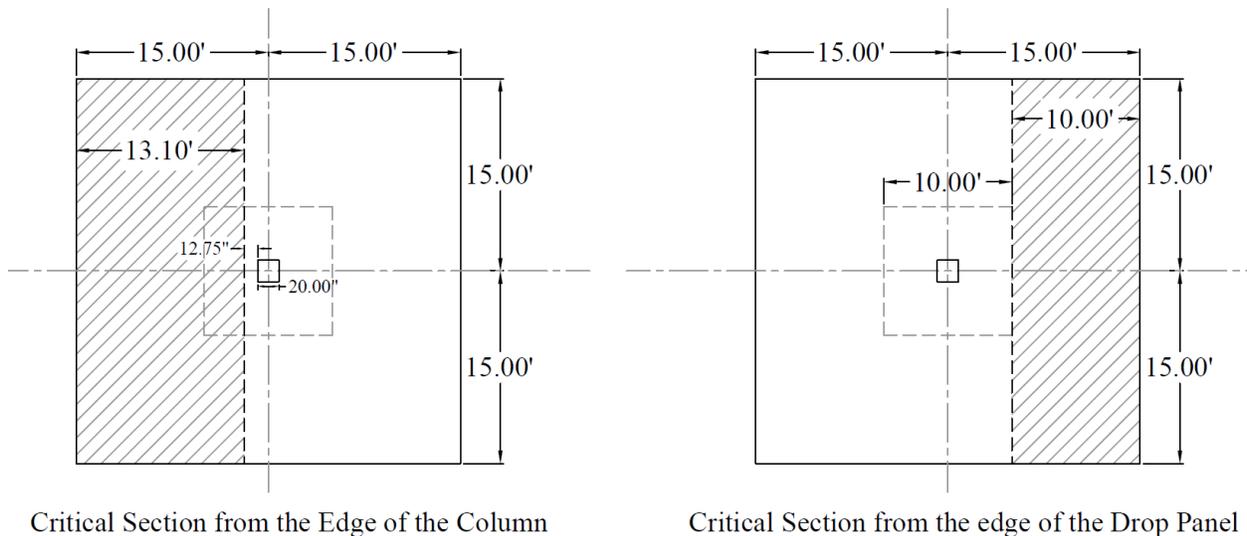


Figure 7 – Critical Sections for One-Way Shear

c. Slab shear strength – two-way shear

For critical section at distance $d/2$ from the edge of the column (slab section with drop panel):

Check the adequacy of slab thickness for punching shear (two-way shear) at an interior column (Figure 8):

$$\text{Tributary area for two-way shear is } A_{Tributary} = (30 \times 30) - \left(\frac{20 + 12.75}{12} \right)^2 = 892.6 \text{ ft}^2$$

$$V_u = q_u \times A_{Tributary} = 0.334 \times 892.6 = 297.9 \text{ kips}$$

$$V_c = 4\lambda\sqrt{f'_c} b_o d \quad \text{(For square interior column)} \quad \text{ACI 318-14 (Table 22.6.5.2(a))}$$

$$V_c = 4 \times \sqrt{5000} \times (4 \times (20 + 12.75)) \times \frac{12.75}{1000} = 472 \text{ kips}$$

$$\phi V_c = 0.75 \times 472 = 354 \text{ kips} > V_u$$

Slab thickness of 14.25 in. is adequate for two-way shear for the first critical section (from the edge of the column).

For critical section at the edge of the drop panel (slab section without drop panel):

Check the adequacy of slab thickness for punching shear (two-way shear) at an interior drop panel (Figure 8):

$$\text{Tributary area for two-way shear is } A_{Tributary} = (30 \times 30) - \left(\frac{120 + 8.51}{12} \right)^2 = 785 \text{ ft}^2$$

$$V_u = q_u \times A_{Tributary} = 0.270 \times 785 = 212 \text{ kips}$$

$$V_c = 4\lambda\sqrt{f'_c} b_o d \text{ (For square interior column)}$$

ACI 318-14 (Table 22.6.5.2(a))

$$V_c = 4 \times \sqrt{5000} \times (4 \times (120 + 8.51)) \times \frac{8.51}{1000} = 1237 \text{ kips}$$

$$\phi V_c = 0.75 \times 1237 = 928 \text{ kips} > V_u$$

Slab thickness of 10 in. is adequate for two-way shear for the second critical section (from the edge of the drop panel).

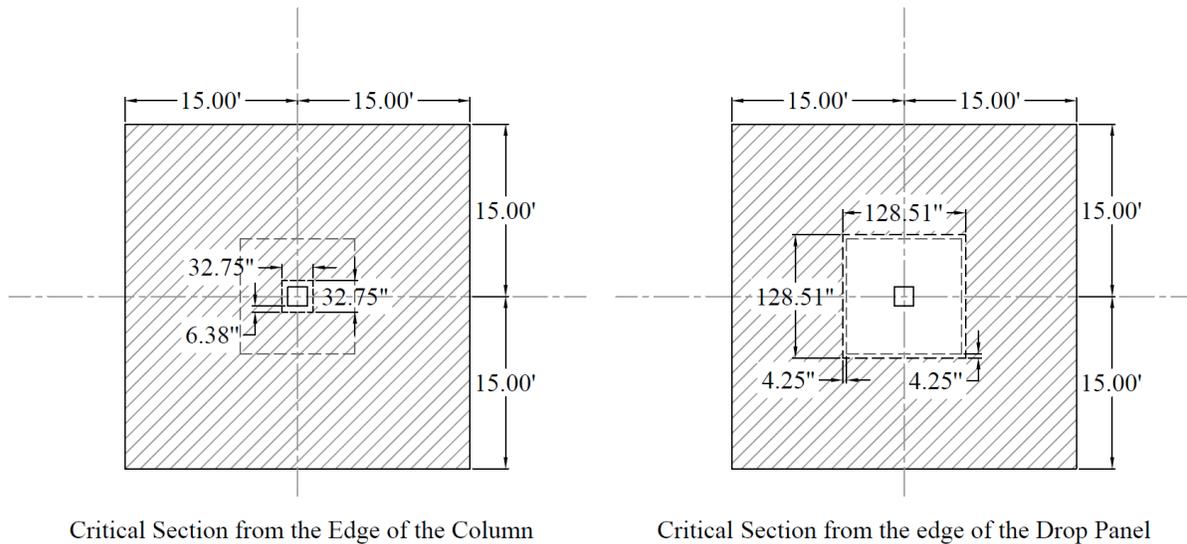


Figure 8 – Critical Sections for Two-Way Shear

d. Column dimensions - axial load

Check the adequacy of column dimensions for axial load:

Tributary area for interior column for live load, superimposed dead load, and self-weight of the slab is

$$A_{Tributary} = 30 \times 30 = 900 \text{ft}^2$$

Tributary area for interior column for self-weight of additional slab thickness due to the presence of the drop panel is

$$A_{Tributary} = 10 \times 10 = 100 \text{ft}^2$$

Assuming five story building

$$P_u = n \times q_u \times A_{Tributary} = 5 \times (0.270 \times 900 + 0.0638 \times 100) = 1247 \text{ kips}$$

Assume 20 in. square column with 4 – No. 14 vertical bars with design axial strength, $\phi P_{n,max}$ of

$$\phi P_{n,max} = 0.80 \phi (0.85 f'_c (A_g - A_{st}) + f_y A_{st}) \quad \text{ACI 318-14 (22.4.2)}$$

$$\phi P_{n,max} = 0.80 \times 0.65 \times (0.85 \times 6000 \times (20 \times 20 - 4 \times 2.25) + 60000 \times 4 \times 2.25) = 1,317,730 \text{ lbs}$$

$$\phi P_{n,max} = 1,318 \text{ kips} > P_u = 1,247 \text{ kips}$$

Column dimensions of 20 in. x 20 in. are adequate for axial load.

2. Flexural Analysis and Design

ACI 318 states that a slab system shall be designed by any procedure satisfying equilibrium and geometric compatibility, provided that strength and serviceability criteria are satisfied. Distinction of two-systems from one-way systems is given by ACI 318-14 (R8.10.2.3 & R8.3.1.2).

ACI 318 permits the use of Direct Design Method (DDM) and Equivalent Frame Method (EFM) for the gravity load analysis of orthogonal frames and is applicable to flat plates, flat slabs, and slabs with beams. The following sections outline the solution per EFM and spSlab software. For the solution per DDM, check the flat plate example.

2.1. Equivalent Frame Method (EFM)

EFM is the most comprehensive and detailed procedure provided by the ACI 318 for the analysis and design of two-way slab systems where the structure is modeled by a series of equivalent frames (interior and exterior) on column lines taken longitudinally and transversely through the building.

The equivalent frame consists of three parts (for a detailed discussion of this method, refer to [the flat plate design example](#)):

- 1) Horizontal slab-beam strip.
- 2) Columns or other vertical supporting members.

- 3) Elements of the structure (Torsional members) that provide moment transfer between the horizontal and vertical members.

2.1.1. Limitations for use of equivalent frame method

In EFM, live load shall be arranged in accordance with 6.4.3 which requires slab systems to be analyzed and designed for the most demanding set of forces established by investigating the effects of live load placed in various critical patterns. ACI 318-14 (8.11.1.2 & 6.4.3)

Complete analysis must include representative interior and exterior equivalent frames in both the longitudinal and transverse directions of the floor. ACI 318-14 (8.11.2.1)

Panels shall be rectangular, with a ratio of longer to shorter panel dimensions, measured center-to-center of supports, not to exceed 2. ACI 318-14 (8.10.2.3)

2.1.2. Frame members of equivalent frame

Determine moment distribution factors and fixed-end moments for the equivalent frame members. The moment distribution procedure will be used to analyze the equivalent frame. Stiffness factors k , carry over factors COF, and fixed-end moment factors FEM for the slab-beams and column members are determined using the design aids tables at Appendix 20A of PCA Notes on ACI 318-11. These calculations are shown below.

- a. Flexural stiffness of slab-beams at both ends, K_{sb} .

$$\frac{c_{N1}}{\ell_1} = \frac{20}{(30 \times 12)} = 0.056, \quad \frac{c_{N2}}{\ell_2} = \frac{20}{(30 \times 12)} = 0.056$$

For $c_{F1} = c_{N1}$, stiffness factors, $k_{NF} = k_{FN} = 5.59$

PCA Notes on ACI 318-11 (Table A1)

$$\text{Thus, } K_{sb} = k_{NF} \frac{E_{cs} I_s}{\ell_1} = 5.59 \frac{E_{cs} I_s}{\ell_1}$$

PCA Notes on ACI 318-11 (Table A1)

$$K_{sb} = 5.59 \times 4287 \times 10^3 \times \frac{30,000}{360} = 1,997 \times 10^6 \text{ in.-lb}$$

$$\text{Where, } I_s = \frac{\ell_s h^3}{12} = \frac{360 \times (10)^3}{12} = 30,000 \text{ in.}^4$$

$$E_{cs} = w_c^{1.5} 33 \sqrt{f'_c} = 150^{1.5} \times 33 \times \sqrt{5000} = 4287 \times 10^3 \text{ psi}$$

ACI 318-14 (19.2.2.1.a)

Carry-over factor $COF = 0.578$

PCA Notes on ACI 318-11 (Table A1)

$$\text{Fixed-end moment, } FEM = \sum_{i=1}^n m_{NFi} \times w_i \times l_i^2$$

PCA Notes on ACI 318-11 (Table A1)

Uniform load fixed end moment coefficient, $m_{NF1} = 0.0915$

Fixed end moment coefficient for (b-a) = 0.2 when a = 0, $m_{NF2} = 0.0163$

Fixed end moment coefficient for (b-a) = 0.2 when a = 0.8, $m_{NF3} = 0.0163$

b. Flexural stiffness of column members at both ends, K_c .

Referring to Table A7, Appendix 20A,

For the Bottom Column (Below):

$$t_a = 10/2 + 4.25 = 9.25 \text{ in.}, t_b = 10/2 = 5 \text{ in.}$$

$$\frac{t_a}{t_b} = \frac{9.25}{5} = 1.85$$

$$H = 13 \text{ ft} = 156 \text{ in.}, H_c = 156 \text{ in.} - 9.25 \text{ in.} - 5 \text{ in.} = 11.81 \text{ ft}$$

$$\frac{H}{H_c} = \frac{13}{11.81} = 1.101$$

Thus, $k_{AB} = 5.32$ and $C_{AB} = 0.54$ by interpolation.

$$K_{c,\text{bottom}} = \frac{5.32 E_{cc} I_c}{\ell_c}$$

PCA Notes on ACI 318-11 (Table A7)

$$K_{c,\text{bottom}} = 5.32 \times 4696 \times 10^3 \times \frac{13,333}{156} = 2135.2 \times 10^6 \text{ in.-lb}$$

$$\text{Where } I_c = \frac{c^4}{12} = \frac{(20)^4}{12} = 13,333 \text{ in.}^4$$

$$E_{cc} = w_c^{1.5} 33 \sqrt{f'_c} = 150^{1.5} \times 33 \times \sqrt{6000} = 4696 \times 10^3 \text{ psi}$$

ACI 318-14 (19.2.2.1.a)

$$\ell_c = 13 \text{ ft} = 156 \text{ in.}$$

For the Top Column (Above):

$$\frac{t_b}{t_a} = \frac{5}{9.25} = 0.54$$

$$\frac{H}{H_c} = \frac{13}{11.81} = 1.101$$

Thus, $k_{BA} = 4.88$ and $C_{BA} = 0.59$ by interpolation.

$$K_c = \frac{4.88 E_{cc} I_c}{\ell_c}$$

PCA Notes on ACI 318-11 (Table A7)

$$K_{c,\text{top}} = 4.88 \times 4696 \times 10^3 \times \frac{13,333}{156} = 1958.6 \times 10^6 \text{ in.-lb}$$

c. Torsional stiffness of torsional members, K_t .

$$K_t = \frac{9E_{cs} C}{[\ell_2 (1 - \frac{c_2}{\ell_2})^3]}$$

ACI 318-14 (R.8.11.5)

$$K_t = \frac{9 \times 4287 \times 10^3 \times 10632}{30 \times 12 \times (1 - 20 / (30 \times 12))^3} = 1353 \times 10^6 \text{ in.-lb}$$

Where $C = \sum (1 - 0.63 \frac{x}{y}) (\frac{x^3 y}{3})$

ACI 318-14 (Eq. 8.10.5.2b)

$$C = (1 - 0.63 \times \frac{14.25}{20}) (14.25^3 \times \frac{20}{3}) = 10632 \text{ in.}^4$$

$$c_2 = 20 \text{ in.}, \ell_2 = 30 \text{ ft} = 360 \text{ in.}$$

Equivalent column stiffness K_{ec} .

$$K_{ec} = \frac{\sum K_c \times \sum K_t}{\sum K_c + \sum K_t}$$

$$K_{ec} = \frac{(2135.2 + 1958.6)(2 \times 1353)}{[(2135.2 + 1958.) + (2 \times 1353)]} \times 10^6$$

$$K_{ec} = 1353 \times 10^6 \text{ in.-lb}$$

Where $\sum K_t$ is for two torsional members one on each side of the column, and $\sum K_c$ is for the upper and lower columns at the slab-beam joint of an intermediate floor.

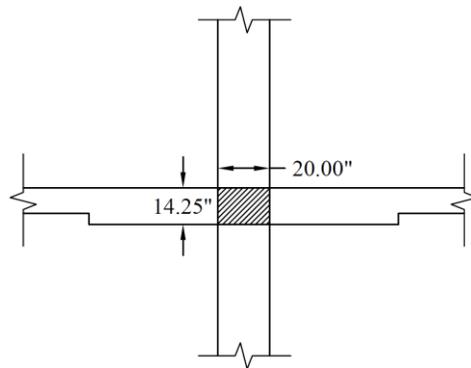


Figure 9 – Torsional Member

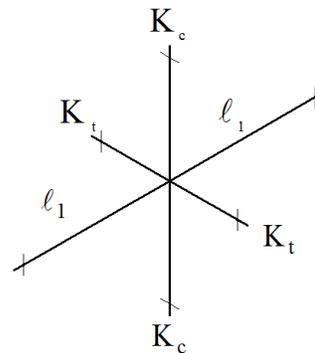


Figure 10 – Column and Edge of Slab

d. Slab-beam joint distribution factors, DF .

At exterior joint,

$$DF = \frac{1996}{(1996 + 1629)} = 0.551$$

At interior joint,

$$DF = \frac{1996}{(1996 + 1996 + 1629)} = 0.355$$

COF for slab-beam = 0.578

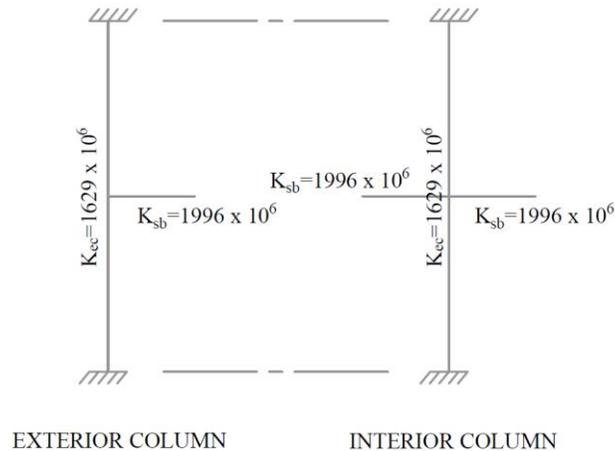


Figure 11 – Slab and Column Stiffness

2.1.3. Equivalent frame analysis

Determine negative and positive moments for the slab-beams using the moment distribution method. Since the unfactored live load does not exceed three-quarters of the unfactored dead load, design moments are assumed to occur at all critical sections with full factored live on all spans. **ACI 318-14 (6.4.3.2)**

$$\frac{L}{D} = \frac{60}{(125 + 20)} = 0.41 < \frac{3}{4}$$

- a. Factored load and Fixed-End Moments (FEM's).

For slab:

$$\text{Factored dead load } q_{Du} = 1.2(125 + 20) = 174 \text{ psf}$$

$$\text{Factored live load } q_{Lu} = 1.6(60) = 96 \text{ psf}$$

$$\text{Factored load } q_u = q_{Du} + q_{Lu} = 270 \text{ psf}$$

For drop panels:

$$\text{Factored dead load } q_{Du} = 1.2(150 \times 4.25 / 12) = 63.75 \text{ psf}$$

$$\text{Factored live load } q_{Lu} = 1.6(0) = 0 \text{ psf}$$

$$\text{Factored load } q_u = q_{Du} + q_{Lu} = 63.75 \text{ psf}$$

$$\text{Fixed-end moment, } FEM = \sum_{i=1}^n m_{NFi} \times w_i \times l_1^2$$

PCA Notes on ACI 318-11 (Table A1)

$$FEM = 0.0915 \times 0.270 \times 30 \times 30^2 + 0.0163 \times 0.064 \times 30 / 3 \times 30^2 + 0.0163 \times 0.064 \times 30 / 3 \times 30^2$$

$$FEM = 677.6 \text{ ft-kips}$$

- b. Moment distribution. Computations are shown in Table 1. Counterclockwise rotational moments acting on the member ends are taken as positive. Positive span moments are determined from the following equation:

$$M_{u, \text{midspan}} = M_o - \frac{(M_{uL} + M_{uR})}{2}$$

Where M_o is the moment at the midspan for a simple beam.

When the end moments are not equal, the maximum moment in the span does not occur at the midspan, but its value is close to that midspan for this example.

Positive moment in span 1-2:

$$M_u = (0.270 \times 30) \frac{30^2}{8} + 2 \times \left[\frac{(0.064 \times 30/6) \times 30/6}{2 \times 30} \times 30/6 \times (30 - 30/2) \right] - \frac{(331.7 + 807.6)}{2}$$

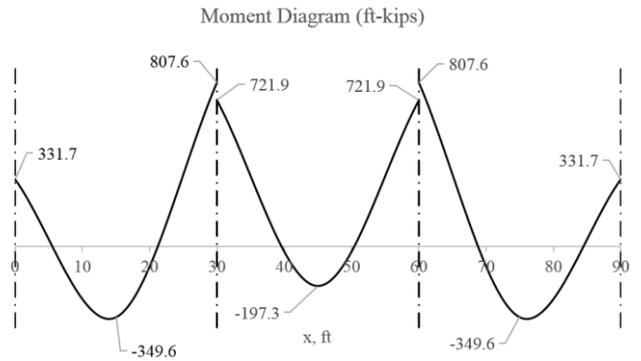
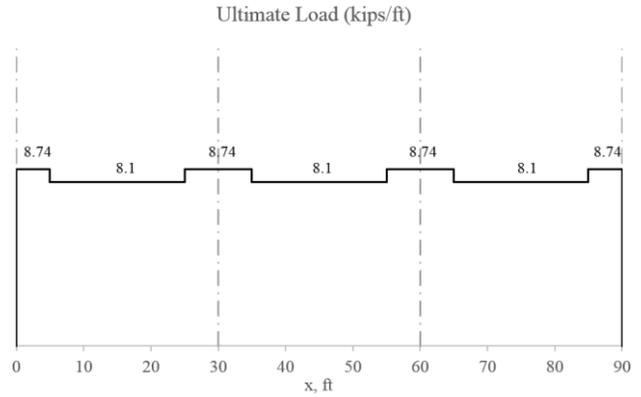
$$M_u = 349.6 \text{ ft-kips}$$

| Table 1 - Moment Distribution for Equivalent Frame | | | | | | |
|--|--------|--------|-------|--------|-------|--------|
| | | | | | | |
| Joint | 1 | 2 | | 3 | | 4 |
| Member | 1-2 | 2-1 | 2-3 | 3-2 | 3-4 | 4-3 |
| DF | 0.551 | 0.355 | 0.355 | 0.355 | 0.355 | 0.551 |
| COF | 0.578 | 0.578 | 0.578 | 0.578 | 0.578 | 0.578 |
| FEM | 677.6 | -677.6 | 677.6 | -677.6 | 677.6 | -677.6 |
| Dist | -373.1 | 0.0 | 0.0 | 0.0 | 0.0 | 373.1 |
| CO | 0.0 | -215.7 | 0.0 | 0.0 | 215.7 | 0.0 |
| Dist | 0.0 | 76.6 | 76.6 | -76.6 | -76.6 | 0.0 |
| CO | 44.3 | 0.0 | -44.3 | 44.3 | 0.0 | -44.3 |
| Dist | -24.4 | 15.7 | 15.7 | -15.7 | -15.7 | 24.4 |
| CO | 9.1 | -14.1 | -9.1 | 9.1 | 14.1 | -9.1 |
| Dist | -5.0 | 8.2 | 8.2 | -8.2 | -8.2 | 5.0 |
| CO | 4.8 | -2.9 | -4.8 | 4.8 | 2.9 | -4.8 |
| Dist | -2.6 | 2.7 | 2.7 | -2.7 | -2.7 | 2.6 |
| CO | 1.6 | -1.5 | -1.6 | 1.6 | 1.5 | -1.6 |
| Dist | -0.9 | 1.1 | 1.1 | -1.1 | -1.1 | 0.9 |
| CO | 0.6 | -0.5 | -0.6 | 0.6 | 0.5 | -0.6 |
| Dist | -0.4 | 0.4 | 0.4 | -0.4 | -0.4 | 0.4 |
| CO | 0.2 | -0.2 | -0.2 | 0.2 | 0.2 | -0.2 |
| Dist | -0.1 | 0.2 | 0.2 | -0.2 | -0.2 | 0.1 |
| CO | 0.1 | -0.1 | -0.1 | 0.1 | 0.1 | -0.1 |
| Dist | -0.1 | 0.1 | 0.1 | -0.1 | -0.1 | 0.1 |
| CO | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| Dist | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| M, k-ft | 331.7 | -807.6 | 721.9 | -721.9 | 807.6 | -331.7 |
| Midspan M, ft-kips | 349.6 | | 197.4 | | 349.6 | |

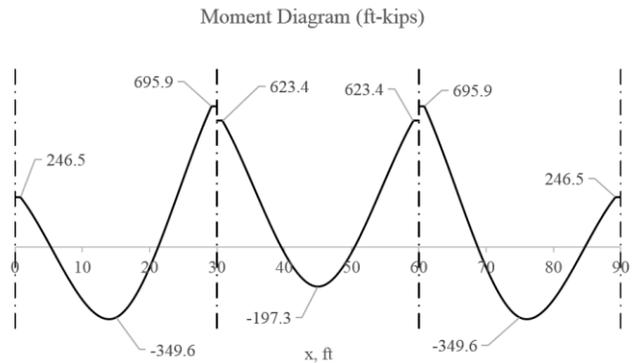
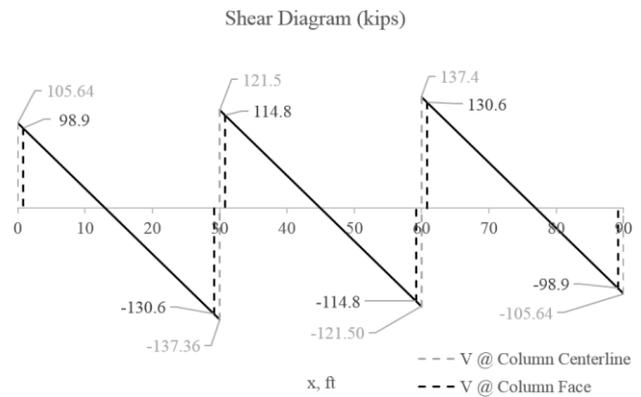
2.1.4. Factored moments used for Design

Positive and negative factored moments for the slab system in the direction of analysis are plotted in Figure 12. The negative moments used for design are taken at the faces of supports (rectangle section or equivalent rectangle for circular or polygon sections) but not at distances greater than $0.175 l_1$ from the centers of supports. *ACI 318-14 (8.11.6.1)*

$$\frac{20 \text{ in.}}{12 \times 2} = 0.83 \text{ ft} < 0.175 \times 30 = 5.25 \text{ ft (use face of supporting location)}$$



* Moment values at columns centerlines



* Moment values at columns faces

Figure 12 - Positive and Negative Design Moments for Slab-Beam (All Spans Loaded with Full Factored Live Load)

2.1.5. Factored moments in slab-beam strip

a. Check whether the moments calculated above can take advantage of the reduction permitted by ACI 318-14 (8.11.6.5):

If the slab system analyzed using EFM within the limitations of ACI 318-14 (8.10.2), it is permitted by the ACI code to reduce the calculated moments obtained from EFM in such proportion that the absolute sum of the positive and average negative design moments need not exceed the total static moment M_o given by Equation 8.10.3.2 in the ACI 318-14.

Check Applicability of Direct Design Method:

1. There is a minimum of three continuous spans in each direction. ACI 318-14 (8.10.2.1)
2. Successive span lengths are equal. ACI 318-14 (8.10.2.2)
3. Long-to-Short ratio is $30/30 = 1.0 < 2.0$. ACI 318-14 (8.10.2.3)
4. Column are not offset. ACI 318-14 (8.10.2.4)
5. Loads are gravity and uniformly distributed with service live-to-dead ratio of $0.41 < 2.0$

(Note: The self-weight of the drop panels is not uniformly distributed entirely along the span. However, the variation in load magnitude is small).

ACI 318-14 (8.10.2.5 and 6)

6. Check relative stiffness for slab panel. ACI 318-14 (8.10.2.7)

Slab system is without beams and this requirement is not applicable.

