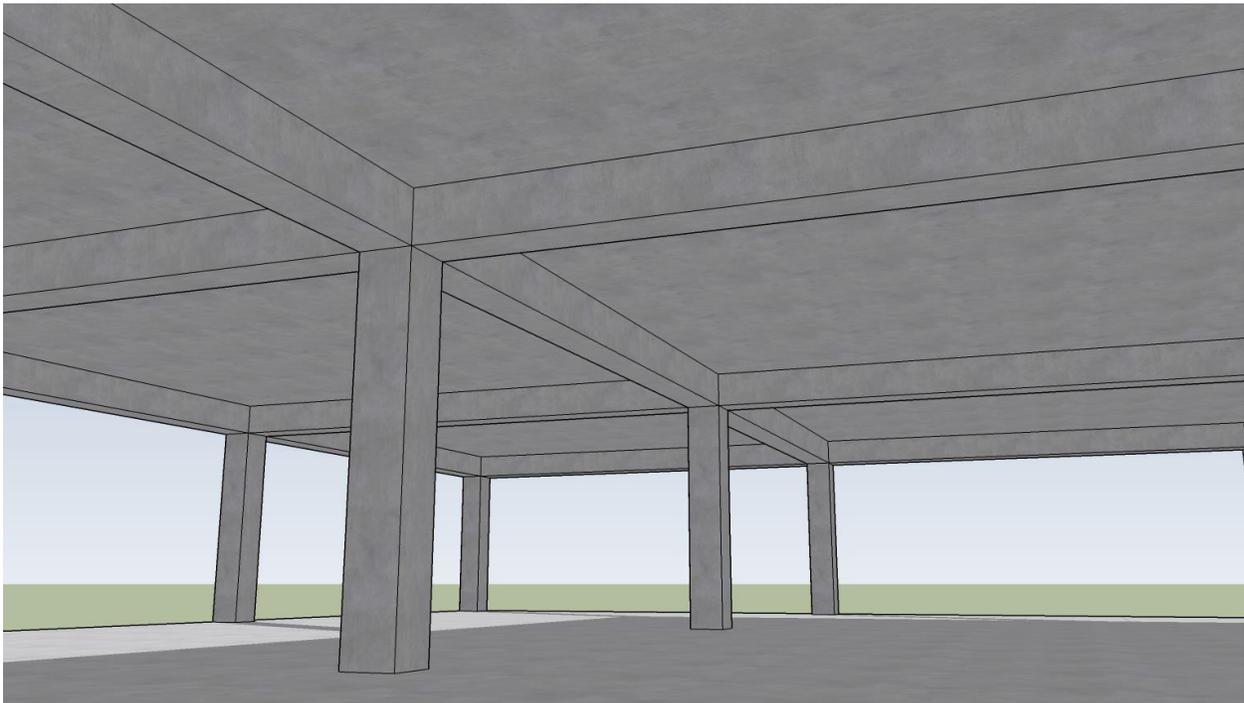
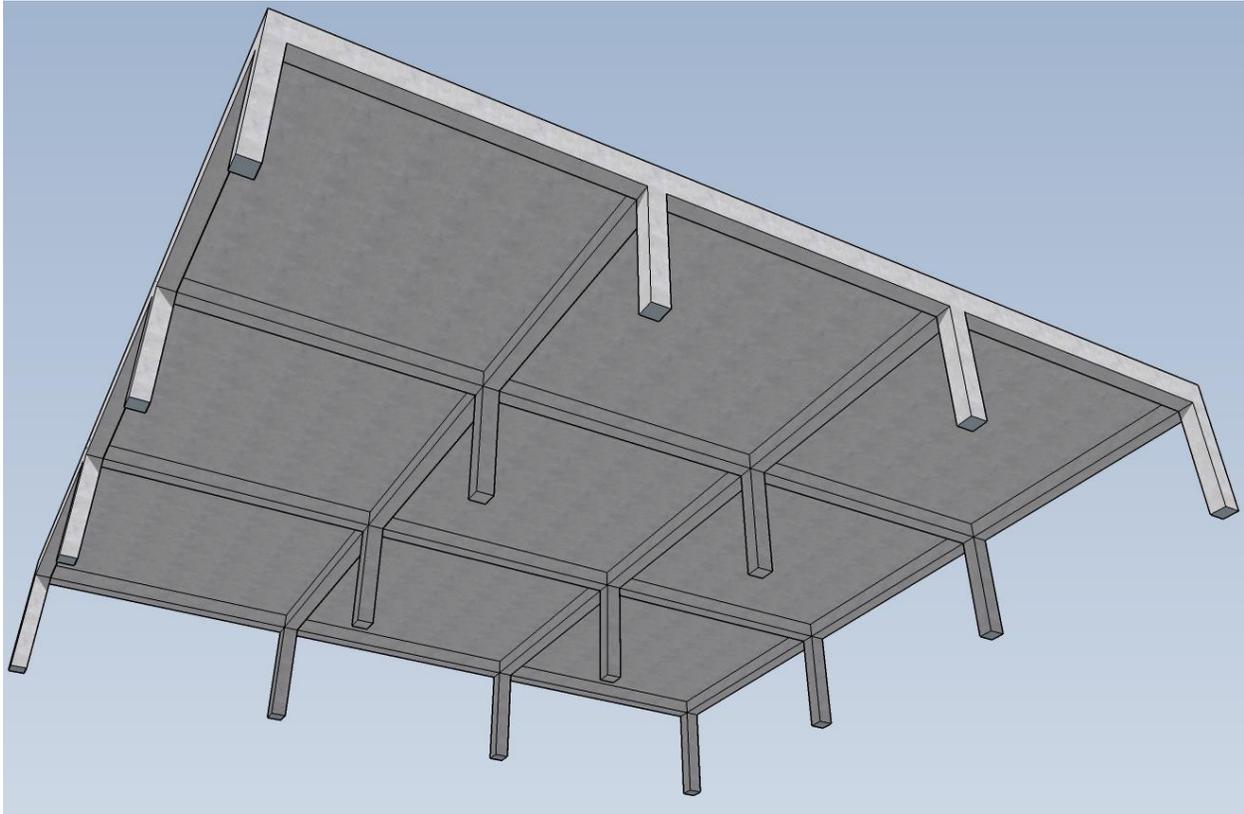