All limitation of ACI 318-14 (8.10.2) are satisfied and the provisions of ACI 318-14 (8.11.6.5) may be applied:

$$M_o = \frac{q_u \ell_n^2}{8} = 0.270 \times 30 \times \frac{(30 - 20/12)^2}{8} = 812.8 \text{ ft-kips} \quad \text{ACI 318-14 (Eq. 8.10.3.2)}$$

$$\text{End spans: } 349.6 + \frac{331.7 + 807.6}{2} = 919.3 \text{ ft-kips}$$

$$\text{Interior span: } 197.3 + \frac{721.9 + 721.9}{2} = 919.2 \text{ ft-kips}$$

To illustrate proper procedure, the interior span factored moments may be reduced as follows:

$$\text{Permissible reduction} = 812.8/919.3 = 0.884$$

$$\text{Adjusted negative design moment} = 721.9 \times 0.884 = 638.2 \text{ ft-kips}$$

$$\text{Adjusted positive design moment} = 197.3 \times 0.884 = 174.4 \text{ ft-kips}$$

$$M_o = 174.4 + \frac{638.2 + 638.2}{2} = 812.8 \text{ ft-kips}$$

ACI 318 allows the reduction of the moment values based on the previous procedure. Since the drop panels may cause gravity loads not to be uniform (Check limitation #5 and Figure 12), the moment values obtained from EFM will be used for comparison reasons.

b. Distribute factored moments to column and middle strips:

After the negative and positive moments have been determined for the slab-beam strip, the ACI code permits the distribution of the moments at critical sections to the column strips, beams (if any), and middle strips in accordance with the DDM. **ACI 318-14 (8.11.6.6)**

Distribution of factored moments at critical sections is summarized in Table 2.

| | | Slab-beam Strip | Column Strip | | Middle Strip | |
|---------------|-------------------|------------------|--------------|------------------|--------------|------------------|
| | | Moment (ft-kips) | Percent | Moment (ft-kips) | Percent | Moment (ft-kips) |
| End Span | Exterior Negative | 246.5 | 100 | 246.5 | 0 | 0.0 |
| | Positive | 349.6 | 60 | 209.8 | 40 | 139.8 |
| | Interior Negative | 695.9 | 75 | 521.9 | 25 | 174.0 |
| Interior Span | Negative | 623.4 | 75 | 467.6 | 25 | 155.9 |
| | Positive | 197.3 | 60 | 118.4 | 40 | 78.9 |

2.1.6. Flexural reinforcement requirements

a. Determine flexural reinforcement required for strip moments

The flexural reinforcement calculation for the column strip of end span – exterior negative location is provided below.

$$M_u = 246.5 \text{ ft-kips}$$

Use $d_{avg} = 12.75 \text{ in.}$

To determine the area of steel, assumptions have to be made whether the section is tension or compression controlled, and regarding the distance between the resultant compression and tension forces along the slab section (jd). In this example, tension-controlled section will be assumed so the reduction factor ϕ is equal to 0.9, and jd will be taken equal to $0.95d$. The assumptions will be verified once the area of steel is finalized.

Assume $jd = 0.95 \times d = 12.11 \text{ in.}$

Column strip width, $b = (30 \times 12) / 2 = 180 \text{ in.}$

Middle strip width, $b = 30 \times 12 - 180 = 180 \text{ in.}$

$$A_s = \frac{M_u}{\phi f_y jd} = \frac{246.5 \times 12000}{0.9 \times 60000 \times 12.11} = 4.52 \text{ in.}^2$$

$$\text{Recalculate 'a' for the actual } A_s = 4.52 \text{ in.}^2 \rightarrow a = \frac{A_s f_y}{0.85 f'_c b} = \frac{5.09 \times 60000}{0.85 \times 5000 \times 180} = 0.355 \text{ in.}$$

$$c = \frac{a}{\beta_1} = \frac{0.355}{0.85} = 0.417 \text{ in.}$$

$$\varepsilon_t = \left(\frac{0.003}{c}\right)d_t - 0.003 = \left(\frac{0.003}{0.417}\right) \times 12.75 - 0.003 = 0.089 > 0.005$$

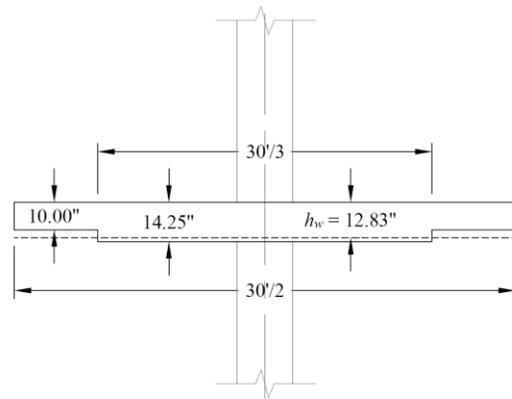
Therefore, the assumption that section is tension-controlled is valid.

$$A_s = \frac{M_u}{\phi f_y (d - a/2)} = \frac{246.5 \times 12000}{0.9 \times 60000 \times (12.75 - 0.355/2)} = 4.357 \text{ in.}^2$$

The slab have two thicknesses in the column strip (14.25 in. for the slab with the drop panel and 10 in. for the slab without the drop panel).

The weighted slab thickness:

$$h_w = \frac{14.25 \times (30/3) + 10 \times (30/2 - 30/3)}{(30/3) + (30/2 - 30/3)} = 12.83 \text{ in.}$$



$$A_{s,\min} = 0.0018 \times 180 \times 12.83 = 4.157 \text{ in.}^2 < 4.357 \text{ in.}^2$$

ACI 318-14 (24.4.3.2)

$$s_{\max} = 2h_w = 2 \times 12.83 = 25.66 \text{ in.} > 18 \text{ in.}$$

ACI 318-14 (8.7.2.2)

$$s_{\max} = 18 \text{ in.}$$

Provide 10 - #6 bars with $A_s = 4.40 \text{ in.}^2$ and $s = 180/10 = 18 \text{ in.} \leq s_{\max}$

Based on the procedure outlined above, values for all span locations are given in Table 3.

| Table 3 - Required Slab Reinforcement for Flexure [Equivalent Frame Method (EFM)] | | | | | | | | |
|---|-------------------|--------------------|------------|------------|--|----------------------------------|---------------------------|--|
| Span Location | | M_u (ft-kips) | b (in.) | d (in.) | A_s Req'd for flexure (in. ²) | Min A_s (in. ²) | Reinforcement Provided | A_s Prov. for flexure (in. ²) |
| End Span | | | | | | | | |
| Column Strip | Exterior Negative | 246.5 | 180 | 12.75 | 4.357 | 4.157 | 10-#6 | 4.40 |
| | Positive | 209.8 | 180 | 8.50 | 5.631 | 3.240 | 13-#6 | 5.72 |
| | Interior Negative | 521.9 | 180 | 12.75 | 9.366 | 4.157 | 22-#6 | 9.68 |
| Middle Strip | Exterior Negative | 0.0 | 180 | 8.50 | 0.0 | 3.240 | 10-#6 *** | 4.40 |
| | Positive | 139.8 | 180 | 8.50 | 3.719 | 3.240 | 10-#6 ** | 4.40 |
| | Interior Negative | 174.0 | 180 | 8.50 | 4.649 | 3.240 | 11-#6 | 4.84 |
| Interior Span | | | | | | | | |
| Column Strip | Positive | 118.4 | 180 | 8.50 | 3.141 | 3.240 | 10-#6 *** | 4.40 |
| Middle Strip | Positive | 78.9 | 180 | 8.50 | 2.083 | 3.240 | 10-#6 *** | 4.40 |
| * Design governed by minimum reinforcement. | | | | | | | | |
| ** Number of bars governed by maximum allowable spacing. | | | | | | | | |

- b. Calculate additional slab reinforcement at columns for moment transfer between slab and column by flexure

The factored slab moment resisted by the column ($\gamma_f \times M_{sc}$) shall be assumed to be transferred by flexure. Concentration of reinforcement over the column by closer spacing or additional reinforcement shall be used to resist this moment. The fraction of slab moment not calculated to be resisted by flexure shall be assumed to be resisted by eccentricity of shear. ACI 318-14 (8.4.2.3)

Portion of the unbalanced moment transferred by flexure is $\gamma_f \times M_{sc}$ ACI 318-14 (8.4.2.3.1)

Where

$$\gamma_f = \frac{1}{1 + (2/3) \times \sqrt{b_1 / b_2}} \quad \text{ACI 318-14 (8.4.2.3.2)}$$

b_1 = Dimension of the critical section b_o measured in the direction of the span for which moments are determined in ACI 318, Chapter 8 (see Figure 13).

b_2 = Dimension of the critical section b_o measured in the direction perpendicular to b_1 in ACI 318, Chapter 8 (see Figure 13).

b_b = Effective slab width = $c_2 + 3 \times h$ ACI 318-14 (8.4.2.3.3)

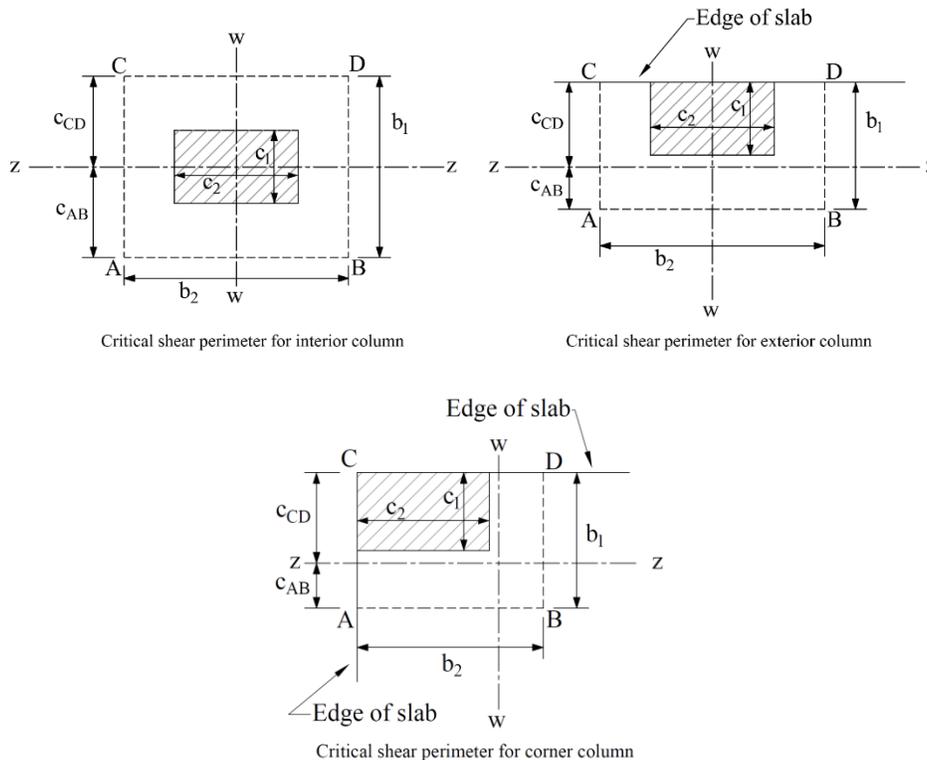


Figure 13 – Critical Shear Perimeters for Columns

For exterior support:

$$d = h - \text{cover} - d/2 = 14.25 - 0.75 - 0.75/2 = 13.13 \text{ in.}$$

$$b_1 = c_1 + d/2 = 20 + 13.13/2 = 26.56 \text{ in.}$$

$$b_2 = c_2 + d = 20 + 13.13 = 33.13 \text{ in.}$$

$$b_b = 20 + 3 \times 14.25 = 62.75 \text{ in.}$$

$$\gamma_f = \frac{1}{1 + (2/3) \times \sqrt{26.56/33.13}} = 0.626$$

$$\gamma_f M_{sc} = 0.626 \times 331.7 = 207.7 \text{ ft-kips}$$

Using the same procedure in 2.1.7.a, the required area of steel:

$$A_s = 3.63 \text{ in.}^2$$

However, the area of steel provided to resist the flexural moment within the effective slab width b_b :

$$A_{s,provided} = 4.40 \times \frac{62.75}{180} = 1.534 \text{ in.}^2$$

Then, the required additional reinforcement at exterior column for moment transfer between slab and column:

$$A_{s,additional} = 3.63 - 1.534 = 2.096 \text{ in.}^2$$

Provide 5 - #6 additional bars with $A_s = 2.20 \text{ in.}^2$

Based on the procedure outlined above, values for all supports are given in Table 4.

| Table 4 - Additional Slab Reinforcement required for moment transfer between slab and column (EFM) | | | | | | | | | |
|--|-------------------|-------------------------|------------|--------------------------------|---|------------|--|--|-----------------|
| Span Location | | M_{sc}^* (ft-kips) | γ_f | $\gamma_f M_{sc}$ (ft-kips) | Effective slab width, b_b (in.) | d (in.) | A_s req'd within b_b (in. ²) | A_s prov. For flexure within b_b (in. ²) | Add'l Reinf. |
| End Span | | | | | | | | | |
| Column Strip | Exterior Negative | 331.7 | 0.626 | 207.7 | 62.75 | 13.13 | 3.63 | 1.534 | 5-#6 |
| | Interior Negative | 85.7 | 0.60 | 51.42 | 62.75 | 13.13 | 0.877 | 3.375 | - |

* M_{sc} is taken at the centerline of the support in Equivalent Frame Method solution.

2.1.7. Factored moments in columns

The unbalanced moment from the slab-beams at the supports of the equivalent frame are distributed to the support columns above and below the slab-beam in proportion to the relative stiffness of the support columns.

Referring to Figure 12, the unbalanced moment at the exterior and interior joints are:

$$\text{Exterior Joint} = +331.7 \text{ ft-kips}$$

$$\text{Joint 2} = -807.6 + 721.9 = -85.7 \text{ ft-kips}$$

The stiffness and carry-over factors of the actual columns and the distribution of the unbalanced slab moments (M_{sc}) to the exterior and interior columns are shown in Figure 14.

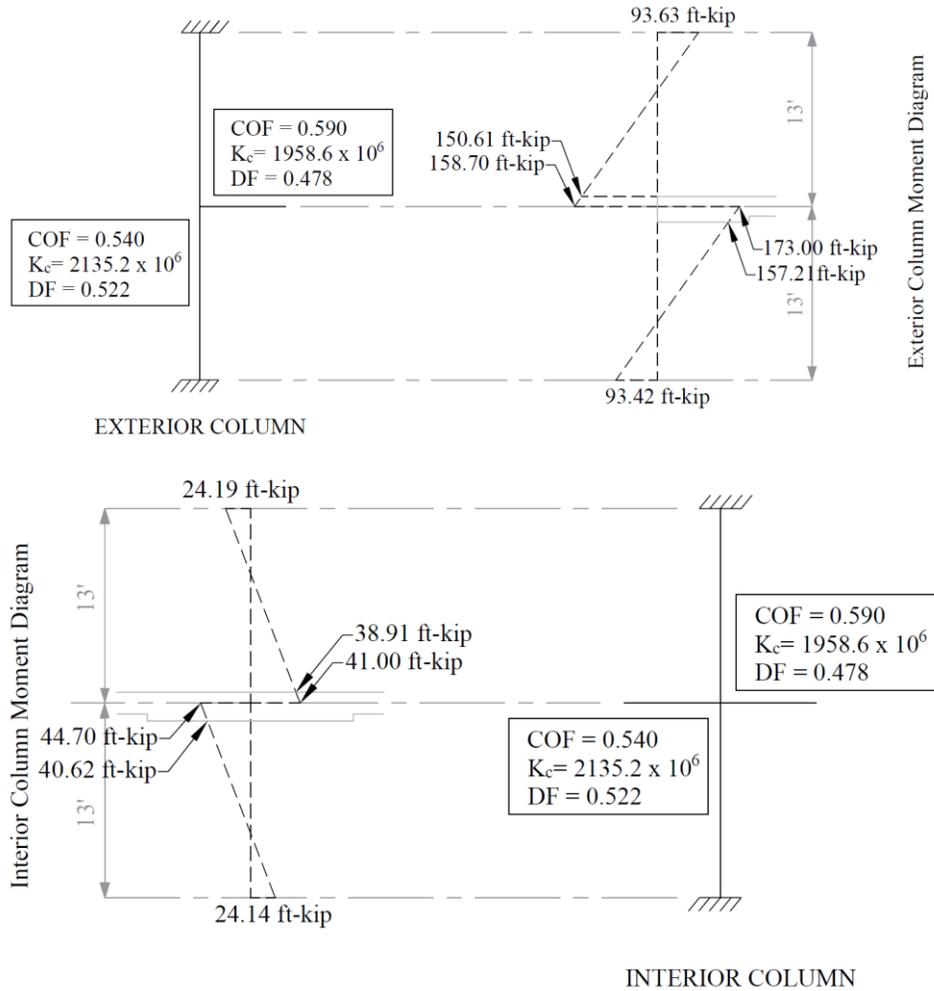


Figure 14 - Column Moments (Unbalanced Moments from Slab-Beam)

In summary:

For Top column (Above):

$$M_{col,Exterior} = 150.61 \text{ ft-kips}$$

$$M_{col,Interior} = 38.91 \text{ ft-kips}$$

For Bottom column (Below):

$$M_{col,Exterior} = 157.21 \text{ ft-kips}$$

$$M_{col,Interior} = 40.62 \text{ ft-kips}$$

The moments determined above are combined with the factored axial loads (for each story) and factored moments in the transverse direction for design of column sections. The moment values at the face of interior, exterior, and corner columns from the unbalanced moment values are shown in the following table.

| Table 5 – Factored Moments in Columns | | | |
|---------------------------------------|-----------------|----------|--------|
| M _u kips-ft | Column Location | | |
| | Interior | Exterior | Corner |
| M _{ux} | 40.62 | 157.21 | 157.21 |
| M _{uy} | 40.62 | 40.62 | 157.21 |

3. Design of Columns by spColumn

This section includes the design of interior, edge, and corner columns using [spColumn](#) software. The preliminary dimensions for these columns were calculated previously in section one. The reduction of live load per [ASCE 7-10](#) will be ignored in this example. However, the detailed procedure to calculate the reduced live loads is explained in the “[wide-Module Joist System](#)” example.

3.1. Determination of factored loads

Interior Column:

Assume 5 story building

Tributary area for interior column for live load, superimposed dead load, and self-weight of the slab is

$$A_{Tributary} = 30 \times 30 = 900 \text{ ft}^2$$

Tributary area for interior column for self-weight of additional slab thickness due to the presence of the drop panel is

$$A_{Tributary} = 10 \times 10 = 100 \text{ ft}^2$$

Assuming five story building

$$P_u = n \times q_u \times A_{Tributary} = 5 \times (0.270 \times 900 + 0.0638 \times 100) = 1247 \text{ kips}$$

$M_{u,x} = 40.62$ ft-kips (see the previous Table)

$M_{u,y} = 40.62$ ft-kips (see the previous Table)

Edge (Exterior) Column:

Tributary area for edge column for live load, superimposed dead load, and self-weight of the slab is

$$A_{Tributary} = \left(\frac{30}{2} + \frac{20/2}{12} \right) \times 30 = 475 \text{ ft}^2$$

Tributary area for edge column for self-weight of additional slab thickness due to the presence of the drop panel is

$$A_{Tributary} = \left(\frac{10}{2} + \frac{20/2}{12} \right) \times 10 = 58.33 \text{ ft}^2$$

$$P_u = n \times q_u \times A_{Tributary} = 5 \times (0.270 \times 475 + 0.0638 \times 58.33) = 660 \text{ kips}$$

$M_{u,x} = 157.21$ ft-kips (see the previous Table)

$$M_{u,y} = 40.62 \text{ ft-kips (see the previous Table)}$$

Corner Column:

Tributary area for corner column for live load, superimposed dead load, and self-weight of the slab is

$$A_{Tributary} = \left(\frac{30}{2} + \frac{20/2}{12} \right) \times \left(\frac{30}{2} + \frac{20/2}{12} \right) = 251 \text{ ft}^2$$

Tributary area for corner column for self-weight of additional slab thickness due to the presence of the drop panel is

$$A_{Tributary} = \left(\frac{10}{2} + \frac{20/2}{12} \right) \times \left(\frac{10}{2} + \frac{20/2}{12} \right) = 34.03 \text{ ft}^2$$

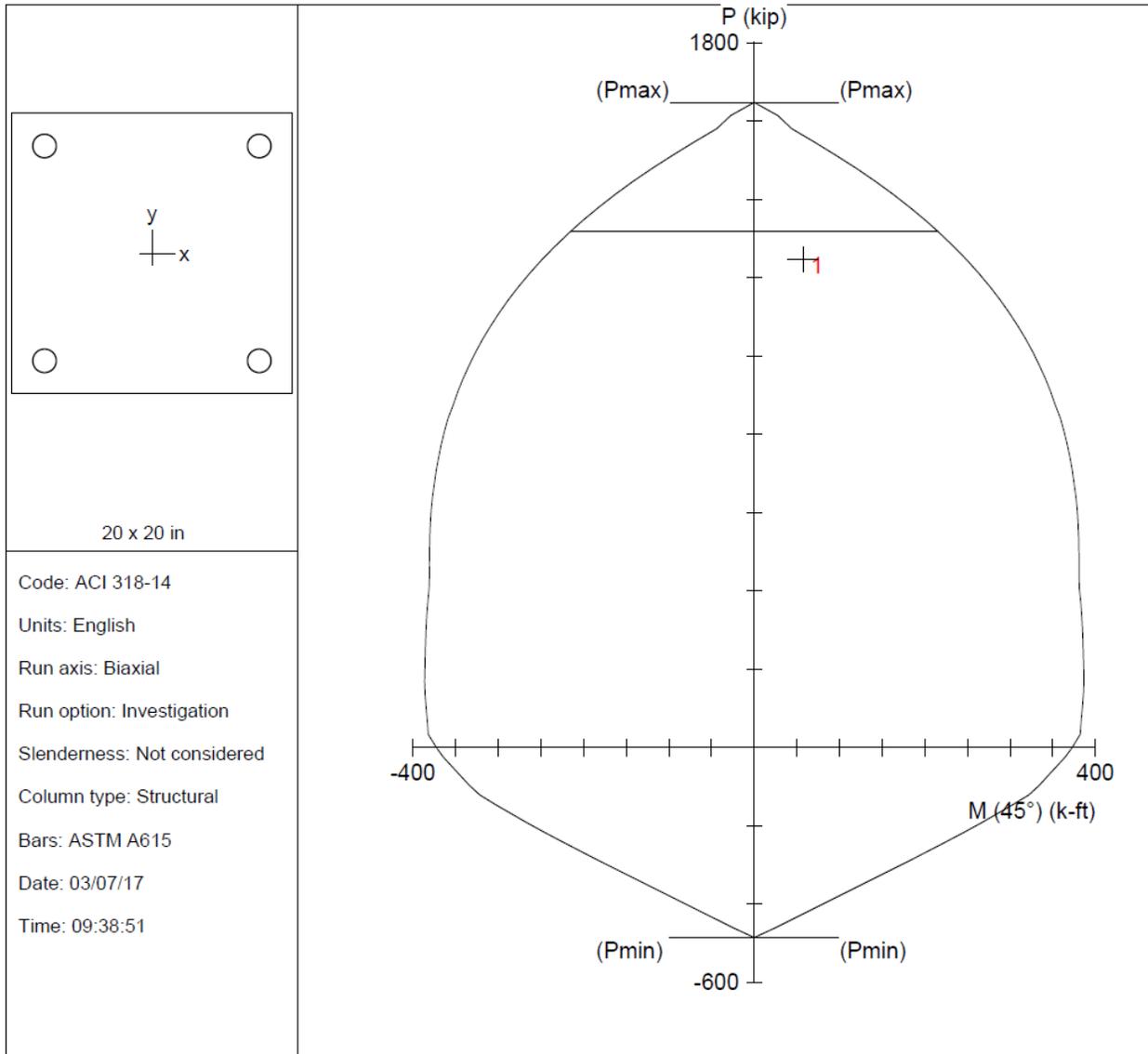
$$P_u = n \times q_u \times A_{Tributary} = 5 \times (0.270 \times 251 + 0.0638 \times 34.03) = 350 \text{ kips}$$

$$M_{u,x} = 157.21 \text{ ft-kips (see the previous Table)}$$

$$M_{u,y} = 157.21 \text{ ft-kips (see the previous Table)}$$

3.2. Moment Interaction Diagram

Interior Column:



Code: ACI 318-14
Units: English
Run axis: Biaxial
Run option: Investigation
Slenderness: Not considered
Column type: Structural
Bars: ASTM A615
Date: 03/07/17
Time: 09:38:51

STRUCTUREPOINT - spColumn v5.50 (TM). Licensed to: StructurePoint. License ID: 00000-0000000-4-25EF2-2C6B6

File: C:\TSDA\Two-Way Slab System with Drop Panels\Interior Column.col

Project: Drop Panel Example

Column: Interior

Engineer: SP

$f_c = 6$ ksi

$f_y = 60$ ksi

$A_g = 400$ in²

4 #14 bars

$E_c = 4415$ ksi

$E_s = 29000$ ksi

$A_s = 9.00$ in²

$\rho = 2.25\%$

$f_c = 5.1$ ksi

$e_{yt} = 0.00206897$ in/in

$X_o = 0.00$ in

$I_x = 13333.3$ in⁴

$e_u = 0.003$ in/in

$Y_o = 0.00$ in

$I_y = 13333.3$ in⁴

Beta1 = 0.75

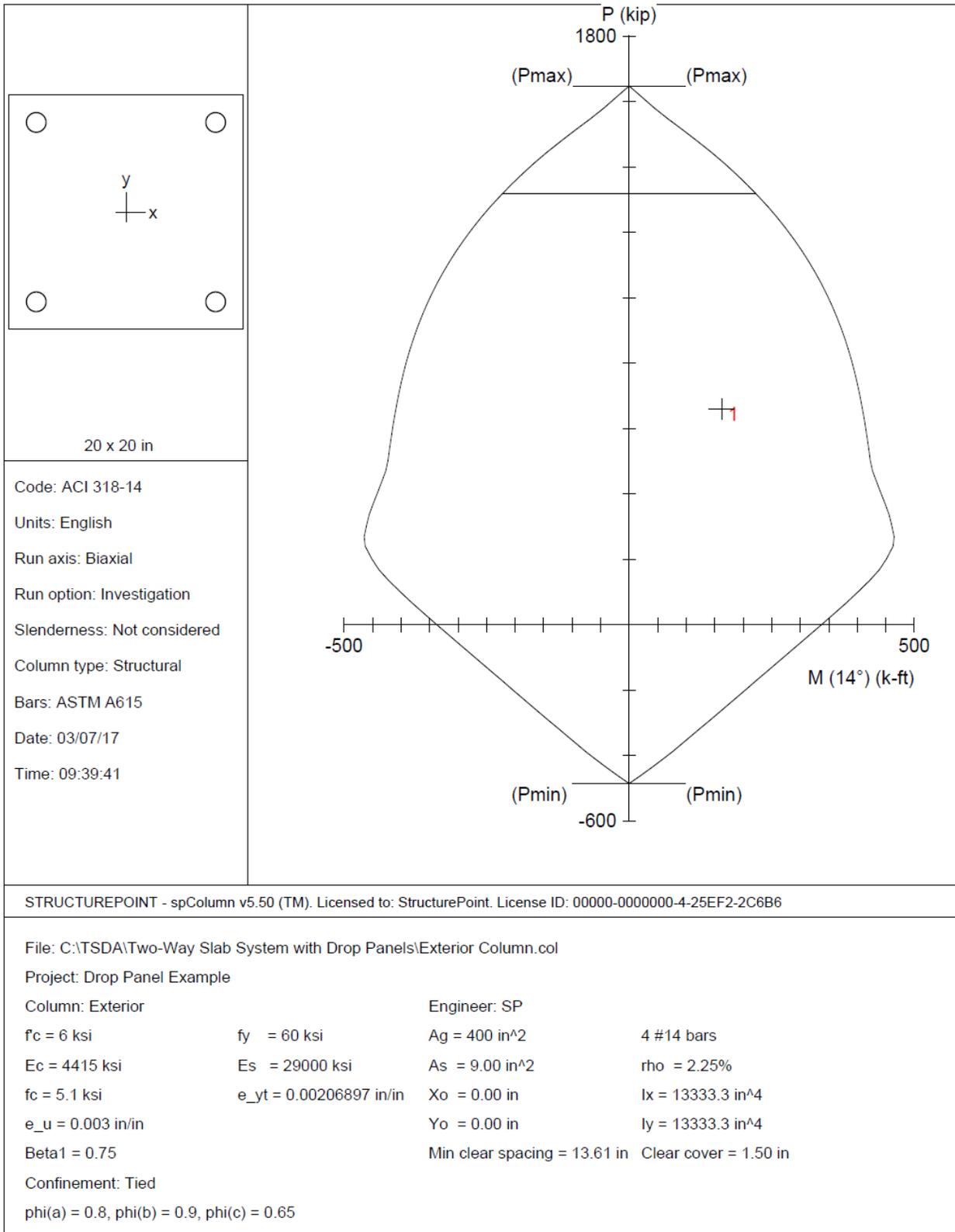
Min clear spacing = 13.61 in

Clear cover = 1.50 in

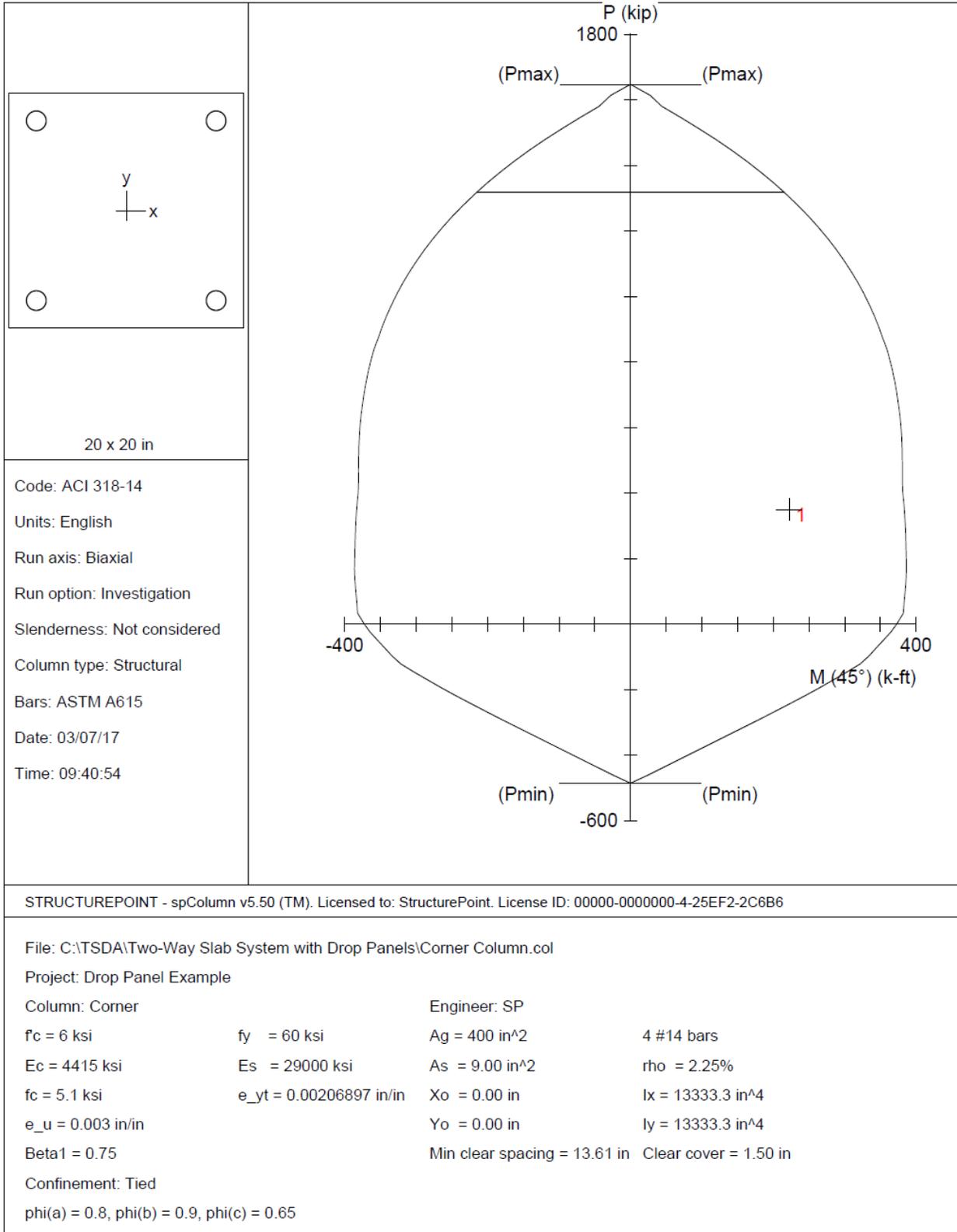
Confinement: Tied

$\phi(a) = 0.8$, $\phi(b) = 0.9$, $\phi(c) = 0.65$

Edge Column:



Corner Column:



4. Shear Strength

Shear strength of the slab in the vicinity of columns/supports includes an evaluation of one-way shear (beam action) and two-way shear (punching) in accordance with ACI 318 Chapter 22.

4.1. One-Way (Beam action) Shear Strength

ACI 318-14 (22.5)

One-way shear is critical at a distance d from the face of the column as shown in Figure 3. Figures 15 and 16 show the factored shear forces (V_u) at the critical sections around each column and each drop panel, respectively. In members without shear reinforcement, the design shear capacity of the section equals to the design shear capacity of the concrete:

$$\phi V_n = \phi V_c + \phi V_s = \phi V_c, \quad (\phi V_s = 0) \quad \text{ACI 318-14 (Eq. 22.5.1.1)}$$

Where:

$$\phi V_c = \phi 2\lambda \sqrt{f'_c} b_w d \quad \text{ACI 318-14 (Eq. 22.5.5.1)}$$

Note: The calculations below follow one of two possible approaches for checking one-way shear. Refer to the conclusions section for a comparison with the other approach.

4.1.1. At distance d from the supporting column

$$h_{\text{weighted}} = \frac{14.25 \times 30 / 6 + 10 \times (30 - 30 / 6)}{30} = 11.42 \text{ in.}$$

$$d_w = 11.42 - 0.75 - 0.75 / 2 = 10.29 \text{ in.}$$

$\lambda = 1$ for normal weight concrete

$$\phi V_c = 0.75 \times 2 \times 1.0 \times \frac{\sqrt{5000}}{1000} \times (30 \times 12) \times 10.29 = 392.91 \text{ kips}$$

Because $\phi V_c \geq V_u$ at all the critical sections, the slab has adequate one-way shear strength.

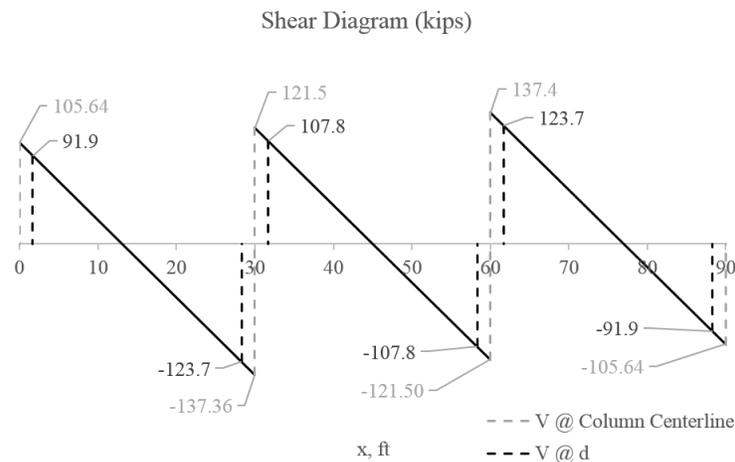


Figure 15 – One-way shear at critical sections (at distance d from the face of the supporting column)

4.1.2. At the face of the drop panel

$$h = 10 \text{ in.}$$

$$d = 10 - 0.75 - 0.75 / 2 = 8.88 \text{ in.}$$

$\lambda = 1$ for normal weight concrete

$$\phi V_c = 0.75 \times 2 \times 1.0 \times \frac{\sqrt{5000}}{1000} \times (30 \times 12) \times 8.88 = 339.1 \text{ kips}$$

Because $\phi V_c \geq V_u$ at all the critical sections, the slab has adequate one-way shear strength.

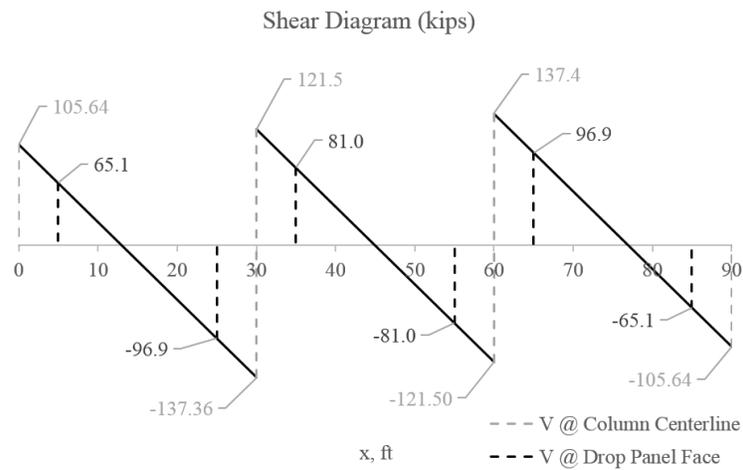


Figure 16 – One-way shear at critical sections (at the face of the drop panel)

4.2. Two-Way (Punching) Shear Strength

ACI 318-14 (22.6)

4.2.1. Around the columns faces

Two-way shear is critical on a rectangular section located at $d/2$ away from the face of the column as shown in Figure 13.

a. Exterior column:

The factored shear force (V_u) in the critical section is computed as the reaction at the centroid of the critical section minus the self-weight and any superimposed surface dead and live load acting within the critical section ($d/2$ away from column face).

$$V_u = V - q_u (b_1 \times b_2) = 105.64 - 0.334 \left(\frac{26.56 \times 33.13}{144} \right) = 103.60 \text{ kips}$$

The factored unbalanced moment used for shear transfer, M_{unb} , is computed as the sum of the joint moments to the left and right. Moment of the vertical reaction with respect to the centroid of the critical section is also taken into account.

$$M_{unb} = M - V_u (b_1 - c_{AB} - c_1 / 2) = 331.7 - 103.60 \left(\frac{26.56 - 8.18 - 20 / 2}{12} \right) = 259 \text{ ft-kips}$$

For the exterior column in Figure 13, the location of the centroidal axis z-z is:

$$c_{AB} = \frac{\text{moment of area of the sides about AB}}{\text{area of the sides}} = \frac{2(26.56 \times 13.13 \times 26.56 / 2)}{2 \times 26.56 \times 13.13 + 33.13 \times 13.13} = 8.18 \text{ in.}$$

The polar moment J_c of the shear perimeter is:

$$J_c = 2 \left(\frac{b_1 d^3}{12} + \frac{db_1^3}{12} + (b_1 d) \left(\frac{b_1}{2} - c_{AB} \right)^2 \right) + b_2 d c_{AB}^2$$

$$J_c = 2 \left(\frac{26.56 \times 13.13^3}{12} + \frac{13.13 \times 26.56^3}{12} + (26.56 \times 13.13) \left(\frac{26.56}{2} - 8.18 \right)^2 \right) + 33.13 \times 13.13 \times 8.18^2$$

$$J_c = 98,315 \text{ in.}^4$$

$$\gamma_v = 1 - \gamma_f = 1 - 0.626 = 0.374$$

ACI 318-14 (Eq. 8.4.4.2.2)

The length of the critical perimeter for the exterior column:

$$b_o = 2 \times 26.56 + 33.13 = 86.26 \text{ in.}$$

The two-way shear stress (v_u) can then be calculated as:

$$v_u = \frac{V_u}{b_o \times d} + \frac{\gamma_v M_{unb} c_{AB}}{J_c}$$

ACI 318-14 (R.8.4.4.2.3)

$$v_u = \frac{103.60 \times 1000}{86.26 \times 13.13} + \frac{0.374 \times (259 \times 12 \times 1000) \times 8.18}{98,315} = 91.47 + 96.71 = 188.3 \text{ psi}$$

$$v_c = \min \left[4\lambda\sqrt{f'_c}, \left(2 + \frac{4}{\beta} \right) \lambda\sqrt{f'_c}, \left(\frac{\alpha_s d}{b_o} + 2 \right) \lambda\sqrt{f'_c} \right]$$

ACI 318-14 (Table 22.6.5.2)

$$v_c = \min \left[4 \times 1 \times \sqrt{5000}, \left(2 + \frac{4}{1} \right) \times 1 \times \sqrt{5000}, \left(\frac{30 \times 13.13}{86.26} + 2 \right) \times 1 \times \sqrt{5000} \right]$$

$$v_c = \min [282.8, 424.3, 464.3] \text{ psi} = 282.8 \text{ psi}$$

$$\phi v_c = 0.75 \times 282.8 = 212.1 \text{ psi}$$

Since $\phi v_c \geq v_u$ at the critical section, the slab has adequate two-way shear strength at this joint.

b. Interior column:

$$V_u = V - q_u (b_1 \times b_2) = 137.36 + 121.5 - 0.334 \left(\frac{33.13 \times 33.13}{144} \right) = 256.35 \text{ kips}$$

$$M_{unb} = M - V_u (b_1 - c_{AB} - c_1 / 2) = 807.6 - 721.9 - 256.31 (0) = 85.70 \text{ ft-kips}$$

For the interior column in Figure 13, the location of the centroidal axis z-z is:

$$c_{AB} = \frac{b_1}{2} = \frac{33.13}{2} = 16.57 \text{ in.}$$

The polar moment J_c of the shear perimeter is:

$$J_c = 2 \left(\frac{b_1 d^3}{12} + \frac{db_1^3}{12} + (b_1 d) \left(\frac{b_1}{2} - c_{AB} \right)^2 \right) + 2b_2 d c_{AB}^2$$

$$J_c = 2 \left(\frac{33.13 \times 13.13^3}{12} + \frac{13.13 \times 33.13^3}{12} + (33.13 \times 13.13) \left(\frac{33.13}{2} - 16.57 \right)^2 \right) + 2 \times 33.13 \times 13.13 \times 16.57^2$$

$$J_c = 330,800 \text{ in.}^4$$

$$\gamma_v = 1 - \gamma_f = 1 - 0.600 = 0.400$$

ACI 318-14 (Eq. 8.4.4.2.2)

The length of the critical perimeter for the interior column:

$$b_o = 2 \times (33.13 + 33.13) = 132.52 \text{ in.}$$

The two-way shear stress (v_u) can then be calculated as:

$$v_u = \frac{V_u}{b_o \times d} + \frac{\gamma_v M_{unb, AB}}{J_c} \quad \text{ACI 318-14 (R.8.4.4.2.3)}$$

$$v_u = \frac{256.31 \times 1000}{132.52 \times 13.13} + \frac{0.400 \times (85.70 \times 12 \times 1000) \times 16.57}{330,800} = 147.3 + 20.6 = 167.9 \text{ psi}$$

$$v_c = \min \left[4\lambda\sqrt{f'_c}, \left(2 + \frac{4}{\beta}\right)\lambda\sqrt{f'_c}, \left(\frac{\alpha_s d}{b_o} + 2\right)\lambda\sqrt{f'_c} \right] \quad \text{ACI 318-14 (Table 22.6.5.2)}$$

$$v_c = \min \left[4 \times 1 \times \sqrt{5000}, \left(2 + \frac{4}{1}\right) \times 1 \times \sqrt{5000}, \left(\frac{40 \times 13.13}{132.52} + 2\right) \times 1 \times \sqrt{5000} \right]$$

$$v_c = \min[282.8, 424.3, 421.7] \text{ psi} = 282.8 \text{ psi}$$

$$\phi v_c = 0.75 \times 282.8 = 212.1 \text{ psi}$$

Since $\phi v_c \geq v_u$ at the critical section, the slab has adequate two-way shear strength at this joint.

c. Corner column:

In this example, interior equivalent frame strip was selected where it only have exterior and interior supports (no corner supports are included in this strip). However, the two-way shear strength of corner supports usually governs. Thus, the two-way shear strength for the corner column in this example will be checked for educational purposes. Same procedure is used to find the reaction and factored unbalanced moment used for shear transfer at the centroid of the critical section for the corner support for the exterior equivalent frame strip.

$$V_u = V - q_u (b_1 \times b_2) = 61.93 - 0.334 \left(\frac{26.56 \times 26.56}{144} \right) = 60.29 \text{ kips}$$

$$M_{unb} = M - V_u (b_1 - c_{AB} - c_1 / 2) = 187.51 - 60.29 \left(\frac{26.56 - 6.64 - 20 / 2}{12} \right) = 137.65 \text{ ft-kips}$$

For the interior column in Figure 13, the location of the centroidal axis z-z is:

$$c_{AB} = \frac{\text{moment of area of the sides about AB}}{\text{area of the sides}} = \frac{(26.56 \times 13.13 \times 26.56 / 2)}{26.56 \times 13.13 + 26.56 \times 13.13} = 6.64 \text{ in.}$$

The polar moment J_c of the shear perimeter is:

$$J_c = \left(\frac{b_1 d^3}{12} + \frac{d b_1^3}{12} + (b_1 d) \left(\frac{b_1}{2} - c_{AB} \right)^2 \right) + b_2 d c_{AB}^2$$

$$J_c = \left(\frac{26.56 \times 13.13^3}{12} + \frac{13.13 \times 26.56^3}{12} + (26.56 \times 13.13) \left(\frac{26.56}{2} - 6.64 \right)^2 \right) + 26.56 \times 13.13 \times 6.64^2$$

$$J_c = 56,292 \text{ in.}^4$$

$$\gamma_v = 1 - \gamma_f = 1 - 0.600 = 0.400$$

ACI 318-14 (Eq. 8.4.4.2.2)

The length of the critical perimeter for the corner column:

$$b_o = 26.56 + 26.56 = 53.13 \text{ in.}$$

The two-way shear stress (v_u) can then be calculated as:

$$v_u = \frac{V_u}{b_o \times d} + \frac{\gamma_v M_{unb, AB}}{J_c}$$

ACI 318-14 (R.8.4.4.2.3)

$$v_u = \frac{60.29 \times 1000}{53.13 \times 13.13} + \frac{0.400 \times (137.65 \times 12 \times 1000) \times 6.64}{56,292} = 86.4 + 77.9 = 164.40 \text{ psi}$$

$$v_c = \min \left[4\lambda\sqrt{f'_c}, \left(2 + \frac{4}{\beta} \right) \lambda\sqrt{f'_c}, \left(\frac{a_s d}{b_o} + 2 \right) \lambda\sqrt{f'_c} \right]$$

ACI 318-14 (Table 22.6.5.2)

$$v_c = \min \left[4 \times 1 \times \sqrt{5000}, \left(2 + \frac{4}{1} \right) \times 1 \times \sqrt{5000}, \left(\frac{20 \times 13.13}{53.13} + 2 \right) \times 1 \times \sqrt{5000} \right]$$

$$v_c = \min [282.8, 424.3, 490.9] \text{ psi} = 282.8 \text{ psi}$$

$$\phi v_c = 0.75 \times 282.8 = 212.1 \text{ psi}$$

Since $\phi v_c \geq v_u$ at the critical section, the slab has adequate two-way shear strength at this joint.

4.2.2. Around drop panels

Two-way shear is critical on a rectangular section located at $d/2$ away from the face of the drop panel.

Note: The two-way shear stress calculations around drop panels do not have the term for unbalanced moment since drop panels are a thickened portion of the slab and are not considered as a support.

a. Exterior drop panel:

$$V_u = V - q_u A = 105.64 - 0.270 \left(\frac{74.44 \times 128.88}{144} \right) = 87.65 \text{ kips}$$

The length of the critical perimeter for the exterior drop panel:

$$b_o = 2 \times 74.44 + 128.88 = 277.76 \text{ in.}$$

The two-way shear stress (v_u) can then be calculated as:

$$v_u = \frac{V_u}{b_o \times d} \quad \text{ACI 318-14 (R.8.4.4.2.3)}$$

$$v_u = \frac{87.65 \times 1000}{277.76 \times 8.88} = 35.5 \text{ psi}$$

$$v_c = \min \left[4\lambda\sqrt{f'_c}, \left(2 + \frac{4}{\beta} \right) \lambda\sqrt{f'_c}, \left(\frac{a_s d}{b_o} + 2 \right) \lambda\sqrt{f'_c} \right] \quad \text{ACI 318-14 (Table 22.6.5.2)}$$

$$v_c = \min \left[4 \times 1 \times \sqrt{5000}, \left(2 + \frac{4}{1} \right) \times 1 \times \sqrt{5000}, \left(\frac{30 \times 8.88}{277.76} + 2 \right) \times 1 \times \sqrt{5000} \right]$$

$$v_c = \min [282.8, 424.3, 209.2] \text{ psi} = 209.2 \text{ psi}$$

$$\phi v_c = 0.75 \times 209.2 = 156.9 \text{ psi}$$

Since $\phi v_c \geq v_u$ at the critical section, the slab has adequate two-way shear strength around this drop panel.

b. Interior drop panel:

$$V_u = V - q_u A$$

$$V_u = 137.36 + 121.5 - 0.270 \left(\frac{128.88 \times 128.88}{144} \right) = 227.72 \text{ kips}$$

The length of the critical perimeter for the interior drop panel:

$$b_o = 2 \times (128.88 + 128.88) = 515.52 \text{ in.}$$

The two-way shear stress (v_u) can then be calculated as:

$$v_u = \frac{V_u}{b_o \times d} \quad \text{ACI 318-14 (R.8.4.4.2.3)}$$

$$v_u = \frac{227.72 \times 1000}{515.52 \times 8.88} = 49.7 \text{ psi}$$

$$v_c = \min \left[4\lambda\sqrt{f'_c}, \left(2 + \frac{4}{\beta} \right) \lambda\sqrt{f'_c}, \left(\frac{a_s d}{b_o} + 2 \right) \lambda\sqrt{f'_c} \right] \quad \text{ACI 318-14 (Table 22.6.5.2)}$$

$$v_c = \min \left[4 \times 1 \times \sqrt{5000}, \left(2 + \frac{4}{1} \right) \times 1 \times \sqrt{5000}, \left(\frac{40 \times 8.88}{515.52} + 2 \right) \times 1 \times \sqrt{5000} \right]$$

$$v_c = \min [282.8, 424.3, 190.1] \text{ psi} = 190.1 \text{ psi}$$

$$\phi v_c = 0.75 \times 190.1 = 142.6 \text{ psi}$$

Since $\phi v_c \geq v_u$ at the critical section, the slab has adequate two-way shear strength around this drop panel.

c. Corner drop panel:

$$V_u = V - q_u A$$

$$V_u = 61.93 - 0.270 \left(\frac{74.44 \times 74.44}{144} \right) = 51.54 \text{ kips}$$

The length of the critical perimeter for the corner drop panel:

$$b_o = 74.44 + 74.44 = 148.88 \text{ in.}$$

The two-way shear stress (v_u) can then be calculated as:

$$v_u = \frac{V_u}{b_o \times d}$$

ACI 318-14 (R.8.4.4.2.3)

$$v_u = \frac{51.54 \times 1000}{148.88 \times 8.88} = 38.98 \text{ psi}$$

$$v_c = \min \left[4\lambda\sqrt{f'_c}, \left(2 + \frac{4}{\beta} \right) \lambda\sqrt{f'_c}, \left(\frac{\alpha_s d}{b_o} + 2 \right) \lambda\sqrt{f'_c} \right]$$

ACI 318-14 (Table 22.6.5.2)

$$v_c = \min \left[4 \times 1 \times \sqrt{5000}, \left(2 + \frac{4}{1} \right) \times 1 \times \sqrt{5000}, \left(\frac{20 \times 8.88}{148.88} + 2 \right) \times 1 \times \sqrt{5000} \right]$$

$$v_c = \min[282.8, 424.3, 225.8] \text{ psi} = 225.8 \text{ psi}$$

$$\phi v_c = 0.75 \times 225.8 = 169.3 \text{ psi}$$

Since $\phi v_c \geq v_u$ at the critical section, the slab has adequate two-way shear strength around this drop panel.

5. Serviceability Requirements (Deflection Check)

Since the slab thickness was selected below the minimum slab thickness tables in ACI 318-14, the deflection calculations of immediate and time-dependent deflections are required and shown below including a comparison with spSlab model results.

5.1. Immediate (Instantaneous) Deflections

The calculation of deflections for two-way slabs is challenging even if linear elastic behavior can be assumed. Elastic analysis for three service load levels (D , $D + L_{sustained}$, $D + L_{Full}$) is used to obtain immediate deflections of the two-way slab in this example. However, other procedures may be used if they result in predictions of deflection in reasonable agreement with the results of comprehensive tests. ACI 318-14 (24.2.3)

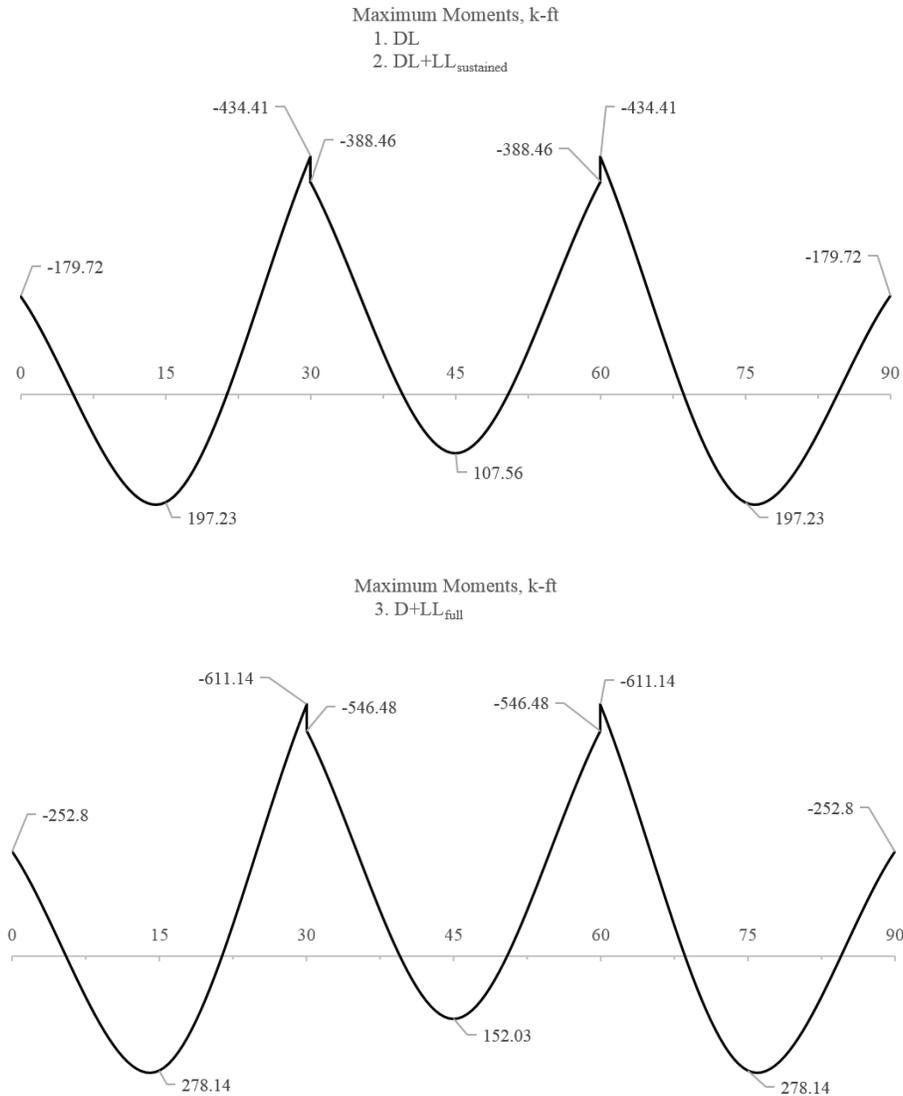
The effective moment of inertia (I_e) is used to account for the cracking effect on the flexural stiffness of the slab. I_e for uncracked section ($M_{cr} > M_a$) is equal to I_g . When the section is cracked ($M_{cr} < M_a$), then the following equation should be used:

$$I_e = \left(\frac{M_{cr}}{M_a} \right)^3 I_g + \left[1 - \left(\frac{M_{cr}}{M_a} \right)^3 \right] I_{cr} \leq I_g \quad \text{ACI 318-14 (Eq. 24.2.3.5a)}$$

Where:

M_a = Maximum moment in member due to service loads at stage deflection is calculated.