Two-Way Concrete Floor Slab with Beams Design and Detailing



Two-Way Concrete Floor Slab with Beams Design and Detailing

Design the slab system shown in Figure 1 for an intermediate floor where the story height = 12 ft, column cross-sectional dimensions = 18 in. x 18 in., edge beam dimensions = 14 in. x 27 in., interior beam dimensions = 14 in. x 20 in., and unfactored live load = 100 psf. The lateral loads are resisted by shear walls. Normal weight concrete with ultimate strength ($f_c' = 4000$ psi) is used for all members, respectively. And reinforcement with $F_y = 60,000$ psi is used. Use the Equivalent Frame Method (EFM) and compare the results with [spSlab](#) model results.

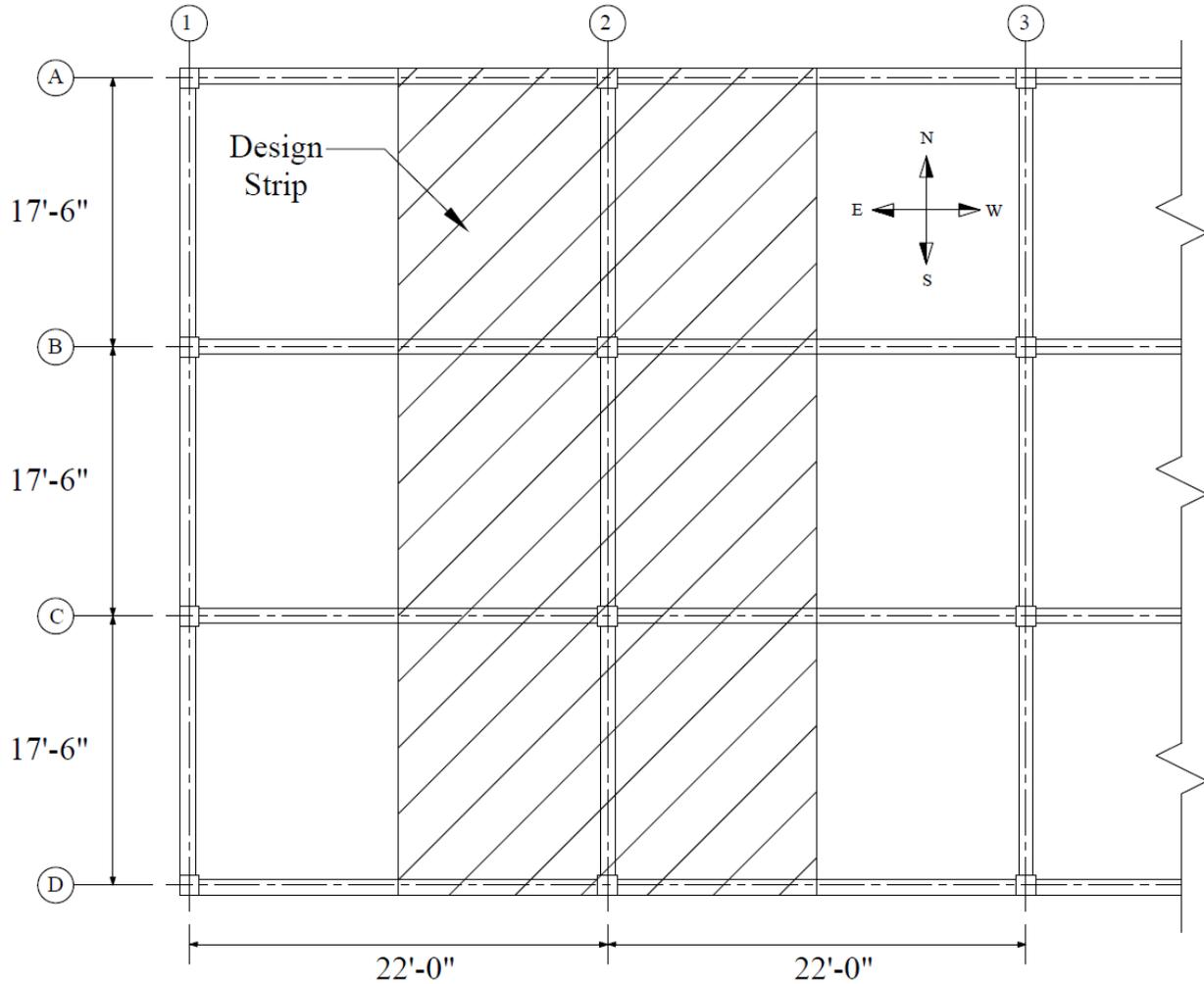


Figure 1 – Two-Way Slab with Beams Spanning between all Supports

Contents

| | |
|--|----|
| 1. Preliminary Slab Thickness Sizing..... | 1 |
| 2. Two-Way Slab Analysis and Design – Using Equivalent Frame Method (EFM)..... | 4 |
| 2.1. Equivalent frame method limitations | 5 |
| 2.2. Frame members of equivalent frame..... | 5 |
| 2.3. Equivalent frame analysis | 11 |