The values of the maximum moments for the three service load levels are calculated from structural analysis as shown previously in this document. These moments are shown in Figure 17.



**Figure 17 – Maximum Moments for the Three Service Load Levels
(No live load is sustained in this example)**

For positive moment (midspan) section:

M_{cr} = Cracking moment.

$$M_{cr} = \frac{f_r I_g}{y_t} = \frac{530.33 \times 30000}{5} \times \frac{1}{12 \times 1000} = 265.17 \text{ ft-kips}$$

ACI 318-14 (Eq. 24.2.3.5b)

f_r = Modulus of rupture of concrete.

$$f_r = 7.5\lambda\sqrt{f'_c} = 7.5 \times 1.0 \times \sqrt{5000} = 530.33 \text{ psi}$$

ACI 318-14 (Eq. 19.2.3.1)

I_g = Moment of inertia of the gross uncracked concrete section.

$$I_g = \frac{l h^3}{12} = \frac{(30 \times 12) (10)^3}{12} = 30000 \text{ in.}^2$$

y_t = Distance from centroidal axis of gross section, neglecting reinforcement, to tension face, in.

$$y_t = \frac{h}{2} = \frac{10}{2} = 5 \text{ in.}$$

I_{cr} = Moment of inertia of the cracked section transformed to concrete. **PCA Notes on ACI 318-11 (9.5.2.2)**

As calculated previously, the positive reinforcement for the end span frame strip is 23 #6 bars located at 1.125 in. along the section from the bottom of the slab. Two of these bars are not continuous and will be conservatively excluded from the calculation of I_{cr} since they might not be adequately developed or tied (21 bars are used). Figure 18 shows all the parameters needed to calculate the moment of inertia of the cracked section transformed to concrete at midspan.

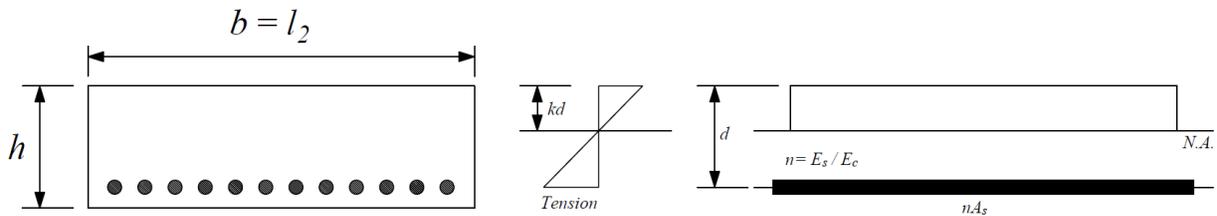


Figure 18 – Cracked Transformed Section (positive moment section)

E_{cs} = Modulus of elasticity of slab concrete.

$$E_{cs} = w_c^{1.5} 33 \sqrt{f'_c} = 150^{1.5} \times 33 \times \sqrt{5000} = 4287 \times 10^3 \text{ psi}$$

ACI 318-14 (19.2.2.1.a)

$$n = \frac{E_s}{E_{cs}} = \frac{29000000}{4287000} = 6.76$$

PCA Notes on ACI 318-11 (Table 10-2)

$$B = \frac{b}{n A_s} = \frac{30 \times 12}{6.76 \times (21 \times 0.44)} = 5.76 \text{ in.}^{-1}$$

PCA Notes on ACI 318-11 (Table 10-2)

$$kd = \frac{\sqrt{2dB+1}-1}{B} = \frac{\sqrt{2 \times 8.88 \times 5.76 + 1} - 1}{5.76} = 1.59 \text{ in.}$$

PCA Notes on ACI 318-11 (Table 10-2)

$$I_{cr} = \frac{b(kd)^3}{3} + nA_s(d - kd)^2$$

PCA Notes on ACI 318-11 (Table 10-2)

$$I_{cr} = \frac{30 \times 12 \times (1.59)^3}{3} + 6.76 \times (21 \times 0.44) (8.88 - 1.59)^2 = 3802 \text{ in.}^4$$

For negative moment section (near the interior support of the end span):

The negative reinforcement for the end span frame strip near the interior support is 32 #6 bars located at 1.125 in. along the section from the top of the slab.

$$M_{cr} = \frac{f_r I_g}{y_t} = \frac{530.33 \times 53445}{5.88} \times \frac{1}{12 \times 1000} = 401.42 \text{ ft-kips}$$

ACI 318-14 (Eq. 24.2.3.5b)

$$f_r = 7.5 \lambda \sqrt{f'_c} = 7.5 \times 1.0 \times \sqrt{5000} = 530.33 \text{ psi}$$

ACI 318-14 (Eq. 19.2.3.1)

$$I_g = 53445 \text{ in.}^2$$

$$y_t = 5.88 \text{ in.}$$

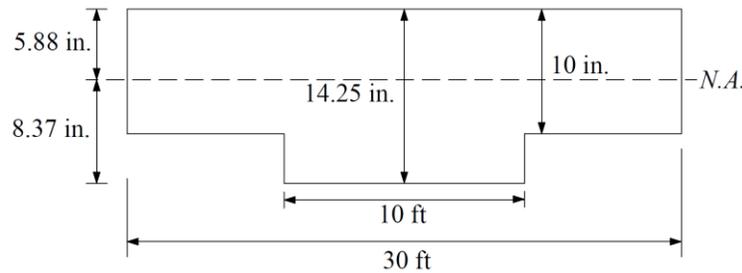


Figure 19 – I_g calculations for slab section near support

$$E_{cs} = w_c^{1.5} 33 \sqrt{f'_c} = 150^{1.5} \times 33 \times \sqrt{5000} = 4287 \times 10^3 \text{ psi}$$

ACI 318-14 (19.2.2.1.a)

$$n = \frac{E_s}{E_{cs}} = \frac{29000000}{4287000} = 6.76$$

PCA Notes on ACI 318-11 (Table 10-2)

$$B = \frac{b}{n A_s} = \frac{10 \times 12}{6.76 \times (32 \times 0.44)} = 1.26 \text{ in.}^{-1}$$

PCA Notes on ACI 318-11 (Table 10-2)

$$kd = \frac{\sqrt{2dB+1}-1}{B} = \frac{\sqrt{2 \times 13.13 \times 1.26 + 1} - 1}{1.26} = 3.84 \text{ in.}$$

PCA Notes on ACI 318-11 (Table 10-2)

$$I_{cr} = \frac{b (kd)^3}{3} + n A_s (d - kd)^2$$

PCA Notes on ACI 318-11 (Table 10-2)

$$I_{cr} = \frac{10 \times 12 \times (3.84)^3}{3} + 6.76 \times (32 \times 0.44) (13.13 - 3.84)^2 = 10471 \text{ in.}^4$$

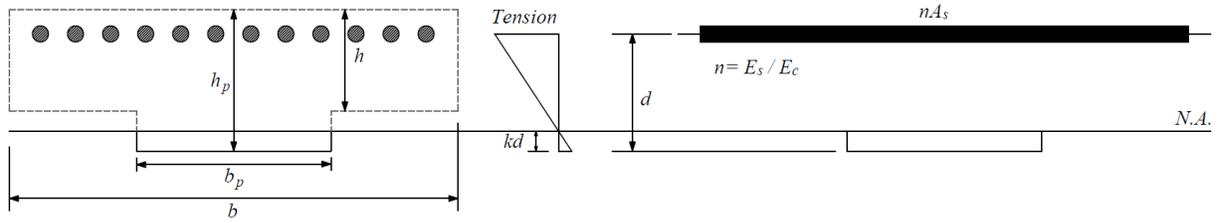


Figure 20 – Cracked Transformed Section (negative moment section)

The effective moment of inertia procedure described in the Code is considered sufficiently accurate to estimate deflections. The effective moment of inertia, I_e , was developed to provide a transition between the upper and lower bounds of I_g and I_{cr} as a function of the ratio M_{cr}/M_a . For conventionally reinforced (nonprestressed) members, the effective moment of inertia, I_e , shall be calculated by Eq. (24.2.3.5a) unless obtained by a more comprehensive analysis.

I_e shall be permitted to be taken as the value obtained from Eq. (24.2.3.5a) at midspan for simple and continuous spans, and at the support for cantilevers. **ACI 318-14 (24.2.3.7)**

For continuous one-way slabs and beams, I_e shall be permitted to be taken as the average of values obtained from Eq. (24.2.3.5a) for the critical positive and negative moment sections. **ACI 318-14 (24.2.3.6)**

For the middle span (span with two ends continuous) with service load level ($D+LL_{full}$):

$$I_e^- = \left(\frac{M_{cr}}{M_a} \right)^3 I_g + \left[1 - \left(\frac{M_{cr}}{M_a} \right)^3 \right] I_{cr}, \text{ since } M_{cr} = 401.4 \text{ ft-kips} < M_a = 546.5 \text{ ft-kips}$$

ACI 318-14 (24.2.3.5a)

Where I_e^- is the effective moment of inertia for the critical negative moment section (near the support).

$$I_e^- = \left(\frac{401.4}{546.5} \right)^3 \times 53445 + \left[1 - \left(\frac{401.4}{546.5} \right)^3 \right] \times 10471 = 27503 \text{ in.}^4$$

$$I_e^+ = I_g = 30000 \text{ in.}^4, \text{ since } M_{cr} = 265.17 \text{ ft-kips} > M_a = 152.03 \text{ ft-kips}$$

Where I_e^+ is the effective moment of inertia for the critical positive moment section (midspan).

Since midspan stiffness (including the effect of cracking) has a dominant effect on deflections, midspan section is heavily represented in calculation of I_e and this is considered satisfactory in approximate deflection calculations. Both the midspan stiffness (I_e^+) and averaged span stiffness ($I_{e,avg}$) can be used in the calculation of immediate (instantaneous) deflection.

The averaged effective moment of inertia ($I_{e,avg}$) is given by:

$$I_{e,avg} = 0.70 I_e^+ + 0.15 (I_{e,l}^- + I_{e,r}^-) \text{ for interior span} \quad \text{PCA Notes on ACI 318-11 (9.5.2.4(2))}$$

$$I_{e,avg} = 0.85 I_e^+ + 0.15 I_e^- \text{ for end span} \quad \text{PCA Notes on ACI 318-11 (9.5.2.4(1))}$$

However, these expressions lead to improved results only for continuous prismatic members. The drop panels in this example result in non-prismatic members and the following expressions should be used according to ACI 318-89:

$$I_{e,avg} = 0.50 I_e^+ + 0.25 (I_{e,l}^- + I_{e,r}^-) \text{ for interior span} \quad \text{ACI 435R-95 (2.14)}$$

For the middle span (span with two ends continuous) with service load level ($D+LL_{full}$):

$$I_{e,avg} = 0.50 \times 30000 + 0.25 (27503 + 27503) = 41723 \text{ in.}^4$$

$$I_{e,avg} = 0.50 I_e^+ + 0.50 I_e^- \text{ for end span} \quad \text{ACI 435R-95 (2.14)}$$

For the end span (span with one end continuous) with service load level ($D+LL_{full}$):

$$I_{e,avg} = 0.50 \times 26503 + 0.50 \times 22649 = 37190 \text{ in.}^4$$

Where:

$I_{e,l}^-$ = The effective moment of inertia for the critical negative moment section near the left support.

$I_{e,r}^-$ = The effective moment of inertia for the critical negative moment section near the right support.

I_e^+ = The effective moment of inertia for the critical positive moment section (midspan).

Table 6 provides a summary of the required parameters and calculated values needed for deflections for exterior and interior spans.

| Table 6 – Averaged Effective Moment of Inertia Calculations | | | | | | | | | | | | | |
|---|---------|-----------------------------------|-------------------------------------|--------------------------|-----------------------|-----------------------|------------------------|-----------------------------------|-----------------------|-----------------------|---------------------------------------|-----------------------|-----------------------|
| For Frame Strip | | | | | | | | | | | | | |
| Span | zone | I _g , in. ⁴ | I _{crs} , in. ⁴ | M _a , kips-ft | | | M _{cr} , k-ft | I _e , in. ⁴ | | | I _{e,avg} , in. ⁴ | | |
| | | | | D | D + LL _{Sus} | D + L _{full} | | D | D + LL _{Sus} | D + L _{full} | D | D + LL _{Sus} | D + L _{full} |
| Ext | Left | 53445 | 7170 | -179.72 | -179.72 | -252.8 | 401.42 | 53445 | 53445 | 53445 | 37190 | 37190 | 24576 |
| | Midspan | 30000 | 3797 | 197.23 | 197.23 | 278.14 | 265.17 | 30000 | 30000 | 26503 | | | |
| | Right | 53445 | 10471 | -434.41 | -434.41 | -611.14 | 401.42 | 44379 | 44379 | 22649 | | | |
| Int | Left | 53445 | 10471 | -388.46 | -388.46 | -546.48 | 401.42 | 53445 | 53445 | 27503 | 41723 | 41723 | 28752 |
| | Mid | 30000 | 3317 | 107.56 | 107.56 | 152.03 | 265.17 | 30000 | 30000 | 30000 | | | |
| | Right | 53445 | 10471 | -388.46 | -388.46 | -546.48 | 401.42 | 53445 | 53445 | 27503 | | | |

Deflections in two-way slab systems shall be calculated taking into account size and shape of the panel, conditions of support, and nature of restraints at the panel edges. For immediate deflections in two-way slab systems, the midpanel deflection is computed as the sum of deflection at midspan of the column strip or column line in one direction (Δ_{cx} or Δ_{cy}) and deflection at midspan of the middle strip in the orthogonal direction (Δ_{mx} or Δ_{my}). Figure 21 shows the deflection computation for a rectangular panel. The average Δ for panels that have different properties in the two direction is calculated as follows:

$$\Delta = \frac{(\Delta_{cx} + \Delta_{my}) + (\Delta_{cy} + \Delta_{mx})}{2}$$

PCA Notes on ACI 318-11 (9.5.3.4 Eq. 8)

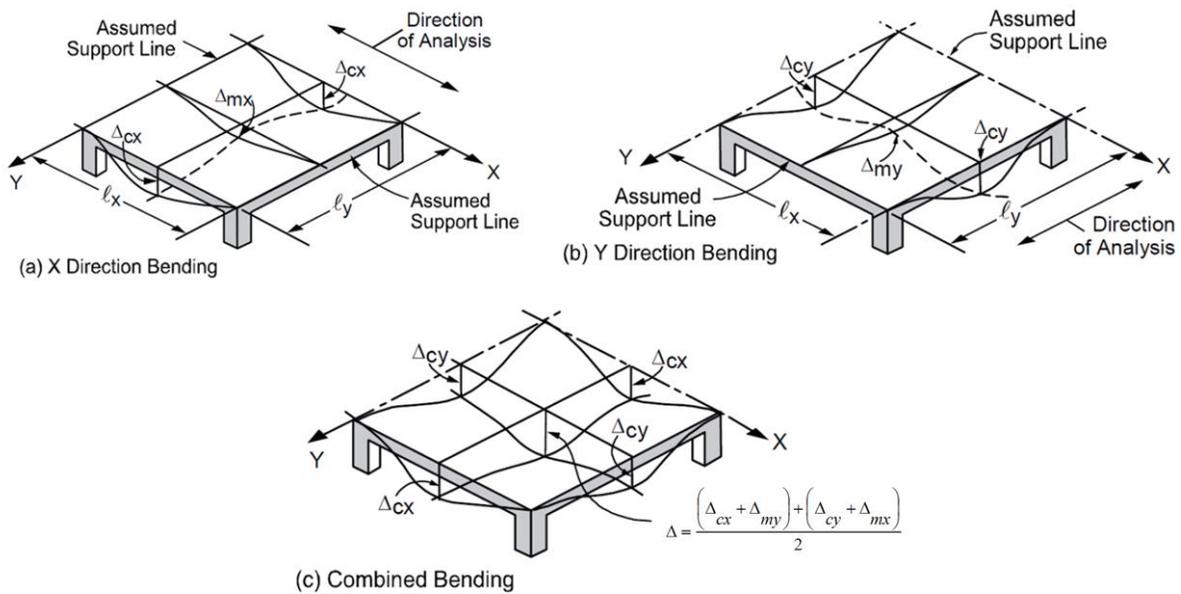


Figure 21 – Deflection Computation for a rectangular Panel

To calculate each term of the previous equation, the following procedure should be used. Figure 22 shows the procedure of calculating the term Δ_{cx} . Same procedure can be used to find the other terms.

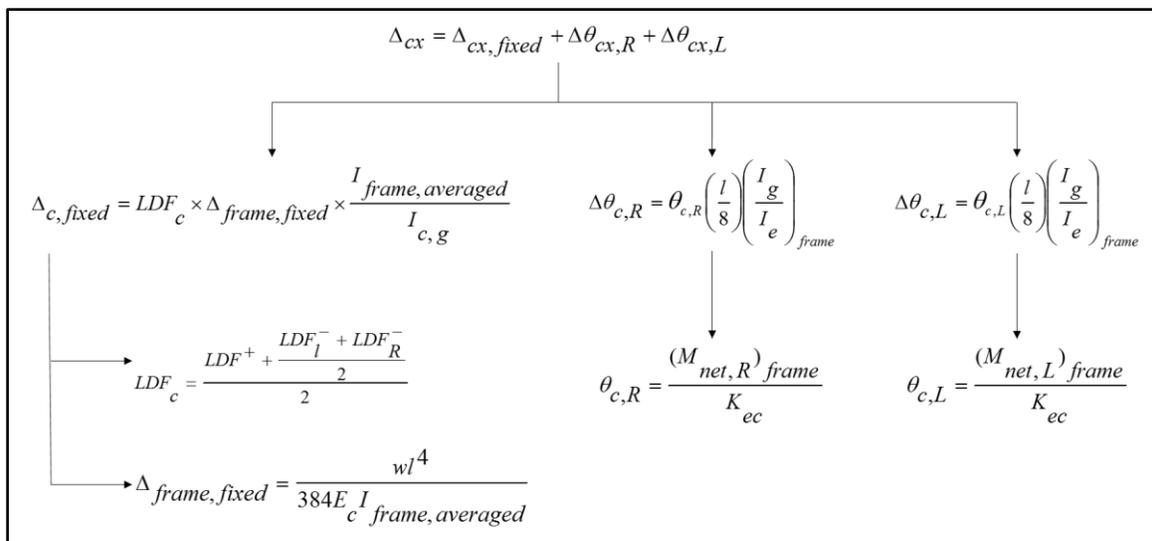


Figure 22 – Δ_{cx} calculation procedure

For end span - service dead load case:

$$\Delta_{frame, fixed} = \frac{wl^4}{384E I_{c, frame, averaged}} \quad \text{PCA Notes on ACI 318-11 (9.5.3.4 Eq. 10)}$$

Where:

$\Delta_{frame, fixed}$ = Deflection of column strip assuming fixed end condition.

$$w = (20 + 150 \times 10 / 12)(30) = 4350 \text{ lb/ft}$$

$$E_c = w_c^{1.5} 33 \sqrt{f'_c} = 4287 \times 10^3 \text{ psi} \quad \text{ACI 318-14 (19.2.2.1.a)}$$

$I_{frame, averaged}$ = The averaged effective moment of inertia ($I_{e, avg}$) for the frame strip for service dead load case from Table 6 = 37190 in.⁴

$$\Delta_{frame, fixed} = \frac{(4350)(30)^4(12)^3}{384(4287 \times 10^3)(37190)} = 0.0995 \text{ in.}$$

$$\Delta_{c, fixed} = LDF_c \times \Delta_{frame, fixed} \times \frac{I_{frame, averaged}}{I_{c, g}} \quad \text{PCA Notes on ACI 318-11 (9.5.3.4 Eq. 11)}$$

For this example and like in the spSlab program, the effective moment of inertia at midspan will be used.

LDF_c is the load distribution factor for the column strip. The load distribution factor for the column strip can be found from the following equation:

$$LDF_c = \frac{LDF^+ + \frac{LDF_l^- + LDF_R^-}{2}}{2}$$

And the load distribution factor for the middle strip can be found from the following equation:

$$LDF_m = 1 - LDF_c$$

For the end span, LDF for exterior negative region (LDF_L^-), interior negative region (LDF_R^-), and positive region (LDF_L^+) are 1.00, 0.75, and 0.60, respectively (From Table 2 of this document). Thus, the load distribution factor for the column strip for the end span is given by:

$$LDF_c = \frac{0.6 + \frac{1.0 + 0.75}{2}}{2} = 0.738$$

$I_{c, g}$ = The gross moment of inertia (I_g) for the column strip for service dead load = 15000 in.⁴

$$\Delta_{c, fixed} = 0.738 \times 0.0995 \times \frac{30000}{15000} = 0.1468 \text{ in.}$$

$$\theta_{c,L} = \frac{(M_{net,L})_{frame}}{K_{ec}}$$

PCA Notes on ACI 318-11 (9.5.3.4 Eq. 12)

Where:

$\theta_{c,L}$ = Rotation of the span left support.

$(M_{net,L})_{frame} = 179.72 \text{ ft-kips} = \text{Net frame strip negative moment of the left support.}$

K_{ec} = effective column stiffness = $1353 \times 10^6 \text{ in.-lb}$ (calculated previously).

$$\theta_{c,L} = \frac{179.72 \times 12 \times 1000}{1353 \times 10^6} = 0.00159 \text{ rad}$$

$$\Delta\theta_{c,L} = \theta_{c,L} \left(\frac{l}{8} \right) \left(\frac{I_g}{I_e} \right)_{frame}$$

PCA Notes on ACI 318-11 (9.5.3.4 Eq. 14)

Where:

$\Delta\theta_{c,L}$ = Midspan deflection due to rotation of left support.

$\left(\frac{I_g}{I_e} \right)_{frame}$ = Gross-to-effective moment of inertia ratio for frame strip.

$$\Delta\theta_{c,L} = 0.00159 \times \frac{30 \times 12}{8} \times \frac{30000}{37190} = 0.05786 \text{ in.}$$

$$\theta_{c,R} = \frac{(M_{net,R})_{frame}}{K_{ec}} = \frac{(611.14 - 546.48) \times 12 \times 1000}{1353 \times 10^6} = 0.00041 \text{ rad}$$

Where

$\theta_{c,R}$ = Rotation of the end span right support.

$(M_{net,R})_{frame} = \text{Net frame strip negative moment of the right support.}$

$$\Delta\theta_{c,R} = \theta_{c,R} \left(\frac{l}{8} \right) \left(\frac{I_g}{I_e} \right)_{frame} = 0.00041 \times \frac{30 \times 12}{8} \times \frac{30000}{37190} = 0.01479 \text{ in.}$$

Where:

$\Delta\theta_{c,R}$ = Midspan deflection due to rotation of right support.

$$\Delta_{cx} = \Delta_{cx, fixed} + \Delta\theta_{cx,R} + \Delta\theta_{cx,L}$$

PCA Notes on ACI 318-11 (9.5.3.4 Eq. 9)

$$\Delta_{cx} = 0.1468 + 0.01479 + 0.05786 = 0.219 \text{ in.}$$

Following the same procedure, Δ_{mx} can be calculated for the middle strip. This procedure is repeated for the equivalent frame in the orthogonal direction to obtain Δ_{cy} , and Δ_{my} for the end and middle spans for the other load levels ($D+LL_{sus}$ and $D+LL_{full}$).

Since in this example the panel is squared, $\Delta_{cx} = \Delta_{cy} = 0.219$ in. and $\Delta_{mx} = \Delta_{my} = 0.125$ in.

The average Δ for the corner panel is calculated as follows:

$$\Delta = \frac{(\Delta_{cx} + \Delta_{my}) + (\Delta_{cy} + \Delta_{mx})}{2} = (\Delta_{cx} + \Delta_{my}) = (\Delta_{cy} + \Delta_{mx}) = 0.219 + 0.125 = 0.344 \text{ in.}$$

Table 7 – Immediate (Instantaneous) Deflections in the x-direction

Column Strip

Middle Strip

| Span | LDF | D | | | | | | |
|------|-------|--|------------------------------------|-------------------------------|-------------------------------|-------------------------------------|-------------------------------------|-------------------------------|
| | | $\Delta_{\text{frame-fixed}}$, in. | $\Delta_{\text{c-fixed}}$, in. | θ_{c1} , rad | θ_{c2} , rad | $\Delta\theta_{\text{c1}}$, in. | $\Delta\theta_{\text{c2}}$, in. | Δ_{cx} , in. |
| Ext | 0.738 | 0.0995 | 0.1468 | 0.00159 | 0.00041 | 0.05786 | 0.01479 | 0.219 |
| Int | 0.675 | 0.0886 | 0.1197 | 0.00041 | 0.00041 | -0.01319 | -0.01319 | 0.093 |

| LDF | D | | | | | | |
|-------|--|------------------------------------|-------------------------------|-------------------------------|-------------------------------------|-------------------------------------|-------------------------------|
| | $\Delta_{\text{frame-fixed}}$, in. | $\Delta_{\text{m-fixed}}$, in. | θ_{m1} , rad | θ_{m2} , rad | $\Delta\theta_{\text{m1}}$, in. | $\Delta\theta_{\text{m2}}$, in. | Δ_{mx} , in. |
| 0.262 | 0.0995 | 0.0521 | 0.00159 | 0.00041 | 0.05786 | 0.01479 | 0.125 |
| 0.325 | 0.0886 | 0.0576 | 0.00041 | 0.00041 | -0.01319 | -0.01319 | 0.031 |

| Span | LDF | D+LL _{sus} | | | | | | |
|------|-------|--|------------------------------------|-------------------------------|-------------------------------|-------------------------------------|-------------------------------------|-------------------------------|
| | | $\Delta_{\text{frame-fixed}}$, in. | $\Delta_{\text{c-fixed}}$, in. | θ_{c1} , rad | θ_{c2} , rad | $\Delta\theta_{\text{c1}}$, in. | $\Delta\theta_{\text{c2}}$, in. | Δ_{cx} , in. |
| Ext | 0.738 | 0.0995 | 0.1468 | 0.00159 | 0.00041 | 0.05786 | 0.01479 | 0.219 |
| Int | 0.675 | 0.0886 | 0.1197 | 0.00041 | 0.00041 | -0.01319 | -0.01319 | 0.093 |

| LDF | D+LL _{sus} | | | | | | |
|-------|--|------------------------------------|-------------------------------|-------------------------------|-------------------------------------|-------------------------------------|-------------------------------|
| | $\Delta_{\text{frame-fixed}}$, in. | $\Delta_{\text{m-fixed}}$, in. | θ_{m1} , rad | θ_{m2} , rad | $\Delta\theta_{\text{m1}}$, in. | $\Delta\theta_{\text{m2}}$, in. | Δ_{mx} , in. |
| 0.262 | 0.0995 | 0.0521 | 0.00159 | 0.00041 | 0.05786 | 0.01479 | 0.125 |
| 0.325 | 0.0886 | 0.0576 | 0.00041 | 0.00041 | -0.01319 | -0.01319 | 0.031 |

| Span | LDF | D+LL _{full} | | | | | | |
|------|-------|--|------------------------------------|-------------------------------|-------------------------------|-------------------------------------|-------------------------------------|-------------------------------|
| | | $\Delta_{\text{frame-fixed}}$, in. | $\Delta_{\text{c-fixed}}$, in. | θ_{c1} , rad | θ_{c2} , rad | $\Delta\theta_{\text{c1}}$, in. | $\Delta\theta_{\text{c2}}$, in. | Δ_{cx} , in. |
| Ext | 0.738 | 0.2128 | 0.2775 | 0.00224 | 0.00057 | 0.12316 | 0.0315 | 0.432 |
| Int | 0.675 | 0.1819 | 0.2455 | 0.00057 | 0.00057 | -0.02693 | -0.02693 | 0.192 |

| LDF | D+LL _{full} | | | | | | |
|-------|--|------------------------------------|-------------------------------|-------------------------------|-------------------------------------|-------------------------------------|-------------------------------|
| | $\Delta_{\text{frame-fixed}}$, in. | $\Delta_{\text{m-fixed}}$, in. | θ_{m1} , rad | θ_{m2} , rad | $\Delta\theta_{\text{m1}}$, in. | $\Delta\theta_{\text{m2}}$, in. | Δ_{mx} , in. |
| 0.262 | 0.2128 | 0.0985 | 0.00224 | 0.00057 | 0.12316 | 0.03125 | 0.253 |
| 0.325 | 0.1819 | 0.1182 | 0.00057 | 0.00057 | -0.02693 | -0.02693 | 0.064 |

| Span | LDF | LL |
|------|-------|-------------------------------|
| | | Δ_{cx} , in. |
| Ext | 0.738 | 0.213 |
| Int | 0.675 | 0.098 |

| LDF | LL |
|-------|-------------------------------|
| | Δ_{mx} , in. |
| 0.262 | 0.128 |
| 0.325 | 0.033 |

5.2. Time-Dependent (Long-Term) Deflections (Δ_{lt})

The additional time-dependent (long-term) deflection resulting from creep and shrinkage (Δ_{cs}) may be estimated as follows:

$$\Delta_{cs} = \lambda_{\Delta} \times (\Delta_{sust})_{Inst} \quad \text{PCA Notes on ACI 318-11 (9.5.2.5 Eq. 4)}$$

The total time-dependent (long-term) deflection is calculated as:

$$(\Delta_{total})_{lt} = (\Delta_{sust})_{Inst} \times (1 + \lambda_{\Delta}) + [(\Delta_{total})_{Inst} - (\Delta_{sust})_{Inst}] \quad \text{CSA A23.3-04 (N9.8.2.5)}$$

Where:

$(\Delta_{sust})_{Inst}$ = Immediate (instantaneous) deflection due to sustained load, in.

$$\lambda_{\Delta} = \frac{\xi}{1 + 50\rho'} \quad \text{ACI 318-14 (24.2.4.1.1)}$$

$(\Delta_{total})_{lt}$ = Time-dependent (long-term) total deflection, in.

$(\Delta_{total})_{Inst}$ = Total immediate (instantaneous) deflection, in.

For the exterior span

$\xi = 2$, consider the sustained load duration to be 60 months or more. ACI 318-14 (Table 24.2.4.1.3)

$\rho' = 0$, conservatively.

$$\lambda_{\Delta} = \frac{2}{1 + 50 \times 0} = 2$$

$$\Delta_{cs} = 2 \times 0.219 = 0.439 \text{ in.}$$

$$(\Delta_{total})_{lt} = 0.219 \times (1 + 2) + (0.432 - 0.219) = 0.871 \text{ in.}$$

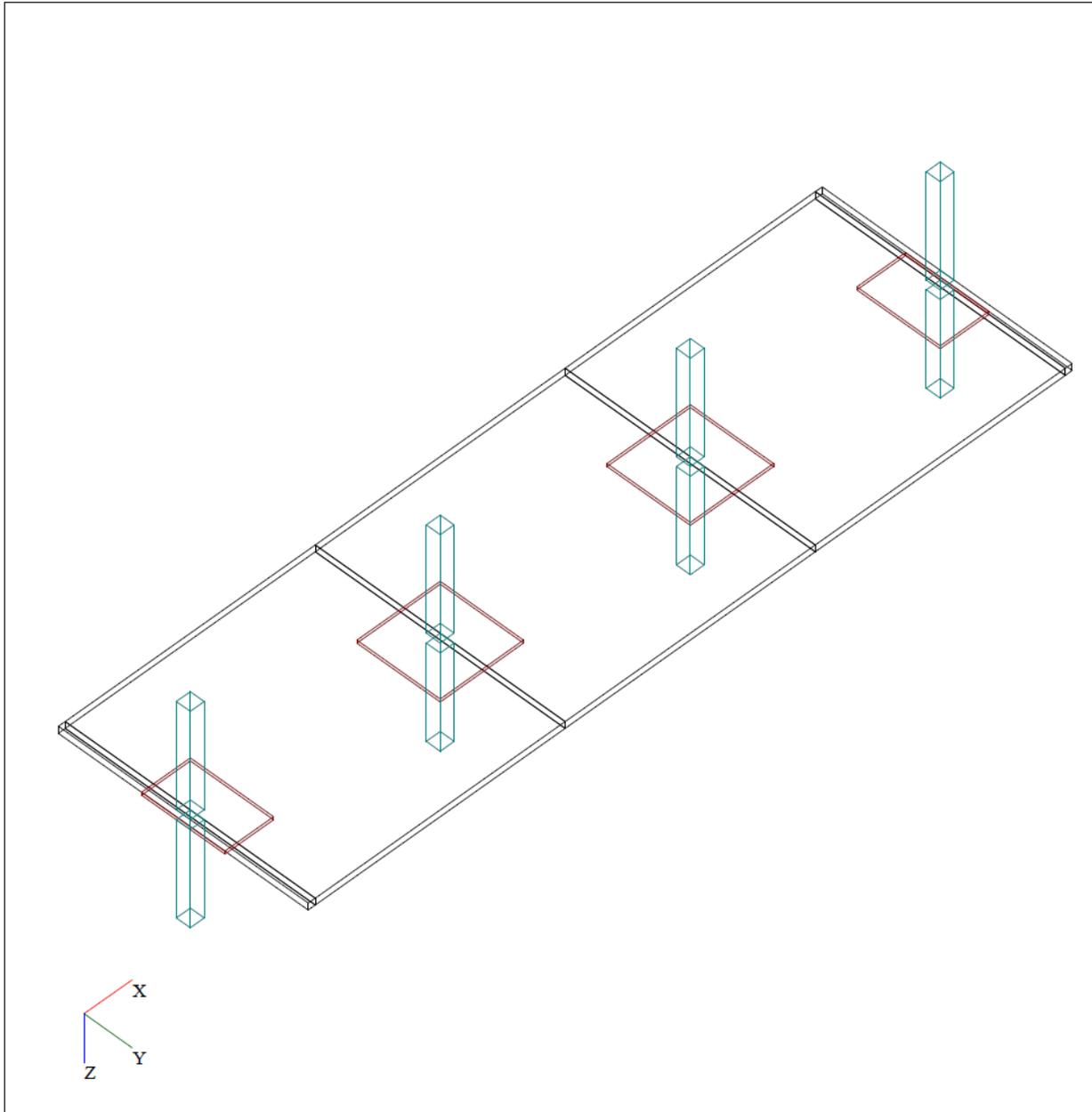
Table 8 shows long-term deflections for the exterior and interior spans for the analysis in the x-direction, for column and middle strips.

| Table 8 - Long-Term Deflections | | | | | |
|--|---|--------------------------------------|--------------------------------------|--|--|
| Column Strip | | | | | |
| Span | $(\Delta_{sust})_{Inst}$, in. | λ_{Δ} | Δ_{cs}, in. | $(\Delta_{total})_{Inst}$, in. | $(\Delta_{total})_{lt}$, in. |
| Exterior | 0.219 | 2.000 | 0.439 | 0.432 | 0.871 |
| Interior | 0.093 | 2.000 | 0.187 | 0.192 | 0.378 |
| Middle Strip | | | | | |
| Exterior | 0.125 | 2.000 | 0.250 | 0.253 | 0.503 |
| Interior | 0.031 | 2.000 | 0.062 | 0.064 | 0.127 |

6. spSlab Software Program Model Solution

[spSlab](#) program utilizes the Equivalent Frame Method described and illustrated in details here for modeling, analysis and design of two-way concrete floor slab systems with drop panels. [spSlab](#) uses the exact geometry and boundary conditions provided as input to perform an elastic stiffness (matrix) analysis of the equivalent frame taking into account the torsional stiffness of the slabs framing into the column. It also takes into account the complications introduced by a large number of parameters such as vertical and torsional stiffness of transverse beams, the stiffening effect of drop panels, column capitals, and effective contribution of columns above and below the floor slab using the of equivalent column concept (*ACI 318-14 (R8.11.4)*).

[spSlab](#) Program models the equivalent frame as a design strip. The design strip is, then, separated by [spSlab](#) into column and middle strips. The program calculates the internal forces (Shear Force & Bending Moment), moment and shear capacity vs. demand diagrams for column and middle strips, instantaneous and long-term deflection results, and required flexural reinforcement for column and middle strips. The graphical and text results are provided below for both input and output of the [spSlab](#) model.



spSlab v5.00. Licensed to: StructurePoint. License ID: 66184-1055152-4-2C6B6-2C6B6

File: C:\TSDA\TSDA-spSlab-Two-Way Slab with Drop Panels.slb

Project: Two-Way Slab with Drop Panels

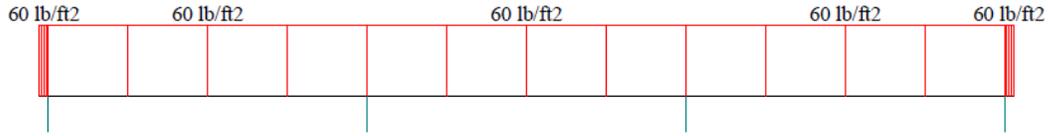
Frame: Interior Frame

Engineer: SP

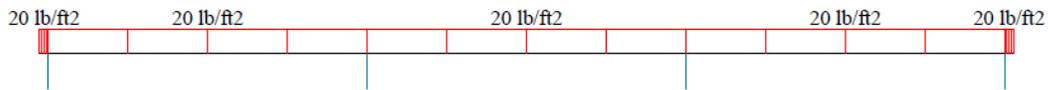
Code: ACI 318-14

Date: 03/16/17

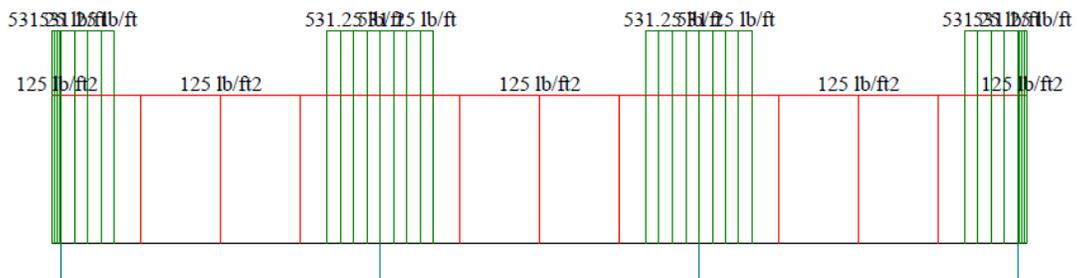
Time: 15:42:36



CASE/PATTERN: Live/All



CASE: Dead



CASE: SELF

spSlab v5.00. Licensed to: StructurePoint. License ID: 66184-1055152-4-2C6B6-2C6B6

File: C:\TSDA\TSDA-spSlab-Two-Way Slab with Drop Panels.slb

Project: Two-Way Slab with Drop Panels

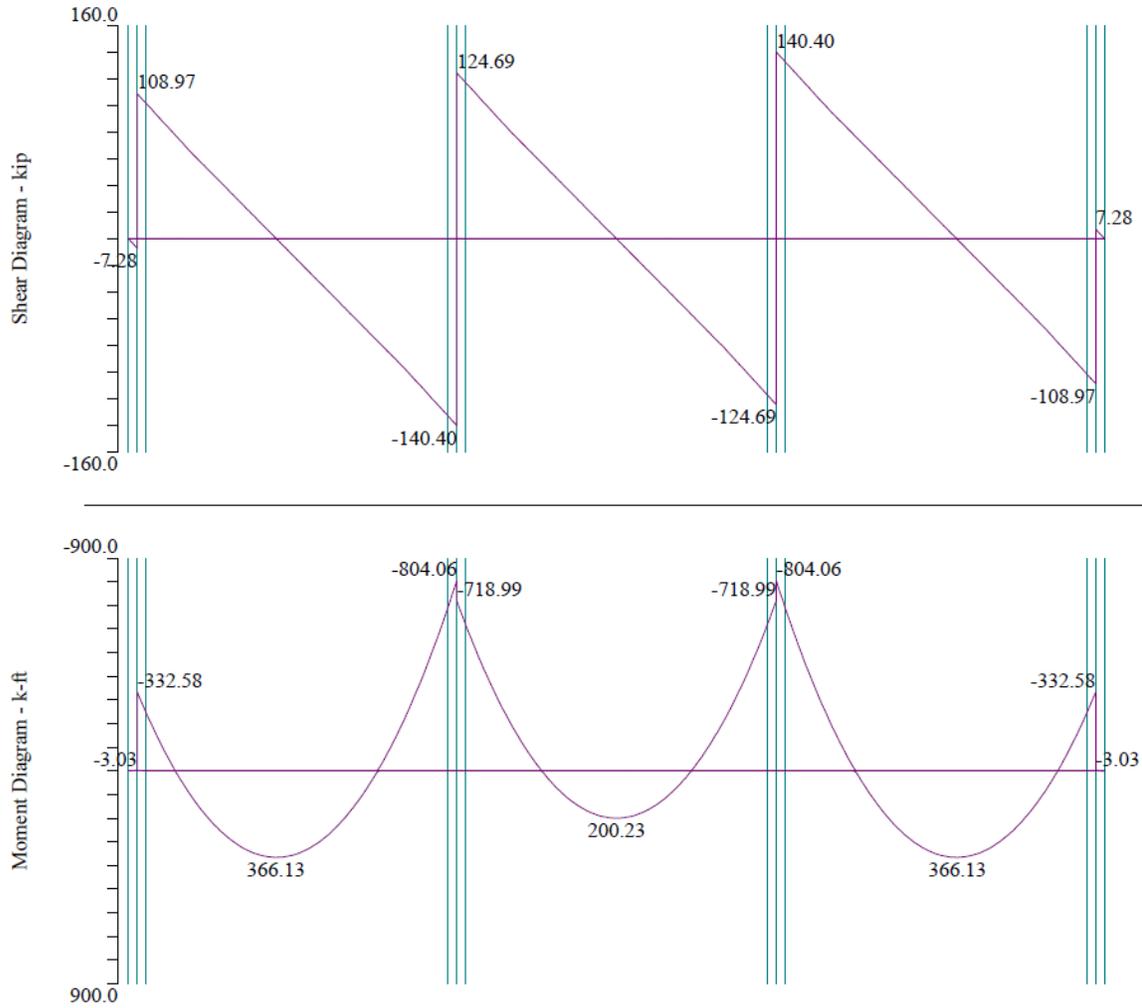
Frame: Interior Frame

Engineer: SP

Code: ACI 318-14

Date: 03/16/17

Time: 15:44:15



spSlab v5.00. Licensed to: StructurePoint. License ID: 66184-1055152-4-2C6B6-2C6B6

File: C:\TSDA\TSDA-spSlab-Two-Way Slab with Drop Panels.slb

Project: Two-Way Slab with Drop Panels

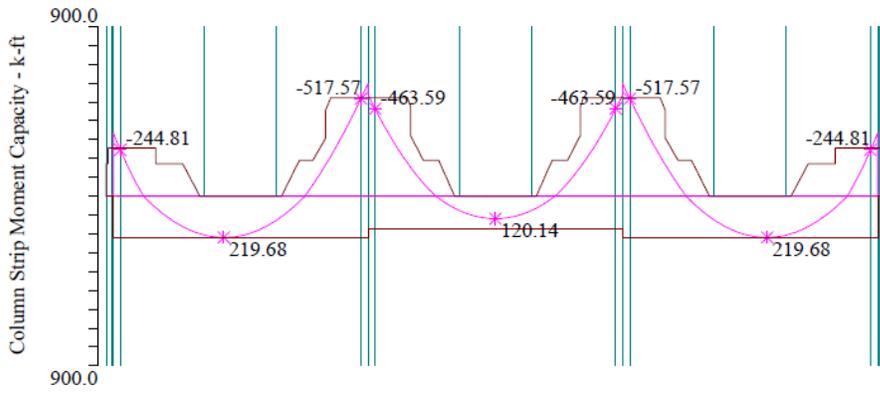
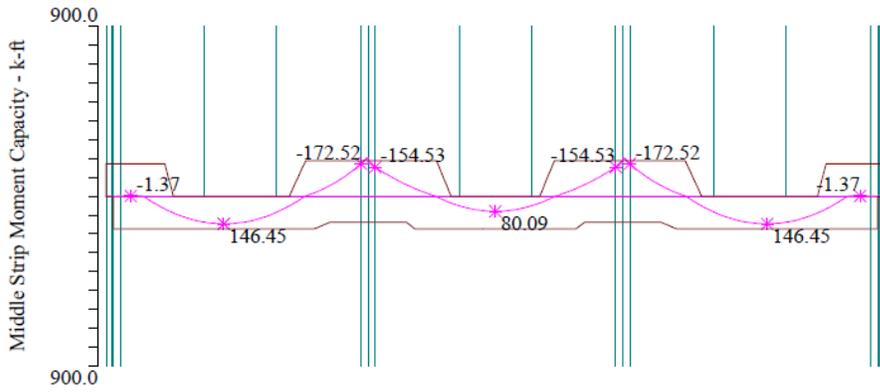
Frame: Interior Frame

Engineer: SP

Code: ACI 318-14

Date: 03/16/17

Time: 15:45:25



LEGEND:
 Envelope Curve
 Capacity Curve
 Support Centerline
 Face of Support
 Zone Limits

spSlab v5.00. Licensed to: StructurePoint. License ID: 66184-1055152-4-2C6B6-2C6B6

File: C:\TSDA\TSDA-spSlab-Two-Way Slab with Drop Panels.slb

Project: Two-Way Slab with Drop Panels

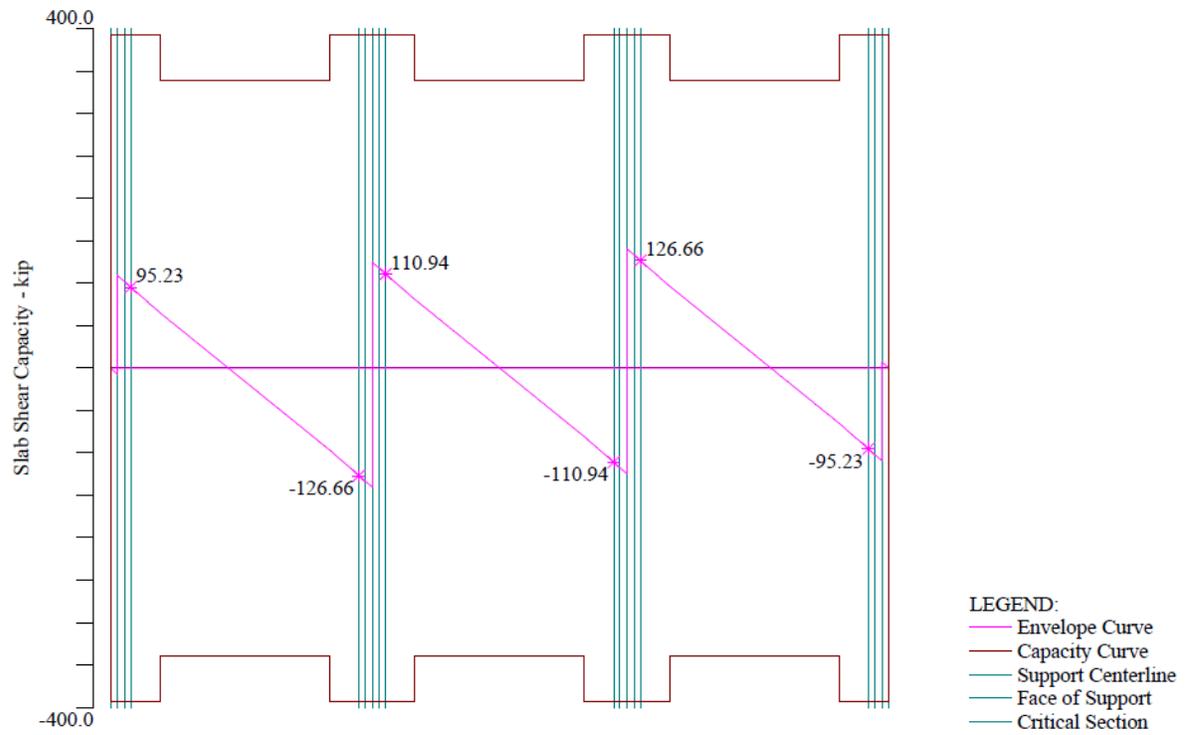
Frame: Interior Frame

Engineer: SP

Code: ACI 318-14

Date: 03/16/17

Time: 15:46:19



spSlab v5.00. Licensed to: StructurePoint. License ID: 66184-1055152-4-2C6B6-2C6B6

File: C:\TSDA\TSDA-spSlab-Two-Way Slab with Drop Panels.slb

Project: Two-Way Slab with Drop Panels

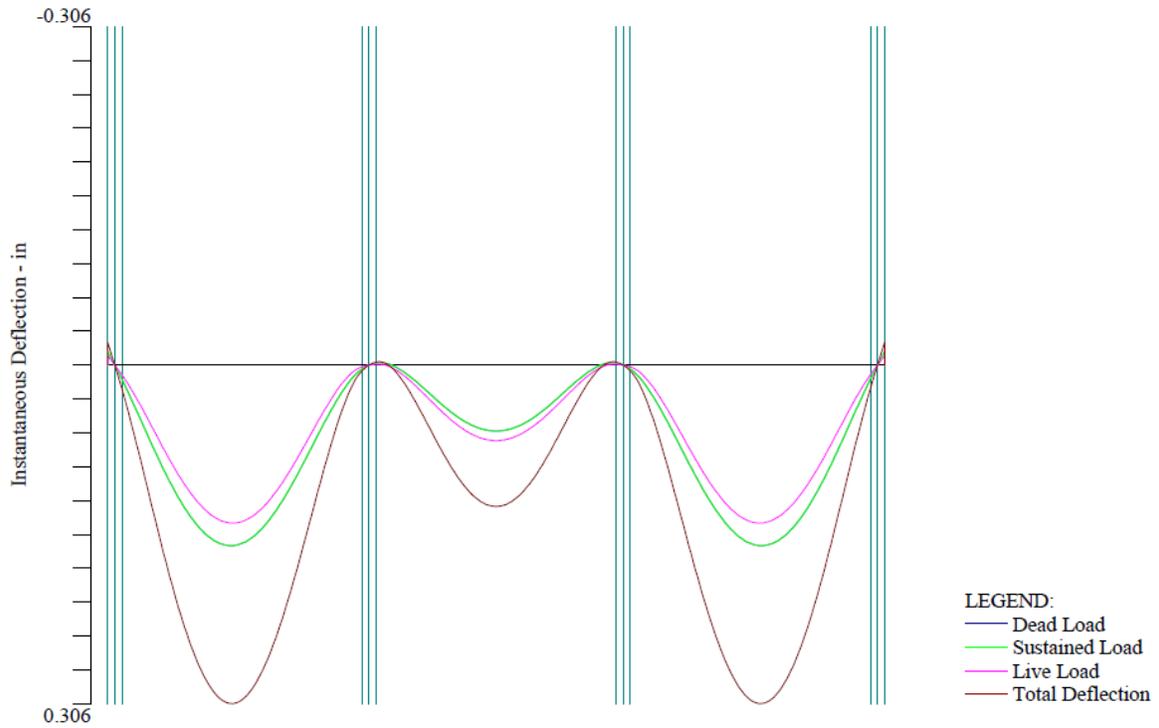
Frame: Interior Frame

Engineer: SP

Code: ACI 318-14

Date: 03/16/17

Time: 15:48:42



spSlab v5.00. Licensed to: StructurePoint. License ID: 66184-1055152-4-2C6B6-2C6B6

File: C:\TSDA\TSDA-spSlab-Two-Way Slab with Drop Panels.slb

Project: Two-Way Slab with Drop Panels

Frame: Interior Frame

Engineer: SP

Code: ACI 318-14

Date: 03/16/17

Time: 15:49:51


```

          000000  0
          00  00  00
000000  000000  00  00  00  000000  00
00  0  00  00  00  00  0  00  00
00  00  00  00  000  00  000000  000000
000000  00  00  000  00  00  00  00  00  00
          00  000000  00  00  00  00  00  00  00
0  00  00  00  00  00  00  0  00  00  00  00
000000  00  000000  000  000000  0  000000  (TM)
    
```

```

=====
                          spSlab v5.00 (TM)
A Computer Program for Analysis, Design, and Investigation of
Reinforced Concrete Beams, One-way and Two-way Slab Systems
Copyright © 2003-2015, STRUCTUREPOINT, LLC
All rights reserved
=====
    
```

Licensee stated above acknowledges that STRUCTUREPOINT (SP) is not and cannot be responsible for either the accuracy or adequacy of the material supplied as input for processing by the spSlab computer program. Furthermore, STRUCTUREPOINT neither makes any warranty expressed nor implied with respect to the correctness of the output prepared by the spSlab program. Although STRUCTUREPOINT has endeavored to produce spSlab error free the program is not and cannot be certified infallible. The final and only responsibility for analysis, design and engineering documents is the licensee's. Accordingly, STRUCTUREPOINT disclaims all responsibility in contract, negligence or other tort for any analysis, design or engineering documents prepared in connection with the use of the spSlab program.

[1] INPUT ECHO

General Information

```

=====
File name: C:\TSDA\TSDA-spSlab-Two-Way Slab with Drop Panels.slb
Project: Two-Way Slab with Drop Panels
Frame: Interior Frame
Engineer: SP
Code: ACI 318-14
Reinforcement Database: ASTM A615
Mode: Design
Number of supports = 4 + Left cantilever + Right cantilever
Floor System: Two-Way

Live load pattern ratio = 0%
Minimum free edge distance for punching shear = 4 times slab thickness.
Circular critical section around circular supports used (if possible).
Deflections are based on cracked section properties.
In negative moment regions, Ig and Mcr DO NOT include flange/slab contribution (if available)
Long-term deflections are calculated for load duration of 60 months.
0% of live load is sustained.
Compression reinforcement calculations NOT selected.
Default incremental rebar design selected.
User-defined slab strip widths NOT selected.
User-defined distribution factors NOT selected.
One-way shear in drop panel selected.
Distribution of shear to strips NOT selected.
Beam T-section design NOT selected.
Longitudinal beam contribution in negative reinforcement design over support NOT selected.
Transverse beam contribution in negative reinforcement design over support NOT selected.
    
```

Material Properties

```

=====
          Slabs|Beams          Columns
          -----          -----
wc =          150          150 lb/ft3
f'c =          5          6 ksi
Ec =          4286.8          4696 ksi
fr =          0.53033          0.58095 ksi

fy =          60 ksi, Bars are not epoxy-coated
fyt =          60 ksi
Es =          29000 ksi
    
```

Reinforcement Database

```

Units: Db (in), Ab (in^2), Wb (lb/ft)
Size      Db      Ab      Wb      Size      Db      Ab      Wb
-----
#3      0.38      0.11      0.38      #4      0.50      0.20      0.67
#5      0.63      0.31      1.04      #6      0.75      0.44      1.50
#7      0.88      0.60      2.04      #8      1.00      0.79      2.67
#9      1.13      1.00      3.40      #10     1.27      1.27      4.30
    
```

spSlab v5.00 © StructurePoint
Licensed to: StructurePoint, License ID: 66184-1055152-4-2C6B6-2C6B6
C:\TSDA\TSDA-spSlab-Two-Way Slab with Drop Panels.slb

03-16-2017, 03:51:55 PM

Page 2

| | | | | | | | |
|-----|------|------|-------|-----|------|------|------|
| #11 | 1.41 | 1.56 | 5.31 | #14 | 1.69 | 2.25 | 7.65 |
| #18 | 2.26 | 4.00 | 13.60 | | | | |

Span Data

Slabs

Units: L1, wL, wR, L2L, L2R (ft); t, Hmin (in)

| Span Loc | L1 | t | wL | wR | L2L | L2R | Hmin | |
|----------|--------|-------|--------|--------|--------|--------|-------|-------|
| 1 Int | 0.833 | 10.00 | 15.000 | 15.000 | 30.000 | 30.000 | --- | LC *i |
| 2 Int | 30.000 | 10.00 | 15.000 | 15.000 | 30.000 | 30.000 | 10.30 | *a |
| 3 Int | 30.000 | 10.00 | 15.000 | 15.000 | 30.000 | 30.000 | 9.44 | |
| 4 Int | 30.000 | 10.00 | 15.000 | 15.000 | 30.000 | 30.000 | 10.30 | *a |
| 5 Int | 0.833 | 10.00 | 15.000 | 15.000 | 30.000 | 30.000 | --- | RC *i |

NOTES:

*a - Deflection check required for panels where slab thickness (t) is less than minimum (Hmin).
Deflection check required for panels where code-specified Hmin for two-way construction doesn't apply due to:
*i - cantilever end span (LC, RC) support condition

Support Data

Columns

Units: c1a, c2a, c1b, c2b (in); Ha, Hb (ft)

| Supp | c1a | c2a | Ha | c1b | c2b | Hb | Red% |
|------|-------|-------|--------|-------|-------|--------|------|
| 1 | 20.00 | 20.00 | 13.000 | 20.00 | 20.00 | 13.000 | 100 |
| 2 | 20.00 | 20.00 | 13.000 | 20.00 | 20.00 | 13.000 | 100 |
| 3 | 20.00 | 20.00 | 13.000 | 20.00 | 20.00 | 13.000 | 100 |
| 4 | 20.00 | 20.00 | 13.000 | 20.00 | 20.00 | 13.000 | 100 |

Drop Panels

Units: h (in); L1, Lr, Wl, Wr (ft)

| Supp | h | L1 | Lr | Wl | Wr |
|------|------|-------|-------|-------|----------|
| 1 | 4.25 | 0.833 | 5.000 | 5.000 | 5.000 *b |
| 2 | 4.25 | 5.000 | 5.000 | 5.000 | 5.000 *b |
| 3 | 4.25 | 5.000 | 5.000 | 5.000 | 5.000 *b |
| 4 | 4.25 | 5.000 | 0.833 | 5.000 | 5.000 *b |

*b - Standard drop.