| 2.4. Design moments..... | 14 |
| 2.5. Distribution of design moments | 15 |
| 2.6. Flexural reinforcement requirements | 17 |
| 2.7. Column design moments..... | 24 |
| 3. Design of Interior, Edge, and Corner Columns | 25 |
| 4. Two-Way Slab Shear Strength..... | 25 |
| 4.1. One-Way (Beam action) Shear Strength..... | 25 |
| 4.2. Two-Way (Punching) Shear Strength | 26 |
| 5. Two-Way Slab Deflection Control (Serviceability Requirements)..... | 29 |
| 5.1. Immediate (Instantaneous) Deflections..... | 29 |
| 5.2. Time-Dependent (Long-Term) Deflections (Δ_{lt})..... | 40 |
| 6. spSlab Software Program Model Solution | 41 |
| 7. Summary and Comparison of Design Results..... | 63 |
| 8. Conclusions & Observations | 66 |

Code

Building Code Requirements for Structural Concrete (ACI 318-14) and Commentary (ACI 318R-14)

Minimum Design Loads for Buildings and Other Structures (ASCE/SEI 7-10)

International Code Council, 2012 International Building Code, Washington, D.C., 2012

References

Notes on ACI 318-11 Building Code Requirements for Structural Concrete, Twelfth Edition, 2013 Portland Cement Association.