Boundary Conditions

Units: Kz (kip/in); Kry (kip-in/rad)

| Supp | Spring Kz | Spring Kry | Far End A | Far End B |
|------|-----------|------------|-----------|-----------|
| 1 | 0 | 0 | Fixed | Fixed |
| 2 | 0 | 0 | Fixed | Fixed |
| 3 | 0 | 0 | Fixed | Fixed |
| 4 | 0 | 0 | Fixed | Fixed |

Load Data

Load Cases and Combinations

| Case Type | SELF DEAD | Dead DEAD | Live LIVE |
|-----------|-----------|-----------|-----------|
| U1 | 1.200 | 1.200 | 1.600 |

Area Loads

Units: Wa (lb/ft2)

| Case/Patt | Span | Wa |
|-----------|------|--------|
| SELF | 1 | 125.00 |
| | 2 | 125.00 |
| | 3 | 125.00 |
| | 4 | 125.00 |
| | 5 | 125.00 |
| Dead | 2 | 20.00 |
| | 3 | 20.00 |
| | 4 | 20.00 |
| | 1 | 20.00 |
| | 5 | 20.00 |
| Live | 2 | 60.00 |
| | 1 | 60.00 |
| | 3 | 60.00 |
| | 4 | 60.00 |
| | 5 | 60.00 |

Line Loads

Units: Wa, Wb (lb/ft), La, Lb (ft)

| Case/Patt | Span | Wa | La | Wb | Lb |
|-----------|------|----|----|----|----|
|-----------|------|----|----|----|----|

spSlab v5.00 © StructurePoint
 Licensed to: StructurePoint, License ID: 66184-1055152-4-2C6B6-2C6B6
 C:\TSDA\TSDA-spSlab-Two-Way Slab with Drop Panels.slb

03-16-2017, 03:51:55 PM

Page 3

```

-----
SELF      1      531.25      -0.000      531.25      0.833
          2      531.25      0.000      531.25      5.000
          2      531.25      25.000      531.25      30.000
          3      531.25      0.000      531.25      5.000
          3      531.25      25.000      531.25      30.000
          4      531.25      0.000      531.25      5.000
          4      531.25      25.000      531.25      30.000
          5      531.25      0.000      531.25      0.833
    
```

Reinforcement Criteria

=====

Slabs and Ribs

| | Top bars | | Bottom bars | |
|-------------|----------|-------|-------------|----------|
| | Min | Max | Min | Max |
| Bar Size | #6 | #6 | #6 | #6 |
| Bar spacing | 1.00 | 18.00 | 1.00 | 18.00 in |
| Reinf ratio | 0.18 | 2.00 | 0.18 | 2.00 % |
| Cover | 0.75 | | 0.75 | in |

There is NOT more than 12 in of concrete below top bars.

Beams

| | Top bars | | Bottom bars | | Stirrups | |
|-------------|----------|-------|-------------|--------|----------|----------|
| | Min | Max | Min | Max | Min | Max |
| Bar Size | #5 | #8 | #5 | #8 | #3 | #5 |
| Bar spacing | 1.00 | 18.00 | 1.00 | 18.00 | 6.00 | 18.00 in |
| Reinf ratio | 0.14 | 5.00 | 0.14 | 5.00 % | | |
| Cover | 1.50 | | 1.50 | | | in |
| Layer dist. | 1.00 | | 1.00 | | | in |
| No. of legs | | | | | 2 | 6 |
| Side cover | | | | | 1.50 | in |
| 1st Stirrup | | | | | 3.00 | in |

There is NOT more than 12 in of concrete below top bars.

```

          oooooo  o
          oo oo oo
ooooo  oooooo  oo oo oo  oooooo  oo
oo o  oo oo  oo oo  o oo oo
oo  oo oo  ooo  oo  oooooo  oooooo
ooooo  oo oo  ooo  oo  oo oo oo oo oo
  oo  oooooo  oo oo  oo oo oo oo oo oo
o oo oo  oo oo oo o  oo oo oo oo oo
ooooo  oo  oooooo  ooo  oooooo o  oooooo  (TM)

```

```

=====
                        spSlab v5.00 (TM)
A Computer Program for Analysis, Design, and Investigation of
Reinforced Concrete Beams, One-way and Two-way Slab Systems
Copyright © 2003-2015, STRUCTUREPOINT, LLC
All rights reserved
=====

```

Licensee stated above acknowledges that STRUCTUREPOINT (SP) is not and cannot be responsible for either the accuracy or adequacy of the material supplied as input for processing by the spSlab computer program. Furthermore, STRUCTUREPOINT neither makes any warranty expressed nor implied with respect to the correctness of the output prepared by the spSlab program. Although STRUCTUREPOINT has endeavored to produce spSlab error free the program is not and cannot be certified infallible. The final and only responsibility for analysis, design and engineering documents is the licensee's. Accordingly, STRUCTUREPOINT disclaims all responsibility in contract, negligence or other tort for any analysis, design or engineering documents prepared in connection with the use of the spSlab program.

```

=====
[2] DESIGN RESULTS*
=====

```

*Unless otherwise noted, all results are in the direction of analysis only. Another analysis in the perpendicular direction has to be carried out for two-way slab systems.

Strip Widths and Distribution Factors

```

Units: Width (ft).

```

| Span | Strip | Width | | | Moment Factor | | |
|------|--------|--------|---------|---------|---------------|---------|---------|
| | | Left** | Right** | Bottom* | Left** | Right** | Bottom* |
| 1 | Column | 15.00 | 15.00 | 15.00 | 1.000 | 1.000 | 0.600 |
| | Middle | 15.00 | 15.00 | 15.00 | 0.000 | 0.000 | 0.400 |
| 2 | Column | 15.00 | 15.00 | 15.00 | 1.000 | 0.750 | 0.600 |
| | Middle | 15.00 | 15.00 | 15.00 | 0.000 | 0.250 | 0.400 |
| 3 | Column | 15.00 | 15.00 | 15.00 | 0.750 | 0.750 | 0.600 |
| | Middle | 15.00 | 15.00 | 15.00 | 0.250 | 0.250 | 0.400 |
| 4 | Column | 15.00 | 15.00 | 15.00 | 0.750 | 1.000 | 0.600 |
| | Middle | 15.00 | 15.00 | 15.00 | 0.250 | 0.000 | 0.400 |
| 5 | Column | 15.00 | 15.00 | 15.00 | 1.000 | 1.000 | 0.600 |
| | Middle | 15.00 | 15.00 | 15.00 | 0.000 | 0.000 | 0.400 |

*Used for bottom reinforcement. **Used for top reinforcement.

Top Reinforcement

```

Units: Width (ft), Mmax (k-ft), Xmax (ft), As (in^2), Sp (in)

```

| Span | Strip | Zone | Width | Mmax | Xmax | AsMin | AsMax | AsReq | SpProv | Bars |
|------|--------|---------|-------|--------|--------|-------|--------|-------|--------|-------------|
| 1 | Column | Left | 15.00 | 0.28 | 0.241 | 3.240 | 31.950 | 0.007 | 18.000 | 10-#6 *3 *5 |
| | | Midspan | 15.00 | 0.90 | 0.447 | 3.240 | 47.250 | 0.015 | 18.000 | 10-#6 *3 *5 |
| | | Right | 15.00 | 2.10 | 0.687 | 4.158 | 31.500 | 0.036 | 18.000 | 10-#6 *3 |
| | Middle | Left | 15.00 | 0.00 | 0.000 | 3.240 | 31.950 | 0.000 | 18.000 | 10-#6 *3 *5 |
| | | Midspan | 15.00 | 0.00 | 0.344 | 3.240 | 31.950 | 0.000 | 18.000 | 10-#6 *3 *5 |
| | | Right | 15.00 | 0.00 | 0.687 | 3.240 | 31.950 | 0.000 | 18.000 | 10-#6 *3 *5 |
| 2 | Column | Left | 15.00 | 244.81 | 0.833 | 4.158 | 31.500 | 4.225 | 18.000 | 10-#6 |
| | | Midspan | 15.00 | 0.00 | 15.000 | 0.000 | 31.950 | 0.000 | 0.000 | --- |
| | | Right | 15.00 | 517.57 | 29.167 | 4.158 | 31.500 | 9.137 | 8.571 | 21-#6 |
| | Middle | Left | 15.00 | 1.37 | 2.059 | 3.240 | 31.950 | 0.034 | 18.000 | 10-#6 *3 *5 |
| | | Midspan | 15.00 | 0.00 | 15.000 | 0.000 | 31.950 | 0.000 | 0.000 | --- |
| | | Right | 15.00 | 172.52 | 29.167 | 3.240 | 31.950 | 4.406 | 16.364 | 11-#6 |
| 3 | Column | Left | 15.00 | 463.59 | 0.833 | 4.158 | 31.500 | 8.147 | 8.571 | 21-#6 |
| | | Midspan | 15.00 | 0.00 | 15.000 | 0.000 | 31.950 | 0.000 | 0.000 | --- |
| | | Right | 15.00 | 463.59 | 29.167 | 4.158 | 31.500 | 8.147 | 8.571 | 21-#6 |
| | Middle | Left | 15.00 | 154.53 | 0.833 | 3.240 | 31.950 | 3.938 | 16.364 | 11-#6 *5 |

spSlab v5.00 © StructurePoint
Licensed to: StructurePoint, License ID: 66184-1055152-4-2C6B6-2C6B6
C:\TSDA\TSDA-spSlab-Two-Way Slab with Drop Panels.slb

03-16-2017, 03:52:33 PM

Page 2

| | | | | | | | | | |
|---|-------------|-------|--------|--------|-------|--------|-------|--------|-------------|
| | Midspan | 15.00 | 0.00 | 15.000 | 0.000 | 31.950 | 0.000 | 0.000 | --- |
| | Right | 15.00 | 154.53 | 29.167 | 3.240 | 31.950 | 3.938 | 16.364 | 11-#6 *5 |
| 4 | Column Left | 15.00 | 517.57 | 0.833 | 4.158 | 31.500 | 9.137 | 8.571 | 21-#6 |
| | Midspan | 15.00 | 0.00 | 15.000 | 0.000 | 31.950 | 0.000 | 0.000 | --- |
| | Right | 15.00 | 244.81 | 29.167 | 4.158 | 31.500 | 4.225 | 18.000 | 10-#6 |
| | Middle Left | 15.00 | 172.52 | 0.833 | 3.240 | 31.950 | 4.406 | 16.364 | 11-#6 |
| | Midspan | 15.00 | 0.00 | 15.000 | 0.000 | 31.950 | 0.000 | 0.000 | --- |
| | Right | 15.00 | 1.37 | 27.941 | 3.240 | 31.950 | 0.034 | 18.000 | 10-#6 *3 *5 |
| 5 | Column Left | 15.00 | 2.10 | 0.146 | 4.158 | 31.500 | 0.036 | 18.000 | 10-#6 *3 |
| | Midspan | 15.00 | 0.90 | 0.386 | 3.240 | 47.250 | 0.015 | 18.000 | 10-#6 *3 *5 |
| | Right | 15.00 | 0.28 | 0.593 | 3.240 | 31.950 | 0.007 | 18.000 | 10-#6 *3 *5 |
| | Middle Left | 15.00 | 0.00 | 0.146 | 3.240 | 31.950 | 0.000 | 18.000 | 10-#6 *3 *5 |
| | Midspan | 15.00 | 0.00 | 0.490 | 3.240 | 31.950 | 0.000 | 18.000 | 10-#6 *3 *5 |
| | Right | 15.00 | 0.00 | 0.833 | 3.240 | 31.950 | 0.000 | 18.000 | 10-#6 *3 *5 |

NOTES:

- *3 - Design governed by minimum reinforcement.
- *5 - Number of bars governed by maximum allowable spacing.

Top Bar Details

Units: Length (ft)

| Span Strip | Bars | Left | | Continuous | | Right | | | |
|------------|-------|--------|------------|------------|-------|--------|-------|--------|------------|
| | | Length | Bars | Length | Bars | Length | Bars | Length | Bars |
| 1 Column | --- | --- | --- | --- | 10-#6 | 0.83 | --- | --- | --- |
| Middle | --- | --- | --- | --- | 10-#6 | 0.83 | --- | --- | --- |
| 2 Column | 10-#6 | 10.18 | --- | --- | --- | --- | 11-#6 | 10.18 | 10-#6 6.50 |
| Middle | 10-#6 | 7.07 | --- | --- | --- | --- | 11-#6 | 9.27 | --- |
| 3 Column | 11-#6 | 10.18 | 10-#6 6.50 | --- | --- | --- | 11-#6 | 10.18 | 10-#6 6.50 |
| Middle | 11-#6 | 9.77 | --- | --- | --- | --- | 11-#6 | 9.77 | --- |
| 4 Column | 11-#6 | 10.18 | 10-#6 6.50 | --- | --- | --- | 10-#6 | 10.18 | --- |
| Middle | 11-#6 | 9.27 | --- | --- | --- | --- | 10-#6 | 7.07 | --- |
| 5 Column | --- | --- | --- | 10-#6 0.83 | --- | --- | --- | --- | --- |
| Middle | --- | --- | --- | 10-#6 0.83 | --- | --- | --- | --- | --- |

Top Bar Development Lengths

Units: Length (in)

| Span Strip | Bars | Left | | Continuous | | Right | | | |
|------------|-------|--------|-------------|-------------|-------|--------|-------|--------|-------------|
| | | DevLen | Bars | DevLen | Bars | DevLen | Bars | DevLen | Bars |
| 1 Column | --- | --- | --- | --- | 10-#6 | 12.00 | --- | --- | --- |
| Middle | --- | --- | --- | --- | 10-#6 | 12.00 | --- | --- | --- |
| 2 Column | 10-#6 | 24.44 | --- | --- | --- | --- | 11-#6 | 25.17 | 10-#6 25.17 |
| Middle | 10-#6 | 12.00 | --- | --- | --- | --- | 11-#6 | 23.17 | --- |
| 3 Column | 11-#6 | 22.44 | 10-#6 22.44 | --- | --- | --- | 11-#6 | 22.44 | 10-#6 22.44 |
| Middle | 11-#6 | 20.71 | --- | --- | --- | --- | 11-#6 | 20.71 | --- |
| 4 Column | 11-#6 | 25.17 | 10-#6 25.17 | --- | --- | --- | 10-#6 | 24.44 | --- |
| Middle | 11-#6 | 23.17 | --- | --- | --- | --- | 10-#6 | 12.00 | --- |
| 5 Column | --- | --- | --- | 10-#6 12.00 | --- | --- | --- | --- | --- |
| Middle | --- | --- | --- | 10-#6 12.00 | --- | --- | --- | --- | --- |

Bottom Reinforcement

Units: Width (ft), Mmax (k-ft), Xmax (ft), As (in²), Sp (in)

| Span Strip | Width | Mmax | Xmax | AsMin | AsMax | AsReq | SpProv | Bars |
|------------|-------|--------|--------|-------|--------|-------|--------|-------------|
| 1 Column | 15.00 | 0.00 | 0.344 | 0.000 | 31.950 | 0.000 | 0.000 | --- |
| Middle | 15.00 | 0.00 | 0.344 | 0.000 | 31.950 | 0.000 | 0.000 | --- |
| 2 Column | 15.00 | 219.68 | 13.000 | 3.240 | 31.950 | 5.641 | 13.846 | 13-#6 |
| Middle | 15.00 | 146.45 | 13.000 | 3.240 | 31.950 | 3.728 | 18.000 | 10-#6 *5 |
| 3 Column | 15.00 | 120.14 | 15.000 | 3.240 | 31.950 | 3.049 | 18.000 | 10-#6 *3 *5 |
| Middle | 15.00 | 80.09 | 15.000 | 3.240 | 31.950 | 2.024 | 18.000 | 10-#6 *3 *5 |
| 4 Column | 15.00 | 219.68 | 17.000 | 3.240 | 31.950 | 5.641 | 13.846 | 13-#6 |
| Middle | 15.00 | 146.45 | 17.000 | 3.240 | 31.950 | 3.728 | 18.000 | 10-#6 *5 |
| 5 Column | 15.00 | 0.00 | 0.490 | 0.000 | 31.950 | 0.000 | 0.000 | --- |
| Middle | 15.00 | 0.00 | 0.490 | 0.000 | 31.950 | 0.000 | 0.000 | --- |

NOTES:

- *3 - Design governed by minimum reinforcement.
- *5 - Number of bars governed by maximum allowable spacing.

Bottom Bar Details

Units: Start (ft), Length (ft)

| Span Strip | Long Bars | | | Short Bars | | |
|------------|-----------|-------|--------|------------|-------|--------|
| | Bars | Start | Length | Bars | Start | Length |
| 1 Column | --- | | | --- | | |
| Middle | --- | | | --- | | |
| 2 Column | 13-#6 | 0.00 | 30.00 | --- | | |
| Middle | 8-#6 | 0.00 | 30.00 | 2-#6 | 0.00 | 25.50 |
| 3 Column | 10-#6 | 0.00 | 30.00 | --- | | |
| Middle | 8-#6 | 0.00 | 30.00 | 2-#6 | 4.50 | 21.00 |
| 4 Column | 13-#6 | 0.00 | 30.00 | --- | | |
| Middle | 8-#6 | 0.00 | 30.00 | 2-#6 | 4.50 | 25.50 |
| 5 Column | --- | | | --- | | |
| Middle | --- | | | --- | | |

Bottom Bar Development Lengths

Units: DevLen (in)

| Span Strip | Long Bars | | Short Bars | |
|------------|-----------|--------|------------|--------|
| | Bars | DevLen | Bars | DevLen |
| 1 Column | --- | | --- | |
| Middle | --- | | --- | |
| 2 Column | 13-#6 | 25.10 | --- | |
| Middle | 8-#6 | 21.57 | 2-#6 | 21.57 |
| 3 Column | 10-#6 | 17.64 | --- | |
| Middle | 8-#6 | 12.00 | 2-#6 | 12.00 |
| 4 Column | 13-#6 | 25.10 | --- | |
| Middle | 8-#6 | 21.57 | 2-#6 | 21.57 |
| 5 Column | --- | | --- | |
| Middle | --- | | --- | |

Flexural Capacity

Units: x (ft), As (in²), PhiMn, Mu (k-ft)

| Span Strip | Top | | | | | | Bottom | | | | | |
|------------|--------|----------|---------|---------|----------|---------|--------|--------|--------|----------|--------|--------|
| | x | AsTop | PhiMn- | Mu- | Comb Pat | Status | AsBot | PhiMn+ | Mu+ | Comb Pat | Status | |
| 1 Column | 0.000 | 4.40 | -172.31 | 0.00 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK | |
| | 0.241 | 4.40 | -256.46 | -0.28 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK | |
| | 0.417 | 4.40 | -256.46 | -0.76 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK | |
| | 0.447 | 4.40 | -254.75 | -0.90 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK | |
| | 0.687 | 4.40 | -254.75 | -2.10 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK | |
| | 0.833 | 4.40 | -254.75 | -3.03 | U1 All | --- | 0.00 | 0.00 | 0.00 | U1 All | --- | |
| | Middle | 0.000 | 4.40 | -172.31 | 0.00 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |
| | | 0.241 | 4.40 | -172.31 | -0.00 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |
| | | 0.417 | 4.40 | -172.31 | -0.00 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |
| | | 0.447 | 4.40 | -172.31 | -0.00 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |
| | | 0.687 | 4.40 | -172.31 | -0.00 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |
| | | 0.833 | 4.40 | -172.31 | -0.00 | U1 All | --- | 0.00 | 0.00 | 0.00 | U1 All | --- |
| | | 2 Column | 0.000 | 4.40 | -254.75 | -335.03 | U1 All | --- | 5.72 | 222.67 | 0.00 | U1 All |
| | 0.625 | | 4.40 | -254.75 | -266.67 | U1 All | --- | 5.72 | 222.67 | 0.00 | U1 All | --- |
| 0.833 | 4.40 | | -254.75 | -244.81 | U1 All | OK | 5.72 | 222.67 | 0.00 | U1 All | OK | |
| 5.000 | 4.40 | | -254.75 | 0.00 | U1 All | OK | 5.72 | 222.67 | 61.82 | U1 All | OK | |
| 5.000 | 4.40 | | -172.31 | 0.00 | U1 All | OK | 5.72 | 222.67 | 61.84 | U1 All | OK | |
| 8.146 | 4.40 | | -172.31 | 0.00 | U1 All | OK | 5.72 | 222.67 | 160.99 | U1 All | OK | |
| 10.183 | 0.00 | | 0.00 | 0.00 | U1 All | OK | 5.72 | 222.67 | 199.55 | U1 All | OK | |
| 10.750 | 0.00 | | 0.00 | 0.00 | U1 All | OK | 5.72 | 222.67 | 206.72 | U1 All | OK | |
| 13.000 | 0.00 | | 0.00 | 0.00 | U1 All | OK | 5.72 | 222.67 | 219.68 | U1 All | OK | |
| 15.000 | 0.00 | | 0.00 | 0.00 | U1 All | OK | 5.72 | 222.67 | 210.54 | U1 All | OK | |
| 19.250 | 0.00 | | 0.00 | 0.00 | U1 All | OK | 5.72 | 222.67 | 126.57 | U1 All | OK | |
| 19.817 | 0.00 | | 0.00 | 0.00 | U1 All | OK | 5.72 | 222.67 | 108.71 | U1 All | OK | |
| 21.914 | 4.84 | | -189.16 | 0.00 | U1 All | OK | 5.72 | 222.67 | 29.13 | U1 All | OK | |
| 23.500 | 4.84 | | -189.16 | -60.24 | U1 All | OK | 5.72 | 222.67 | 0.00 | U1 All | OK | |
| 25.000 | 7.99 | -307.67 | -166.19 | U1 All | OK | 5.72 | 222.67 | 0.00 | U1 All | OK | | |
| 25.000 | 7.99 | -454.84 | -166.23 | U1 All | OK | 5.72 | 222.67 | 0.00 | U1 All | OK | | |
| 25.598 | 9.24 | -523.14 | -211.55 | U1 All | OK | 5.72 | 222.67 | 0.00 | U1 All | OK | | |
| 29.167 | 9.24 | -523.14 | -517.57 | U1 All | OK | 5.72 | 222.67 | 0.00 | U1 All | OK | | |
| 29.375 | 9.24 | -523.14 | -537.19 | U1 All | --- | 5.72 | 222.67 | 0.00 | U1 All | --- | | |
| 30.000 | 9.24 | -523.14 | -597.13 | U1 All | --- | 5.72 | 222.67 | 0.00 | U1 All | --- | | |
| Middle | 0.000 | 4.40 | -172.31 | 2.45 | U1 All | --- | 4.40 | 172.31 | 0.00 | U1 All | --- | |
| | 0.833 | 4.40 | -172.31 | -0.00 | U1 All | OK | 4.40 | 172.31 | 0.00 | U1 All | OK | |
| | 2.059 | 4.40 | -172.31 | -1.37 | U1 All | OK | 4.40 | 172.31 | 0.00 | U1 All | OK | |
| | 6.067 | 4.40 | -172.31 | 0.00 | U1 All | OK | 4.40 | 172.31 | 67.21 | U1 All | OK | |
| | 7.067 | 0.00 | 0.00 | 0.00 | U1 All | OK | 4.40 | 172.31 | 88.25 | U1 All | OK | |
| | 10.750 | 0.00 | 0.00 | 0.00 | U1 All | OK | 4.40 | 172.31 | 137.81 | U1 All | OK | |