Concrete Floor Systems (Guide to Estimating and Economizing), Second Edition, 2002 David A. Fanella

Simplified Design of Reinforced Concrete Buildings, Fourth Edition, 2011 Mahmoud E. Kamara and Lawrence C. Novak

Design Data

Floor-to-Floor Height = 12 ft (provided by architectural drawings)

Columns = 18 x 18 in.

Interior beams = 14 x 20 in.

Edge beams = 14 x 27 in.

$w_c = 150$ pcf

$f_c' = 4,000$ psi

$f_y = 60,000$ psi

Live load, $L_o = 100$ psf (Office building)

ASCE/SEI 7-10 (Table 4-1)

Solution

1. Preliminary Slab Thickness Sizing

Control of deflections.

ACI 318-14 (8.3.1.2)

In lieu of detailed calculation for deflections, ACI 318 Code gives minimum thickness for two-way slab with beams spanning between supports on all sides in **Table 8.3.1.2**.

Beam-to-slab flexural stiffness (relative stiffness) ratio (α_f) is computed as follows:

$$\alpha_f = \frac{E_{cb} I_b}{E_{cs} I_s} = \frac{I_b}{I_s}$$

ACI 318-14 (8.10.2.7b)

The moment of inertia for the effective beam and slab sections can be calculated as follows:

$$I_s = \frac{l_z h^3}{12} \quad \text{and} \quad I_b = \left(\frac{b a^3}{12} \right) \times f$$

Then,

$$\alpha_f = \left(\frac{b}{l_2}\right) \left(\frac{a}{h}\right)^3 f$$

For Edge Beams:

The effective beam and slab sections for the computation of stiffness ratio for edge beam is shown in Figure 2.

For North-South Edge Beam:

$$l_2 = \frac{22 \times 12}{2} + \frac{18}{2} = 141 \text{ in.}$$

$$\frac{a}{h} = \frac{27}{6} = 4.5$$

$$\frac{b}{h} = \frac{14}{6} = 2.33$$

$f = 1.47$ using Figure 3.

$$\alpha_f = \left(\frac{14}{141}\right) \left(\frac{27}{6}\right)^3 (1.47) = 13.30$$

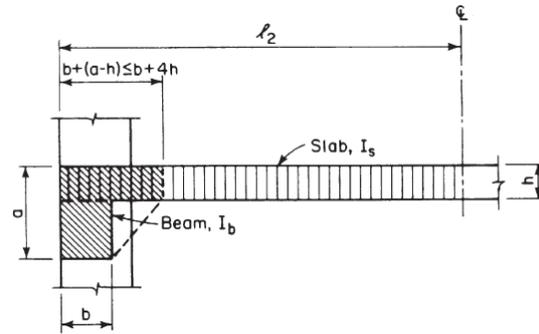


Figure 2 – Effective Beam and Slab Sections (Edge Beam)

For East-West Edge Beam:

$$l_2 = \frac{17.5 \times 12}{2} + \frac{18}{2} = 114 \text{ in.}$$

$$\frac{a}{h} = \frac{27}{6} = 4.5$$

$$\frac{b}{h} = \frac{14}{6} = 2.33$$

$f = 1.47$ using Figure 3.

$$\alpha_f = \left(\frac{14}{114}\right) \left(\frac{27}{6}\right)^3 (1.47) = 16.45$$

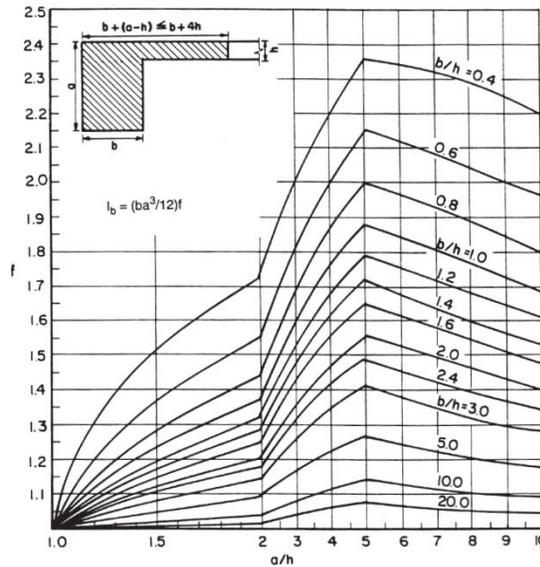


Figure 3 – Beam Stiffness (Edge Beam)

For interior Beams:

The effective beam and slab sections for the computation of stiffness ratio for interior beam is shown in Figure 4.