| | | | | | | | | | | | |
|----------|--------|------|---------|---------|--------|-----|------|--------|--------|--------|-----|
| | 13.000 | 0.00 | 0.00 | 0.00 | U1 All | OK | 4.40 | 172.31 | 146.45 | U1 All | OK |
| | 15.000 | 0.00 | 0.00 | 0.00 | U1 All | OK | 4.40 | 172.31 | 140.36 | U1 All | OK |
| | 19.250 | 0.00 | 0.00 | 0.00 | U1 All | OK | 4.40 | 172.31 | 84.38 | U1 All | OK |
| | 20.729 | 0.00 | 0.00 | 0.00 | U1 All | OK | 4.40 | 172.31 | 51.16 | U1 All | OK |
| | 22.660 | 4.84 | -189.16 | -1.38 | U1 All | OK | 4.40 | 172.31 | 0.00 | U1 All | OK |
| | 23.702 | 4.84 | -189.16 | -18.69 | U1 All | OK | 4.40 | 172.31 | 0.00 | U1 All | OK |
| | 25.500 | 4.84 | -189.16 | -56.75 | U1 All | OK | 3.52 | 138.39 | 0.00 | U1 All | OK |
| | 29.167 | 4.84 | -189.16 | -172.52 | U1 All | OK | 3.52 | 138.39 | 0.00 | U1 All | OK |
| | 29.583 | 4.84 | -189.16 | -189.32 | U1 All | --- | 3.52 | 138.39 | 0.00 | U1 All | --- |
| | 30.000 | 4.84 | -189.16 | -206.93 | U1 All | --- | 3.52 | 138.39 | 0.00 | U1 All | --- |
| 3 Column | 0.000 | 9.24 | -523.14 | -539.24 | U1 All | --- | 4.40 | 172.31 | 0.00 | U1 All | --- |
| | 0.833 | 9.24 | -523.14 | -463.59 | U1 All | OK | 4.40 | 172.31 | 0.00 | U1 All | OK |
| | 4.630 | 9.24 | -523.14 | -176.57 | U1 All | OK | 4.40 | 172.31 | 0.00 | U1 All | OK |
| | 5.000 | 8.37 | -475.78 | -153.60 | U1 All | OK | 4.40 | 172.31 | 0.00 | U1 All | OK |
| | 5.000 | 8.37 | -321.84 | -153.56 | U1 All | OK | 4.40 | 172.31 | 0.00 | U1 All | OK |
| | 6.500 | 4.84 | -189.16 | -69.29 | U1 All | OK | 4.40 | 172.31 | 0.00 | U1 All | OK |
| | 8.313 | 4.84 | -189.16 | 0.00 | U1 All | OK | 4.40 | 172.31 | 11.45 | U1 All | OK |
| | 10.183 | 0.00 | 0.00 | 0.00 | U1 All | OK | 4.40 | 172.31 | 63.73 | U1 All | OK |
| | 10.750 | 0.00 | 0.00 | 0.00 | U1 All | OK | 4.40 | 172.31 | 76.24 | U1 All | OK |
| | 15.000 | 0.00 | 0.00 | 0.00 | U1 All | OK | 4.40 | 172.31 | 120.14 | U1 All | OK |
| | 19.250 | 0.00 | 0.00 | 0.00 | U1 All | OK | 4.40 | 172.31 | 76.24 | U1 All | OK |
| | 19.817 | 0.00 | 0.00 | 0.00 | U1 All | OK | 4.40 | 172.31 | 63.73 | U1 All | OK |
| | 21.687 | 4.84 | -189.16 | 0.00 | U1 All | OK | 4.40 | 172.31 | 11.45 | U1 All | OK |
| | 23.500 | 4.84 | -189.16 | -69.29 | U1 All | OK | 4.40 | 172.31 | 0.00 | U1 All | OK |
| | 25.000 | 8.37 | -321.84 | -153.56 | U1 All | OK | 4.40 | 172.31 | 0.00 | U1 All | OK |
| | 25.000 | 8.37 | -475.78 | -153.60 | U1 All | OK | 4.40 | 172.31 | 0.00 | U1 All | OK |
| | 25.370 | 9.24 | -523.14 | -176.57 | U1 All | OK | 4.40 | 172.31 | 0.00 | U1 All | OK |
| | 29.167 | 9.24 | -523.14 | -463.59 | U1 All | OK | 4.40 | 172.31 | 0.00 | U1 All | OK |
| | 30.000 | 9.24 | -523.14 | -539.24 | U1 All | --- | 4.40 | 172.31 | 0.00 | U1 All | --- |
| Middle | 0.000 | 4.84 | -189.16 | -179.75 | U1 All | --- | 3.52 | 138.39 | 0.00 | U1 All | --- |
| | 0.833 | 4.84 | -189.16 | -154.53 | U1 All | OK | 3.52 | 138.39 | 0.00 | U1 All | OK |
| | 4.500 | 4.84 | -189.16 | -61.59 | U1 All | OK | 3.52 | 138.39 | 0.00 | U1 All | OK |
| | 5.500 | 4.84 | -189.16 | -41.32 | U1 All | OK | 4.40 | 172.31 | 0.00 | U1 All | OK |
| | 8.045 | 4.84 | -189.16 | 0.00 | U1 All | OK | 4.40 | 172.31 | 1.71 | U1 All | OK |
| | 9.771 | 0.00 | 0.00 | 0.00 | U1 All | OK | 4.40 | 172.31 | 35.79 | U1 All | OK |
| | 10.750 | 0.00 | 0.00 | 0.00 | U1 All | OK | 4.40 | 172.31 | 50.83 | U1 All | OK |
| | 15.000 | 0.00 | 0.00 | 0.00 | U1 All | OK | 4.40 | 172.31 | 80.09 | U1 All | OK |
| | 19.250 | 0.00 | 0.00 | 0.00 | U1 All | OK | 4.40 | 172.31 | 50.83 | U1 All | OK |
| | 20.229 | 0.00 | 0.00 | 0.00 | U1 All | OK | 4.40 | 172.31 | 35.79 | U1 All | OK |
| | 21.955 | 4.84 | -189.16 | 0.00 | U1 All | OK | 4.40 | 172.31 | 1.71 | U1 All | OK |
| | 24.500 | 4.84 | -189.16 | -41.32 | U1 All | OK | 4.40 | 172.31 | 0.00 | U1 All | OK |
| | 25.500 | 4.84 | -189.16 | -61.59 | U1 All | OK | 3.52 | 138.39 | 0.00 | U1 All | OK |
| | 29.167 | 4.84 | -189.16 | -154.53 | U1 All | OK | 3.52 | 138.39 | 0.00 | U1 All | OK |
| | 30.000 | 4.84 | -189.16 | -179.75 | U1 All | --- | 3.52 | 138.39 | 0.00 | U1 All | --- |
| 4 Column | 0.000 | 9.24 | -523.14 | -597.13 | U1 All | --- | 5.72 | 222.67 | 0.00 | U1 All | --- |
| | 0.625 | 9.24 | -523.14 | -537.19 | U1 All | --- | 5.72 | 222.67 | 0.00 | U1 All | --- |
| | 0.833 | 9.24 | -523.14 | -517.57 | U1 All | OK | 5.72 | 222.67 | 0.00 | U1 All | OK |
| | 4.402 | 9.24 | -523.14 | -211.55 | U1 All | OK | 5.72 | 222.67 | 0.00 | U1 All | OK |
| | 5.000 | 7.99 | -454.84 | -166.23 | U1 All | OK | 5.72 | 222.67 | 0.00 | U1 All | OK |
| | 5.000 | 7.99 | -307.67 | -166.19 | U1 All | OK | 5.72 | 222.67 | 0.00 | U1 All | OK |
| | 6.500 | 4.84 | -189.16 | -60.24 | U1 All | OK | 5.72 | 222.67 | 0.00 | U1 All | OK |
| | 8.086 | 4.84 | -189.16 | 0.00 | U1 All | OK | 5.72 | 222.67 | 29.13 | U1 All | OK |
| | 10.183 | 0.00 | 0.00 | 0.00 | U1 All | OK | 5.72 | 222.67 | 108.71 | U1 All | OK |
| | 10.750 | 0.00 | 0.00 | 0.00 | U1 All | OK | 5.72 | 222.67 | 126.57 | U1 All | OK |
| | 15.000 | 0.00 | 0.00 | 0.00 | U1 All | OK | 5.72 | 222.67 | 210.54 | U1 All | OK |
| | 17.000 | 0.00 | 0.00 | 0.00 | U1 All | OK | 5.72 | 222.67 | 219.68 | U1 All | OK |
| | 19.250 | 0.00 | 0.00 | 0.00 | U1 All | OK | 5.72 | 222.67 | 206.72 | U1 All | OK |
| | 19.817 | 0.00 | 0.00 | 0.00 | U1 All | OK | 5.72 | 222.67 | 199.55 | U1 All | OK |
| | 21.854 | 4.40 | -172.31 | 0.00 | U1 All | OK | 5.72 | 222.67 | 160.99 | U1 All | OK |
| | 25.000 | 4.40 | -172.31 | 0.00 | U1 All | OK | 5.72 | 222.67 | 61.84 | U1 All | OK |
| | 25.000 | 4.40 | -254.75 | 0.00 | U1 All | OK | 5.72 | 222.67 | 61.82 | U1 All | OK |
| | 29.167 | 4.40 | -254.75 | -244.81 | U1 All | OK | 5.72 | 222.67 | 0.00 | U1 All | OK |
| | 29.375 | 4.40 | -254.75 | -266.68 | U1 All | --- | 5.72 | 222.67 | 0.00 | U1 All | --- |
| | 30.000 | 4.40 | -254.75 | -335.03 | U1 All | --- | 5.72 | 222.67 | 0.00 | U1 All | --- |
| Middle | 0.000 | 4.84 | -189.16 | -206.93 | U1 All | --- | 3.52 | 138.39 | 0.00 | U1 All | --- |
| | 0.417 | 4.84 | -189.16 | -189.32 | U1 All | --- | 3.52 | 138.39 | 0.00 | U1 All | --- |
| | 0.833 | 4.84 | -189.16 | -172.52 | U1 All | OK | 3.52 | 138.39 | 0.00 | U1 All | OK |
| | 4.500 | 4.84 | -189.16 | -56.75 | U1 All | OK | 3.52 | 138.39 | 0.00 | U1 All | OK |
| | 6.298 | 4.84 | -189.16 | -18.69 | U1 All | OK | 4.40 | 172.31 | 0.00 | U1 All | OK |
| | 7.340 | 4.84 | -189.16 | -1.38 | U1 All | OK | 4.40 | 172.31 | 0.00 | U1 All | OK |
| | 9.271 | 0.00 | 0.00 | 0.00 | U1 All | OK | 4.40 | 172.31 | 51.16 | U1 All | OK |
| | 10.750 | 0.00 | 0.00 | 0.00 | U1 All | OK | 4.40 | 172.31 | 84.38 | U1 All | OK |
| | 15.000 | 0.00 | 0.00 | 0.00 | U1 All | OK | 4.40 | 172.31 | 140.36 | U1 All | OK |
| | 17.000 | 0.00 | 0.00 | 0.00 | U1 All | OK | 4.40 | 172.31 | 146.45 | U1 All | OK |
| | 19.250 | 0.00 | 0.00 | 0.00 | U1 All | OK | 4.40 | 172.31 | 137.81 | U1 All | OK |
| | 22.933 | 0.00 | 0.00 | 0.00 | U1 All | OK | 4.40 | 172.31 | 88.25 | U1 All | OK |
| | 23.933 | 4.40 | -172.31 | 0.00 | U1 All | OK | 4.40 | 172.31 | 67.21 | U1 All | OK |
| | 27.941 | 4.40 | -172.31 | -1.37 | U1 All | OK | 4.40 | 172.31 | 0.00 | U1 All | OK |
| | 29.167 | 4.40 | -172.31 | -0.00 | U1 All | OK | 4.40 | 172.31 | 0.00 | U1 All | OK |
| | 30.000 | 4.40 | -172.31 | 2.45 | U1 All | --- | 4.40 | 172.31 | 0.00 | U1 All | --- |
| 5 Column | 0.000 | 4.40 | -254.75 | -3.03 | U1 All | --- | 0.00 | 0.00 | 0.00 | U1 All | --- |
| | 0.146 | 4.40 | -254.75 | -2.10 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |
| | 0.386 | 4.40 | -256.46 | -0.90 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |
| | 0.417 | 4.40 | -256.46 | -0.76 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |

spSlab v5.00 © StructurePoint
Licensed to: StructurePoint, License ID: 66184-1055152-4-2C6B6-2C6B6
C:\TSDA\TSDA-spSlab-Two-Way Slab with Drop Panels.slb

03-16-2017, 03:52:33 PM

Page 5

| | | | | | | | | | |
|--------|-------|------|---------|-------|------------|------|------|------|------------|
| | 0.593 | 4.40 | -172.31 | -0.28 | U1 All OK | 0.00 | 0.00 | 0.00 | U1 All OK |
| | 0.833 | 4.40 | -172.31 | -0.00 | U1 All OK | 0.00 | 0.00 | 0.00 | U1 All OK |
| Middle | 0.000 | 4.40 | -172.31 | -0.00 | U1 All --- | 0.00 | 0.00 | 0.00 | U1 All --- |
| | 0.146 | 4.40 | -172.31 | -0.00 | U1 All OK | 0.00 | 0.00 | 0.00 | U1 All OK |
| | 0.386 | 4.40 | -172.31 | -0.00 | U1 All OK | 0.00 | 0.00 | 0.00 | U1 All OK |
| | 0.417 | 4.40 | -172.31 | -0.00 | U1 All OK | 0.00 | 0.00 | 0.00 | U1 All OK |
| | 0.593 | 4.40 | -172.31 | -0.00 | U1 All OK | 0.00 | 0.00 | 0.00 | U1 All OK |
| | 0.833 | 4.40 | -172.31 | -0.00 | U1 All OK | 0.00 | 0.00 | 0.00 | U1 All OK |

Slab Shear Capacity

Units: b, d (in), Xu (ft), PhiVc, Vu(kip)

| Span | b | d | Vratio | PhiVc | Vu | Xu |
|------|--------|-------|--------|--------|--------|-------|
| 1 | 360.00 | 8.88 | 1.000 | 338.88 | 7.28 | -0.00 |
| | 360.00 | 10.29 | 1.000 | 392.97 | 7.28 | -0.00 |
| 2 | 360.00 | 10.29 | 1.000 | 392.97 | 95.23 | 1.57 |
| | 360.00 | 8.88 | 1.000 | 338.88 | 96.72 | 25.00 |
| | 360.00 | 10.29 | 1.000 | 392.97 | 126.66 | 28.43 |
| 3 | 360.00 | 10.29 | 1.000 | 392.97 | 110.94 | 1.57 |
| | 360.00 | 8.88 | 1.000 | 338.88 | 81.00 | 25.00 |
| | 360.00 | 10.29 | 1.000 | 392.97 | 110.94 | 28.43 |
| 4 | 360.00 | 10.29 | 1.000 | 392.97 | 126.66 | 1.57 |
| | 360.00 | 8.88 | 1.000 | 338.88 | 96.72 | 5.00 |
| | 360.00 | 10.29 | 1.000 | 392.97 | 95.23 | 28.43 |
| 5 | 360.00 | 10.29 | 1.000 | 392.97 | 0.00 | 0.83 |
| | 360.00 | 8.88 | 1.000 | 338.88 | 0.00 | 0.83 |

Flexural Transfer of Negative Unbalanced Moment at Supports

Units: Width (in), Munb (k-ft), As (in^2)

| Supp | Width | Width-c | d | Munb | Comb | Pat | GammaF | AsReq | AsProv | Add Bars |
|------|-------|---------|-------|--------|------|-----|--------|-------|--------|----------|
| 1 | 62.75 | 62.75 | 13.13 | 329.55 | U1 | All | 0.626 | 3.605 | 1.534 | 5-#6 |
| 2 | 62.75 | 62.75 | 13.13 | 85.07 | U1 | All | 0.600 | 0.871 | 3.221 | --- |
| 3 | 62.75 | 62.75 | 13.13 | 85.07 | U1 | All | 0.600 | 0.871 | 3.221 | --- |
| 4 | 62.75 | 62.75 | 13.13 | 329.55 | U1 | All | 0.626 | 3.605 | 1.534 | 5-#6 |

Punching Shear Around Columns

Critical Section Properties

Units: b1, b2, b0, davg, CG, c(left), c(right) (in), Ac (in^2), Jc (in^4)

| Supp | Type | b1 | b2 | b0 | davg | CG | c(left) | c(right) | Ac | Jc |
|------|------|-------|-------|--------|-------|-------|---------|----------|--------|-------------|
| 1 | Rect | 26.56 | 33.13 | 86.25 | 13.13 | 8.38 | 18.38 | 8.18 | 1132 | 98239 |
| 2 | Rect | 33.13 | 33.13 | 132.50 | 13.13 | 0.00 | 16.56 | 16.56 | 1739.1 | 3.3052e+005 |
| 3 | Rect | 33.13 | 33.13 | 132.50 | 13.13 | 0.00 | 16.56 | 16.56 | 1739.1 | 3.3052e+005 |
| 4 | Rect | 26.56 | 33.13 | 86.25 | 13.13 | -8.38 | 8.18 | 18.38 | 1132 | 98239 |

Punching Shear Results

Units: Vu (kip), Munb (k-ft), vu (psi), Phi*vc (psi)

| Supp | Vu | Munb | Comb | Pat | GammaV | vu | Phi*vc |
|------|--------|-------|------|-----|--------|-------|--------|
| 1 | 114.58 | 101.2 | U1 | All | 0.374 | 194.4 | 212.1 |
| 2 | 262.99 | 151.2 | U1 | All | 0.400 | 171.7 | 212.1 |
| 3 | 262.99 | 151.2 | U1 | All | 0.400 | 171.7 | 212.1 |
| 4 | 114.58 | 101.2 | U1 | All | 0.374 | 194.4 | 212.1 |

Punching Shear Around Drops

Critical Section Properties

Units: b1, b2, b0, davg, CG, c(left), c(right) (in), Ac (in^2), Jc (in^4)

| Supp | Type | b1 | b2 | b0 | davg | CG | c(left) | c(right) | Ac | Jc |
|------|------|--------|--------|--------|------|--------|---------|----------|--------|-------------|
| 1 | Rect | 74.44 | 128.88 | 277.75 | 8.88 | 44.49 | 54.49 | 19.95 | 2465 | 1.468e+006 |
| 2 | Rect | 128.88 | 128.88 | 515.50 | 8.88 | 0.00 | 64.44 | 64.44 | 4575.1 | 1.2679e+007 |
| 3 | Rect | 128.88 | 128.88 | 515.50 | 8.88 | 0.00 | 64.44 | 64.44 | 4575.1 | 1.2679e+007 |
| 4 | Rect | 74.44 | 128.88 | 277.75 | 8.88 | -44.49 | 19.95 | 54.49 | 2465 | 1.468e+006 |

Punching Shear Results

Units: Vu (kip), vu (psi), Phi*vc (psi)

| Supp | Vu | Comb | Pat | vu | Phi*vc |
|------|--------|------|-----|------|--------|
| 1 | 98.24 | U1 | All | 39.9 | 156.9 |
| 2 | 233.91 | U1 | All | 51.1 | 142.6 |
| 3 | 233.91 | U1 | All | 51.1 | 142.6 |
| 4 | 98.24 | U1 | All | 39.9 | 156.9 |

Material Takeoff

Reinforcement in the Direction of Analysis

Top Bars: 2261.0 lb <=> 24.67 lb/ft <=> 0.822 lb/ft^2

spSlab v5.00 © StructurePoint
Licensed to: StructurePoint, License ID: 66184-1055152-4-2C6B6-2C6B6
C:\TSDA\TSDA-spSlab-Two-Way Slab with Drop Panels.slb

03-16-2017, 03:52:33 PM

Page 6

| | | | | | |
|--------------|------------------------|-----|---------------------------|-----|--|
| Bottom Bars: | 2919.9 lb | <=> | 31.85 lb/ft | <=> | 1.062 lb/ft ² |
| Stirrups: | 0.0 lb | <=> | 0.00 lb/ft | <=> | 0.000 lb/ft ² |
| Total Steel: | 5180.9 lb | <=> | 56.52 lb/ft | <=> | 1.884 lb/ft ² |
| Concrete: | 2403.8 ft ³ | <=> | 26.22 ft ³ /ft | <=> | 0.874 ft ³ /ft ² |

```

          oooooo  o
          oo  oo  oo
          oooooo  oo  oooooo  oo
          oo  o  oo  oo  oo  oo  oo  oo
          oo  oo  oo  oo  oo  oooooo  oooooo
          oooooo  oo  oo  oo  oo  oo  oo  oo  oo
          oo  oo  oooooo  oo  oo  oo  oo  oo  oo
          o  oo  oo  oo  oo  oo  oo  o  oo  oo  oo  oo
          oooooo  oo  oooooo  oo  oooooo  o  oooooo  (TM)
    
```

```

=====
                        spSlab v5.00 (TM)
A Computer Program for Analysis, Design, and Investigation of
Reinforced Concrete Beams, One-way and Two-way Slab Systems
Copyright © 2003-2015, STRUCTUREPOINT, LLC
All rights reserved
=====
    
```

Licensee stated above acknowledges that STRUCTUREPOINT (SP) is not and cannot be responsible for either the accuracy or adequacy of the material supplied as input for processing by the spSlab computer program. Furthermore, STRUCTUREPOINT neither makes any warranty expressed nor implied with respect to the correctness of the output prepared by the spSlab program. Although STRUCTUREPOINT has endeavored to produce spSlab error free the program is not and cannot be certified infallible. The final and only responsibility for analysis, design and engineering documents is the licensee's. Accordingly, STRUCTUREPOINT disclaims all responsibility in contract, negligence or other tort for any analysis, design or engineering documents prepared in connection with the use of the spSlab program.

=====

[3] DEFLECTION RESULTS

=====

Section Properties

=====

Frame Section Properties

Units: Ig, Icr (in⁴), Mcr (k-ft)

| Span Zone | M+ve | | | M-ve | | |
|-----------|-------|------|--------|-------|-------|---------|
| | Ig | Icr | Mcr | Ig | Icr | Mcr |
| 1 Left | 30000 | 0 | 265.17 | 30000 | 3641 | -265.17 |
| Midspan | 30000 | 0 | 265.17 | 30000 | 3641 | -265.17 |
| Right | 53445 | 0 | 282.33 | 53445 | 7174 | -401.42 |
| 2 Left | 53445 | 3164 | 282.33 | 53445 | 7174 | -401.42 |
| Midspan | 30000 | 3800 | 265.17 | 30000 | 0 | -265.17 |
| Right | 53445 | 3164 | 282.33 | 53445 | 10477 | -401.42 |
| 3 Left | 53445 | 2799 | 282.33 | 53445 | 10477 | -401.42 |
| Midspan | 30000 | 3319 | 265.17 | 30000 | 0 | -265.17 |
| Right | 53445 | 2799 | 282.33 | 53445 | 10477 | -401.42 |
| 4 Left | 53445 | 3164 | 282.33 | 53445 | 10477 | -401.42 |
| Midspan | 30000 | 3800 | 265.17 | 30000 | 0 | -265.17 |
| Right | 53445 | 3164 | 282.33 | 53445 | 7174 | -401.42 |
| 5 Left | 53445 | 0 | 282.33 | 53445 | 7174 | -401.42 |
| Midspan | 30000 | 0 | 265.17 | 30000 | 3641 | -265.17 |
| Right | 30000 | 0 | 265.17 | 30000 | 3641 | -265.17 |

NOTES: M+ve values are for positive moments (tension at bottom face).
M-ve values are for negative moments (tension at top face).

Frame Effective Section Properties

Units: Ie, Ie,avg (in⁴), Mmax (k-ft)

| Span Zone | Weight | Load Level | | | | | |
|-----------|--------|------------|-------|-----------|-------|-----------|-------|
| | | Dead | | Sustained | | Dead+Live | |
| | | Mmax | Ie | Mmax | Ie | Mmax | Ie |
| 1 Right | 1.000 | -1.69 | 53445 | -1.69 | 53445 | -2.32 | 53445 |
| Span Avg | ---- | ---- | 53445 | ---- | 53445 | ---- | 53445 |
| 2 Middle | 0.500 | 197.23 | 30000 | 197.23 | 30000 | 278.14 | 26502 |
| Right | 0.500 | -434.41 | 44379 | -434.41 | 44379 | -611.14 | 22653 |
| Span Avg | ---- | ---- | 37189 | ---- | 37189 | ---- | 24578 |
| 3 Left | 0.250 | -388.46 | 53445 | -388.46 | 53445 | -546.48 | 27506 |
| Middle | 0.500 | 107.56 | 30000 | 107.56 | 30000 | 152.03 | 30000 |
| Right | 0.250 | -388.46 | 53445 | -388.46 | 53445 | -546.48 | 27506 |
| Span Avg | ---- | ---- | 41723 | ---- | 41723 | ---- | 28753 |
| 4 Left | 0.500 | -434.41 | 44379 | -434.41 | 44379 | -611.14 | 22653 |
| Middle | 0.500 | 197.23 | 30000 | 197.23 | 30000 | 278.14 | 26502 |
| Span Avg | ---- | ---- | 37189 | ---- | 37189 | ---- | 24578 |
| 5 Left | 1.000 | -1.69 | 53445 | -1.69 | 53445 | -2.32 | 53445 |
| Span Avg | ---- | ---- | 53445 | ---- | 53445 | ---- | 53445 |

Strip Section Properties at Midspan

Units: Ig (in⁴)

| Span | Column Strip | | | Middle Strip | | |
|------|--------------|-------|-------|--------------|-------|-------|
| | Ig | LDF | Ratio | Ig | LDF | Ratio |
| 1 | 15000 | 0.800 | 1.600 | 15000 | 0.200 | 0.400 |
| 2 | 15000 | 0.738 | 1.475 | 15000 | 0.262 | 0.525 |
| 3 | 15000 | 0.675 | 1.350 | 15000 | 0.325 | 0.650 |
| 4 | 15000 | 0.738 | 1.475 | 15000 | 0.262 | 0.525 |
| 5 | 15000 | 0.800 | 1.600 | 15000 | 0.200 | 0.400 |

NOTES: Load distribution factor, LDL, averages moment distribution factors listed in [2] Design Results.
Ratio refers to proportion of strip to frame deflections under fix-end conditions.

Instantaneous Deflections

Extreme Instantaneous Frame Deflections and Corresponding Locations

Units: Def (in), Loc (ft)

| Span | Direction | Value | Live | | | Total | |
|------|-----------|-------|--------|-----------|-------------|--------|-----------|
| | | | Dead | Sustained | Unsustained | Total | Sustained |
| 1 | Down | Def | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- |
| | Up | Def | -0.012 | --- | -0.008 | -0.008 | -0.012 |
| | | Loc | 0.000 | --- | 0.000 | 0.000 | 0.000 |
| 2 | Down | Def | 0.163 | --- | 0.143 | 0.143 | 0.163 |
| | | Loc | 13.750 | --- | 14.000 | 14.000 | 13.750 |
| | Up | Def | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- |
| 3 | Down | Def | 0.060 | --- | 0.068 | 0.068 | 0.060 |
| | | Loc | 15.000 | --- | 15.000 | 15.000 | 15.000 |
| | Up | Def | -0.002 | --- | -0.001 | -0.001 | -0.002 |
| | | Loc | 1.324 | --- | 1.078 | 1.078 | 1.324 |
| 4 | Down | Def | 0.163 | --- | 0.143 | 0.143 | 0.163 |
| | | Loc | 16.250 | --- | 16.000 | 16.000 | 16.250 |
| | Up | Def | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- |
| 5 | Down | Def | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- |
| | Up | Def | -0.012 | --- | -0.008 | -0.008 | -0.012 |
| | | Loc | 0.833 | --- | 0.833 | 0.833 | 0.833 |

Extreme Instantaneous Column Strip Deflections and Corresponding Locations

Units: Def (in), Loc (ft)

| Span | Direction | Value | Live | | | Total | |
|------|-----------|-------|--------|-----------|-------------|--------|-----------|
| | | | Dead | Sustained | Unsustained | Total | Sustained |
| 1 | Down | Def | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- |
| | Up | Def | -0.012 | --- | -0.008 | -0.008 | -0.012 |
| | | Loc | 0.000 | --- | 0.000 | 0.000 | 0.000 |
| 2 | Down | Def | 0.207 | --- | 0.188 | 0.188 | 0.207 |
| | | Loc | 14.000 | --- | 14.250 | 14.250 | 14.000 |
| | Up | Def | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- |
| 3 | Down | Def | 0.089 | --- | 0.096 | 0.096 | 0.089 |
| | | Loc | 15.000 | --- | 15.000 | 15.000 | 15.000 |
| | Up | Def | -0.002 | --- | -0.001 | -0.001 | -0.002 |
| | | Loc | 1.078 | --- | 0.833 | 0.833 | 1.078 |
| 4 | Down | Def | 0.207 | --- | 0.188 | 0.188 | 0.207 |
| | | Loc | 16.000 | --- | 15.750 | 15.750 | 16.000 |
| | Up | Def | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- |
| 5 | Down | Def | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- |
| | Up | Def | -0.012 | --- | -0.008 | -0.008 | -0.012 |
| | | Loc | 0.833 | --- | 0.833 | 0.833 | 0.833 |

Extreme Instantaneous Middle Strip Deflections and Corresponding Locations

Units: Def (in), Loc (ft)

| Span | Direction | Value | Live | | | Total | |
|------|-----------|-------|--------|-----------|-------------|--------|-----------|
| | | | Dead | Sustained | Unsustained | Total | Sustained |
| 1 | Down | Def | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- |
| | Up | Def | -0.012 | --- | -0.008 | -0.008 | -0.012 |
| | | Loc | 0.000 | --- | 0.000 | 0.000 | 0.000 |
| 2 | Down | Def | 0.120 | --- | 0.098 | 0.098 | 0.120 |
| | | Loc | 13.000 | --- | 13.250 | 13.250 | 13.000 |
| | Up | Def | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- |
| 3 | Down | Def | 0.030 | --- | 0.040 | 0.040 | 0.030 |
| | | Loc | 15.000 | --- | 15.000 | 15.000 | 15.000 |
| | Up | Def | -0.003 | --- | -0.001 | -0.001 | -0.003 |
| | | Loc | 1.814 | --- | 1.324 | 1.324 | 1.814 |

spSlab v5.00 © StructurePoint
Licensed to: StructurePoint, License ID: 66184-1055152-4-2C6B6-2C6B6
C:\TSDA\TSDA-spSlab-Two-Way Slab with Drop Panels.slb

03-16-2017, 03:53:17 PM

Page 3

| | | | | | | | | |
|---|------|-----|--------|--------|--------|--------|--------|--------|
| 4 | Down | Def | 0.120 | --- | 0.098 | 0.098 | 0.120 | 0.218 |
| | | Loc | 17.000 | --- | 16.750 | 16.750 | 17.000 | 16.750 |
| | | Up | Def | --- | --- | --- | --- | --- |
| 5 | Down | Def | --- | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- | --- |
| | | Up | Def | -0.012 | --- | -0.008 | -0.008 | -0.012 |
| | | Loc | 0.833 | --- | 0.833 | 0.833 | 0.833 | 0.833 |

Long-term Deflections

Long-term Column Strip Deflection Factors

Time dependant factor for sustained loads = 2.000
Units: Astop, Asbot (in²), b, d (in), Rho' (%), Lambda (-)

| Span | Zone | M+ve | | | | M-ve | | | |
|------|---------|-------|-----|-----|-------------|-------|-----|-----|-------------|
| | | Astop | b | d | Rho' Lambda | Asbot | b | d | Rho' Lambda |
| 1 | Right | --- | --- | --- | 0.000 2.000 | --- | --- | --- | 0.000 2.000 |
| 2 | Midspan | --- | --- | --- | 0.000 2.000 | --- | --- | --- | 0.000 2.000 |
| 3 | Midspan | --- | --- | --- | 0.000 2.000 | --- | --- | --- | 0.000 2.000 |
| 4 | Midspan | --- | --- | --- | 0.000 2.000 | --- | --- | --- | 0.000 2.000 |
| 5 | Left | --- | --- | --- | 0.000 2.000 | --- | --- | --- | 0.000 2.000 |

NOTES: Deflection multiplier, Lambda, depends on moment sign at sustained load level and Rho' in given zone.
Rho' is assumed zero because Compression Reinforcement option is NOT selected in Solve Options.

Long-term Middle Strip Deflection Factors

Time dependant factor for sustained loads = 2.000
Units: Astop, Asbot (in²), b, d (in), Rho' (%), Lambda (-)

| Span | Zone | M+ve | | | | M-ve | | | |
|------|---------|-------|-----|-----|-------------|-------|-----|-----|-------------|
| | | Astop | b | d | Rho' Lambda | Asbot | b | d | Rho' Lambda |
| 1 | Right | --- | --- | --- | 0.000 2.000 | --- | --- | --- | 0.000 2.000 |
| 2 | Midspan | --- | --- | --- | 0.000 2.000 | --- | --- | --- | 0.000 2.000 |
| 3 | Midspan | --- | --- | --- | 0.000 2.000 | --- | --- | --- | 0.000 2.000 |
| 4 | Midspan | --- | --- | --- | 0.000 2.000 | --- | --- | --- | 0.000 2.000 |
| 5 | Left | --- | --- | --- | 0.000 2.000 | --- | --- | --- | 0.000 2.000 |

NOTES: Deflection multiplier, Lambda, depends on moment sign at sustained load level and Rho' in given zone.
Rho' is assumed zero because Compression Reinforcement option is NOT selected in Solve Options.

Extreme Long-term Column Strip Deflections and Corresponding Locations

Units: D (in), x (ft)

| Span | Direction | Value | cs | cs+lu | cs+l | Total |
|------|-----------|-------|--------|--------|--------|--------|
| 1 | Down | Def | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- |
| | | Up | Def | -0.025 | -0.033 | -0.033 |
| | | Loc | 0.000 | 0.000 | 0.000 | 0.000 |
| 2 | Down | Def | 0.414 | 0.601 | 0.601 | 0.808 |
| | | Loc | 14.000 | 14.000 | 14.000 | 14.000 |
| | | Up | Def | --- | --- | --- |
| | | Loc | --- | --- | --- | --- |
| 3 | Down | Def | 0.178 | 0.274 | 0.274 | 0.363 |
| | | Loc | 15.000 | 15.000 | 15.000 | 15.000 |
| | | Up | Def | -0.003 | -0.004 | -0.004 |
| | | Loc | 1.078 | 1.078 | 1.078 | 1.078 |
| 4 | Down | Def | 0.414 | 0.601 | 0.601 | 0.808 |
| | | Loc | 16.000 | 16.000 | 16.000 | 16.000 |
| | | Up | Def | --- | --- | --- |
| | | Loc | --- | --- | --- | --- |
| 5 | Down | Def | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- |
| | | Up | Def | -0.025 | -0.033 | -0.033 |
| | | Loc | 0.833 | 0.833 | 0.833 | 0.833 |

NOTES: Incremental deflections due to creep and shrinkage (cs) based on sustained load level values.
Incremental deflections after partitions are installed can be estimated by deflections due to:
- creep and shrinkage plus unsustained live load (cs+lu), if live load applied before partitions,
- creep and shrinkage plus live load (cs+l), if live load applied after partitions.
Total deflections consist of dead, live, and creep and shrinkage deflections.

Extreme Long-term Middle Strip Deflections and Corresponding Locations

Units: D (in), x (ft)

| Span | Direction | Value | cs | cs+lu | cs+l | Total |
|------|-----------|-------|--------|--------|--------|--------|
| 1 | Down | Def | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- |
| | | Up | Def | -0.025 | -0.033 | -0.033 |
| | | Loc | 0.000 | 0.000 | 0.000 | 0.000 |
| 2 | Down | Def | 0.241 | 0.339 | 0.339 | 0.459 |
| | | Loc | 13.000 | 13.000 | 13.000 | 13.000 |
| | | Up | Def | --- | --- | --- |

spSlab v5.00 © StructurePoint
Licensed to: StructurePoint, License ID: 66184-10551S2-4-2C6B6-2C6B6
C:\TSDA\TSDA-spSlab-Two-Way Slab with Drop Panels.slb

03-16-2017, 03:53:17 PM

Page 4

| | | | | | | |
|---|------|-----|--------|--------|--------|--------|
| | | Loc | --- | --- | --- | --- |
| 3 | Down | Def | 0.060 | 0.101 | 0.101 | 0.131 |
| | | Loc | 15.000 | 15.000 | 15.000 | 15.000 |
| | Up | Def | -0.006 | -0.007 | -0.007 | -0.010 |
| | | Loc | 1.814 | 1.814 | 1.814 | 1.814 |
| 4 | Down | Def | 0.241 | 0.339 | 0.339 | 0.459 |
| | | Loc | 17.000 | 17.000 | 17.000 | 17.000 |
| | Up | Def | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- |
| 5 | Down | Def | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- |
| | Up | Def | -0.025 | -0.033 | -0.033 | -0.045 |
| | | Loc | 0.833 | 0.833 | 0.833 | 0.833 |

NOTES: Incremental deflections due to creep and shrinkage (cs) based on sustained load level values.
Incremental deflections after partitions are installed can be estimated by deflections due to:
- creep and shrinkage plus unsustained live load (cs+lu), if live load applied before partitions,
- creep and shrinkage plus live load (cs+l), if live load applied after partitions.
Total deflections consist of dead, live, and creep and shrinkage deflections.

7. Summary and Comparison of Design Results

| Table 9 - Comparison of Moments obtained from Hand (EFM) and spSlab Solution (ft-kips) | | | |
|---|--------------------|-------------------|---------------|
| | | Hand (EFM) | spSlab |
| Exterior Span | | | |
| Column Strip | Exterior Negative* | 246.5 | 244.8 |
| | Positive | 209.8 | 219.7 |
| | Interior Negative* | 521.9 | 517.6 |
| Middle Strip | Exterior Negative* | 0.0 | 0.0 |
| | Positive | 139.8 | 146.5 |
| | Interior Negative* | 174.0 | 172.5 |
| Interior Span | | | |
| Column Strip | Interior Negative* | 467.6 | 463.6 |
| | Positive | 118.4 | 120.1 |
| Middle Strip | Interior Negative* | 155.9 | 154.5 |
| | Positive | 78.9 | 80.1 |

* negative moments are taken at the faces of supports

| Table 10 - Comparison of Reinforcement Results | | | | | | | |
|---|-------------------|---|---------------|--|---------------|-------------------------------------|---------------|
| Span Location | | Reinforcement Provided for Flexure | | Additional Reinforcement Provided for Unbalanced Moment Transfer* | | Total Reinforcement Provided | |
| | | Hand | spSlab | Hand | spSlab | Hand | spSlab |
| Exterior Span | | | | | | | |
| Column Strip | Exterior Negative | 10-#6 | 10-#6 | 5-#6 | 5-#6 | 15-#6 | 15-#6 |
| | Positive | 13-#6 | 13-#6 | n/a | n/a | 13-#6 | 13-#6 |
| | Interior Negative | 22-#6 | 21-#6 | --- | --- | 22-#6 | 21-#6 |
| Middle Strip | Exterior Negative | 10-#6 | 10-#6 | n/a | n/a | 10-#6 | 10-#6 |
| | Positive | 10-#6 | 10-#6 | n/a | n/a | 10-#6 | 10-#6 |
| | Interior Negative | 11-#6 | 11-#6 | n/a | n/a | 11-#6 | 11-#6 |
| Interior Span | | | | | | | |
| Column Strip | Positive | 10-#6 | 10-#6 | n/a | n/a | 10-#6 | 10-#6 |
| Middle Strip | Positive | 10-#6 | 10-#6 | n/a | n/a | 10-#6 | 10-#6 |

| Span | V_u @ d, kips | | V_u @ drop panel, kips | | ϕV_c @ d, kips | | ϕV_c @ drop panel, kips | |
|----------|-----------------|--------|--------------------------|--------|----------------------|--------|-------------------------------|--------|
| | Hand | spSlab | Hand | spSlab | Hand | spSlab | Hand | spSlab |
| Exterior | 123.7 | 126.7 | 96.9 | 96.7 | 392.91 | 392.97 | 339.10 | 338.88 |
| Interior | 107.8 | 110.9 | 81.0 | 81.0 | 392.91 | 392.97 | 339.10 | 338.88 |

* x_u calculated from the centerline of the left column for each span

| Support | b_1 , in. | | b_2 , in. | | b_o , in. | | V_u , kips | | c_{AB} , in. | |
|----------|-------------|--------|-------------|--------|-------------|--------|--------------|--------|----------------|--------|
| | Hand | spSlab | Hand | spSlab | Hand | spSlab | Hand | spSlab | Hand | spSlab |
| Exterior | 26.56 | 26.56 | 33.13 | 33.13 | 86.26 | 86.25 | 103.6 | 114.6 | 8.18 | 8.18 |
| Interior | 33.13 | 33.13 | 33.13 | 33.13 | 132.52 | 132.50 | 256.4 | 263.0 | 16.57 | 16.56 |
| Corner | 26.56 | 26.56 | 26.56 | 26.56 | 53.13 | 53.12 | 60.3 | 60.6 | 6.64 | 6.64 |

| Support | J_c , in. ⁴ | | γ_v | | M_{unb} , ft-kips | | v_u , psi | | ϕv_c , psi | |
|----------|--------------------------|---------|------------|--------|---------------------|--------|-------------|--------|------------------|--------|
| | Hand | spSlab | Hand | spSlab | Hand | spSlab | Hand | spSlab | Hand | spSlab |
| Exterior | 98,315 | 98,239 | 0.374 | 0.374 | 259 | 249.5 | 188.3 | 194.4 | 212.1 | 212.1 |
| Interior | 330,800 | 330,520 | 0.400 | 0.400 | 85.70 | 85.07 | 167.9 | 171.7 | 212.1 | 212.1 |
| Corner | 56,292 | 56,249 | 0.400 | 0.400 | 137.65 | 137.40 | 164.4 | 164.8 | 212.1 | 212.1 |

| Support | b_1 , in. | | b_2 , in. | | b_o , in. | | V_u , kips | | c_{AB} , in. | |
|----------|-------------|--------|-------------|--------|-------------|--------|--------------|--------|----------------|--------|
| | Hand | spSlab | Hand | spSlab | Hand | spSlab | Hand | spSlab | Hand | spSlab |
| Exterior | 74.44 | 74.44 | 128.88 | 128.88 | 277.76 | 277.75 | 87.65 | 98.24 | 19.95 | 19.95 |
| Interior | 128.88 | 128.88 | 128.88 | 128.88 | 515.52 | 515.5 | 225.5 | 233.91 | 64.44 | 64.44 |
| Corner | 74.44 | 74.44 | 74.44 | 74.44 | 148.88 | 148.87 | 51.54 | 51.53 | 18.61 | 18.61 |

| Support | J_c , in. ⁴ | | γ_v | | M_{unb} , ft-kips | | v_u , psi | | ϕv_c , psi | |
|----------|--------------------------|------------|------------|--------|---------------------|--------|-------------|--------|------------------|--------|
| | Hand | spSlab | Hand | spSlab | Hand | spSlab | Hand | spSlab | Hand | spSlab |
| Exterior | 1,468,983 | 1,468,000 | N.A. | N.A. | N.A. | N.A. | 35.5 | 39.9 | 156.9 | 156.9 |
| Interior | 12,688,007 | 12,679,000 | N.A. | N.A. | N.A. | N.A. | 49.7 | 51.1 | 142.6 | 142.6 |
| Corner | 767,460 | 766,930 | N.A. | N.A. | N.A. | N.A. | 38.98 | 39.00 | 169.3 | 169.3 |

Note: Shear stresses from spSlab are higher than hand calculations since it considers the load effects beyond the column centerline known in the model as right/left cantilevers. This small increase is often neglected in simplified hand calculations like the one used here.

| Table 14 - Comparison of Immediate Deflection Results (in.) | | | | | | | | |
|---|-------|--------|---------------------|--------|----------------------|--------|-------|--------|
| Column Strip | | | | | | | | |
| Span | D | | D+LL _{sus} | | D+LL _{full} | | LL | |
| | Hand | spSlab | Hand | spSlab | Hand | spSlab | Hand | spSlab |
| Exterior | 0.219 | 0.207 | 0.219 | 0.207 | 0.432 | 0.395 | 0.213 | 0.188 |
| Interior | 0.093 | 0.089 | 0.093 | 0.089 | 0.192 | 0.185 | 0.098 | 0.096 |
| Middle Strip | | | | | | | | |
| Span | D | | D+LL _{sus} | | D+LL _{full} | | LL | |
| | Hand | spSlab | Hand | spSlab | Hand | spSlab | Hand | spSlab |
| Exterior | 0.125 | 0.120 | 0.125 | 0.120 | 0.253 | 0.218 | 0.128 | 0.098 |
| Interior | 0.031 | 0.030 | 0.031 | 0.030 | 0.064 | 0.071 | 0.033 | 0.040 |

| Table 15 - Comparison of Time-Dependent Deflection Results | | | | | | |
|--|-------------|--------|---------------------------|--------|------------------------------|--------|
| Column Strip | | | | | | |
| Span | λ_A | | $\Delta_{cs}, \text{in.}$ | | $\Delta_{total}, \text{in.}$ | |
| | Hand | spSlab | Hand | spSlab | Hand | spSlab |
| Exterior | 2.0 | 2.0 | 0.439 | 0.414 | 0.871 | 0.808 |
| Interior | 2.0 | 2.0 | 0.187 | 0.178 | 0.378 | 0.363 |
| Middle Strip | | | | | | |
| Span | λ_A | | $\Delta_{cs}, \text{in.}$ | | $\Delta_{total}, \text{in.}$ | |
| | Hand | spSlab | Hand | spSlab | Hand | spSlab |
| Exterior | 2.0 | 2.0 | 0.250 | 0.241 | 0.503 | 0.459 |
| Interior | 2.0 | 2.0 | 0.062 | 0.060 | 0.127 | 0.131 |

In all of the hand calculations illustrated above, the results are in close or exact agreement with the automated analysis and design results obtained from the spSlab model. Excerpts of spSlab graphical and text output are given below for illustration.

8. Conclusions & Observations

8.1. One-Way Shear Distribution to Slab Strips

In one-way shear checks above, shear is distributed uniformly along the width of the design strip (30 ft.). [StructurePoint](#) finds it necessary sometimes to allocate the one-way shears with the same proportion moments are distributed to column and middle strips.

[spSlab](#) allows the one-way shear check using two approaches: 1) calculating the one-way shear capacity using the average slab thickness and comparing it with the total factored one-shear load as shown in the hand calculations above; 2) distributing the factored one-way shear forces to the column and middle strips and comparing it with the shear capacity of each strip as illustrated in the following figures. An engineering judgment is needed to decide which approach to be used.

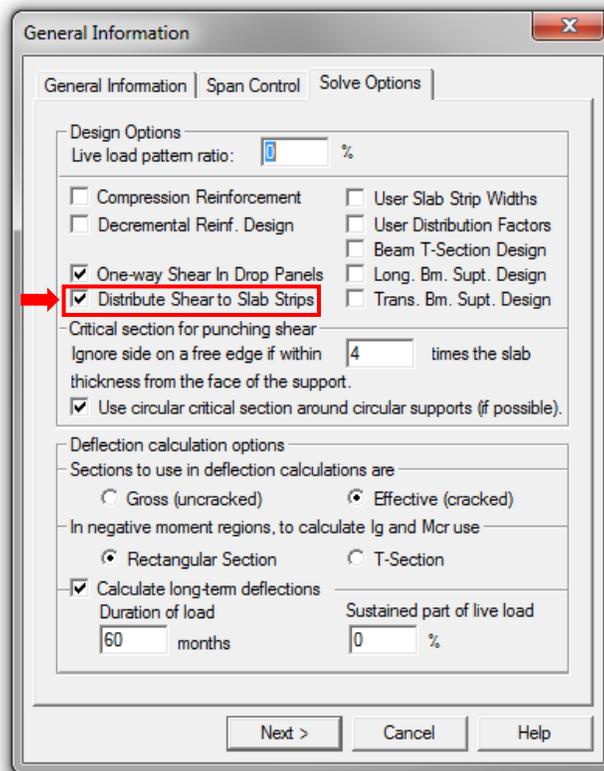


Figure 23a – Distributing Shear to Column and Middle Strips ([spSlab](#) Input)

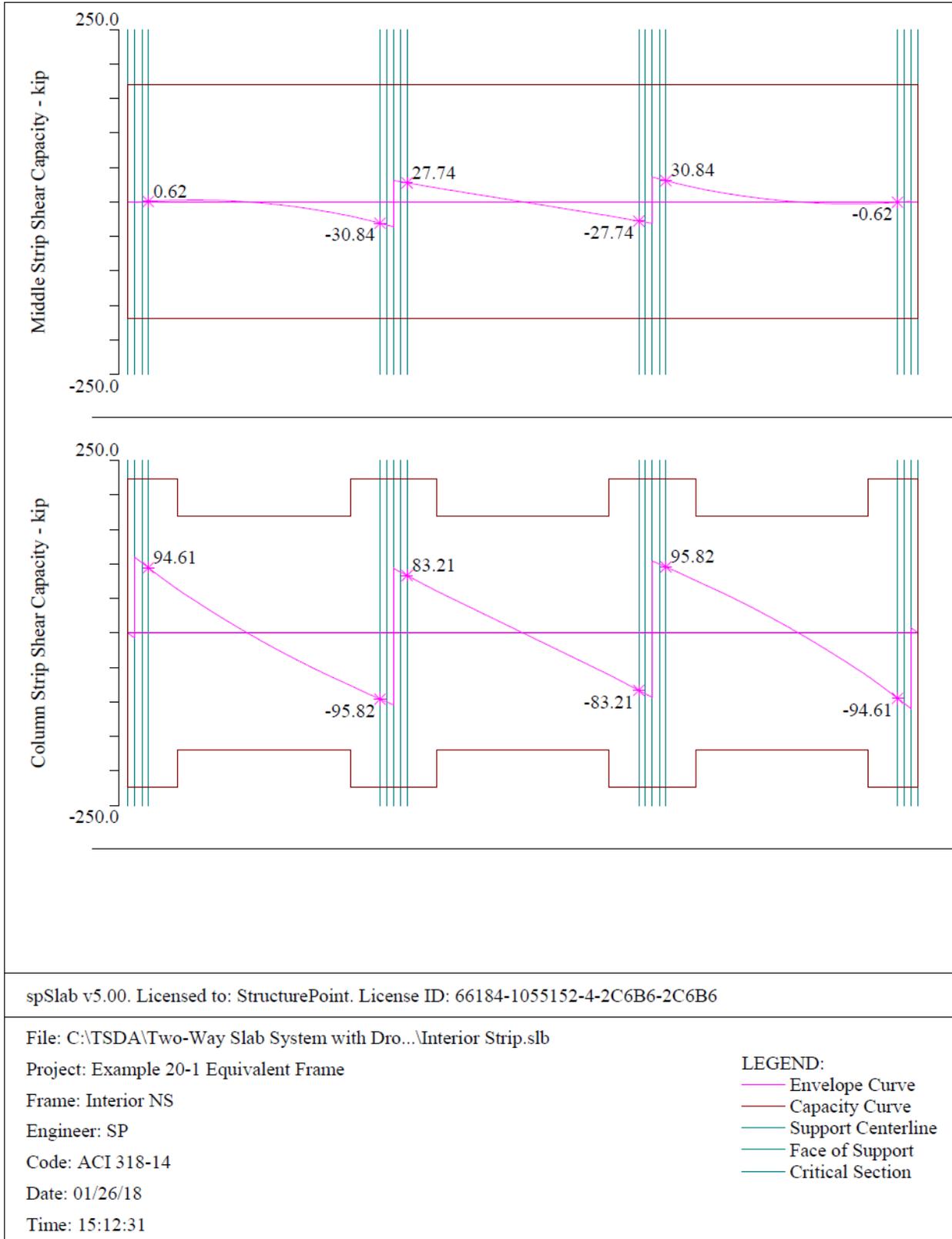


Figure 23b – Distributed Column and Middle Strip Shear Force Diagram (spSlab Output)

spSlab v5.00 © StructurePoint
Licensed to: StructurePoint, License ID: 66184-1055152-4-2C6B6-2C6B6
C:\TSDA\Two-Way Slab System with Drop Panels\Interior Strip.slb

01-24-2018, 08:59:48 AM

Page 1

Slab Shear Capacity

```

=====
Units: b, d (in), Xu (ft), PhiVc, Vu(kip)
Span Strip      b      d      Vratio      PhiVc      Vu      Xu
-----
1 Column 180.00  8.88  1.000      169.44      7.28     -0.00
      180.00 11.71  1.000      223.53      7.28     -0.00
  Middle 180.00  8.88  0.000      169.44      0.00      0.00
      180.00  8.88  0.000      169.44      0.00      0.00
2 Column 180.00 11.71  0.993      223.53      94.61     1.57
      180.00  8.88  0.787      169.44      76.09     25.00
      180.00 11.71  0.757      223.53      95.82     28.43
  Middle 180.00  8.88  0.037      169.44      2.40      5.00
      180.00  8.88  0.213      169.44      20.62     25.00
      180.00  8.88  0.243      169.44      30.84     28.43
3 Column 180.00 11.71  0.750      223.53      83.21     1.57
      180.00  8.88  0.750      169.44      60.75     25.00
      180.00 11.71  0.750      223.53      83.21     28.43
  Middle 180.00  8.88  0.250      169.44      27.74     1.57
      180.00  8.88  0.250      169.44      20.25     25.00
      180.00  8.88  0.250      169.44      27.74     28.43
4 Column 180.00 11.71  0.757      223.53      95.82     1.57
      180.00  8.88  0.787      169.44      76.09     5.00
      180.00 11.71  0.993      223.53      94.61     28.43
  Middle 180.00  8.88  0.243      169.44      30.84     1.57
      180.00  8.88  0.213      169.44      20.62     5.00
      180.00  8.88  0.037      169.44      2.40     25.00
5 Column 180.00 11.71  1.000      223.53      0.00      0.83
      180.00  8.88  1.000      169.44      0.00      0.83
  Middle 180.00  8.88  0.000      169.44      0.00      0.00
      180.00  8.88  0.000      169.44      0.00      0.00

```

Figure 23c – Tabulated Shear Force & Capacity at Critical Sections (spSlab Output)

8.2. Two-Way Concrete Slab Analysis Methods

A slab system can be analyzed and designed by any procedure satisfying equilibrium and geometric compatibility. Three established methods are widely used. The requirements for two of them are described in detail in ACI 318-14 Chapter 8 (8.2.1).

Direct Design Method (DDM) is an approximate method and is applicable to two-way slab concrete floor systems that meet the stringent requirements of ACI 318-14 (8.10.2). In many projects, however, these requirements limit the usability of the Direct Design Method significantly.

The Equivalent Frame Method (EFM) does not have the limitations of Direct Design Method. It requires more accurate analysis methods that, depending on the size and geometry can prove to be long, tedious, and time-consuming.

StructurePoint's [spSlab](#) software program solution utilizes the Equivalent Frame Method to automate the process providing considerable time-savings in the analysis and design of two-way slab systems as compared to hand solutions using DDM or EFM.

Finite Element Method (FEM) is another method for analyzing reinforced concrete slabs, particularly useful for irregular slab systems with variable thicknesses, openings, and other features not permissible in DDM or EFM. Many reputable commercial FEM analysis software packages are available on the market today such as [spMats](#). Using FEM requires critical understanding of the relationship between the actual behavior of the structure and the numerical simulation since this method is an approximate numerical method. The method is based on several assumptions and the operator has a great deal of decisions to make while setting up the model and applying loads and boundary conditions. The results obtained from FEM models should be verified to confirm their suitability for design and detailing of concrete structures.

The following table shows a general comparison between the DDM, EFM and FEM. This table covers general limitations, drawbacks, advantages, and cost-time efficiency of each method where it helps the engineer in deciding which method to use based on the project complexity, schedule, and budget.

| Applicable ACI 318-14 Provision | Limitations/Applicability | Concrete Slab Analysis Method | | |
|--|--|---|---|--|
| | | DDM (Hand) | EFM (Hand//spSlab) | FEM (spMats) |
| 8.10.2.1 | Minimum of three continuous spans in each direction | <input checked="" type="checkbox"/> | | |
| 8.10.2.2 | Successive span lengths measured center-to-center of supports in each direction shall not differ by more than one-third the longer span | <input checked="" type="checkbox"/> | | |
| 8.10.2.3 | Panels shall be rectangular, with ratio of longer to shorter panel dimensions, measured center-to-center supports, not exceed 2. | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> | |
| 8.10.2.4 | Column offset shall not exceed 10% of the span in direction of offset from either axis between centerlines of successive columns | <input checked="" type="checkbox"/> | | |
| 8.10.2.5 | All loads shall be due to gravity only | <input checked="" type="checkbox"/> | | |
| 8.10.2.5 | All loads shall be uniformly distributed over an entire panel (q_u) | <input checked="" type="checkbox"/> | | |
| 8.10.2.6 | Unfactored live load shall not exceed two times the unfactored dead load | <input checked="" type="checkbox"/> | | |
| 8.10.2.7 | For a panel with beams between supports on all sides, slab-to-beam stiffness ratio shall be satisfied for beams in the two perpendicular directions. | <input checked="" type="checkbox"/> | | |
| 8.7.4.2 | Structural integrity steel detailing | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> |
| 8.5.4 | Openings in slab systems | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> |
| 8.2.2 | Concentrated loads | Not permitted | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> |
| 8.11.1.2 | Live load arrangement (Load Patterning) | Not required | Required | Engineering judgment required based on modeling technique |
| R8.10.4.5 ^e | Reinforcement for unbalanced slab moment transfer to column (M_{sc}) | Moments @ support face | Moments @ support centerline | Engineering judgment required based on modeling technique |
| | Irregularities (i.e. variable thickness, non-prismatic, partial bands, mixed systems, support arrangement, etc.) | Not permitted | Engineering judgment required | Engineering judgment required |
| Complexity | | Low | Average | Complex to very complex |
| Design time/costs | | Fast | Limited | Unpredictable/Costly |
| Design Economy | | Conservative (see detailed comparison with spSlab output) | Somewhat conservative | Unknown - highly dependent on modeling assumptions: 1. Linear vs. non-linear 2. Isotropic vs non-isotropic 3. Plate element choice 4. Mesh size and aspect ratio 5. Design & detailing features |
| General (Drawbacks) | | Very limited applications | Limited geometry | Limited guidance non-standard application (user dependent). Required significant engineering judgment |
| General (Advantages) | | Very limited analysis is required | Detailed analysis is required or via software (e.g. spSlab) | Unlimited applicability to handle complex situations permissible by the features of the software used (e.g. spMats) |

^e The unbalanced slab moment transferred to the column M_{sc} (M_{unb}) is the difference in slab moment on either side of a column at a specific joint. In DDM only moments at the face of the support are calculated and are also used to obtain M_{sc} (M_{unb}). In EFM where a frame analysis is used, moments at the column center line are used to obtain M_{sc} (M_{unb}).