For North-South Interior Beam:

$$l_2 = 22 \times 12 = 264 \text{ in.}$$

$$\frac{a}{h} = \frac{20}{6} = 3.33$$

$$\frac{b}{h} = \frac{14}{6} = 2.33$$

$f = 1.61$ using Figure 5.

$$\alpha_f = \left(\frac{14}{264} \right) \left(\frac{20}{6} \right)^3 (1.61) = 3.16$$

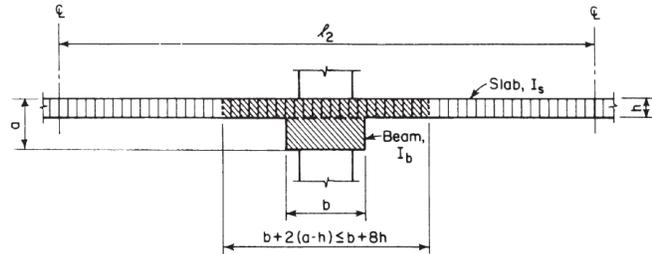


Figure 4 – Effective Beam and Slab Sections (Interior Beam)

For East-West Interior Beam:

$$l_2 = 17.5 \times 12 = 210 \text{ in.}$$

$$\frac{a}{h} = \frac{20}{6} = 3.33$$

$$\frac{b}{h} = \frac{14}{6} = 2.33$$

$f = 1.61$ using Figure 5.

$$\alpha_f = \left(\frac{14}{210} \right) \left(\frac{20}{6} \right)^3 (1.61) = 3.98$$

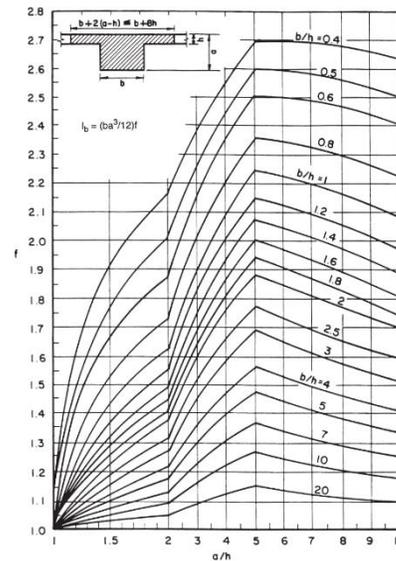


Figure 5 – Beam Stiffness (Interior Beam)

Since $\alpha_f > 2.0$ for all beams, the minimum slab thickness is given by:

$$h_{\min} = \text{greater of } \left\{ \frac{l_n \left(0.8 + \frac{f_y}{200,000} \right)}{36 + 9\beta}, \frac{l_n}{5.0} \right\}$$

ACI 318-14 (8.3.1.2)

Where:

l_n = clear span in the long direction measured face to face of columns = 20.5 ft = 246 in.

$$\beta = \frac{\text{clear span in the long direction}}{\text{clear span in the short direction}} = \frac{22 - 18/12}{17.2 - 18/12} = 1.28$$

$$h_{\min} = \text{greater of } \left\{ \frac{246 \left(0.8 + \frac{60,000}{200,000} \right)}{36 + 9(1.28)} = 5.7 \right\} = 5.7 \text{ in.}$$

Use 6 in. slab thickness.

2. Two-Way Slab Analysis and Design – Using Equivalent Frame Method (EFM)

ACI 318 states that a slab system shall be designed by any procedure satisfying equilibrium and geometric compatibility, provided that strength and serviceability criteria are satisfied. Distinction of two-systems from one-way systems is given by ACI 318-14 (R8.10.2.3 & R8.3.1.2).

ACI 318 permits the use of Direct Design Method (DDM) and Equivalent Frame Method (EFM) for the gravity load analysis of orthogonal frames and is applicable to flat plates, flat slabs, and slabs with beams. The following sections outline the solution per EFM and [spSlab](#) software. The solution per DDM can be found in the “Two-Way Plate Concrete Floor System Design” example.

EFM is the most comprehensive and detailed procedure provided by the ACI 318 for the analysis and design of two-way slab systems where the structure is modeled by a series of equivalent frames (interior and exterior) on column lines taken longitudinally and transversely through the building.

The equivalent frame consists of three parts:

- 1) Horizontal slab-beam strip, including any beams spanning in the direction of the frame. Different values of moment of inertia along the axis of slab-beams should be taken into account where the gross moment of inertia at any cross section outside of joints or column capitals shall be taken, and the moment of inertia of the slab-beam at the face of the column, bracket or capital divide by the quantity $(1-c_2/l_2)^2$ shall be assumed for the calculation of the moment of inertia of slab-beams from the center of the column to the face of the column, bracket or capital. ACI 318-14 (8.11.3)
- 2) Columns or other vertical supporting members, extending above and below the slab. Different values of moment of inertia along the axis of columns should be taken into account where the moment of inertia of columns from top and bottom of the slab-beam at a joint shall be assumed to be infinite, and the gross cross section of the concrete is permitted to be used to determine the moment of inertia of columns at any cross section outside of joints or column capitals. ACI 318-14 (8.11.4)
- 3) Elements of the structure (Torsional members) that provide moment transfer between the horizontal and vertical members. These elements shall be assumed to have a constant cross section throughout their length consisting of the greatest of the following: (1) portion of slab having a width equal to that of the column, bracket, or capital in the direction of the span for which moments are being determined, (2) portion of slab specified in (1) plus that part of the transverse beam above and below the slab for monolithic or fully composite construction, (3) the transverse beam includes that portion of slab on each side of the beam extending a distance equal to the projection of the beam above or below the slab, whichever is greater, but not greater than four times the slab thickness. ACI 318-14 (8.11.5)

2.1. Equivalent frame method limitations

In EFM, live load shall be arranged in accordance with 6.4.3 which requires slab systems to be analyzed and designed for the most demanding set of forces established by investigating the effects of live load placed in various critical patterns. ACI 318-14 (8.11.1.2 & 6.4.3)

Complete analysis must include representative interior and exterior equivalent frames in both the longitudinal and transverse directions of the floor. ACI 318-14 (8.11.2.1)

Panels shall be rectangular, with a ratio of longer to shorter panel dimensions, measured center-to-center of supports, not to exceed 2. ACI 318-14 (8.10.2.3)

2.2. Frame members of equivalent frame

Determine moment distribution factors and fixed-end moments for the equivalent frame members. The moment distribution procedure will be used to analyze the equivalent frame. Stiffness factors k , carry over factors COF, and fixed-end moment factors FEM for the slab-beams and column members are determined using the design aids tables at Appendix 20A of PCA Notes on ACI 318-11. These calculations are shown below.

- a. Flexural stiffness of slab-beams at both ends, K_{sb} .

$$\frac{c_{N1}}{\ell_1} = \frac{18}{(17.5 \times 12)} = 0.0857 \approx 0.1, \quad \frac{c_{N2}}{\ell_2} = \frac{18}{(22 \times 12)} = 0.0682$$

For $c_{F1} = c_{F2}$ stiffness factors, $k_{NF} = k_{FN} = 4.11$

$$\text{Thus, } K_{sb} = k_{NF} \frac{E_c I_{sb}}{\ell_1} = 4.11 \frac{E_c I_{sb}}{\ell_1}$$

Where I_{sb} is the moment of inertia of slab-beam section shown in Figure 6 and can be computed with the aid of Figure 7 as follows:

$$I_{sb} = C_t \left(\frac{b_w h^3}{12} \right) = 2.72 \left(\frac{14 \times 20^3}{12} \right) = 25387 \text{ in.}^4$$

$$K_{sb} = 4.11 \frac{E_c \times 25,387}{17.5 \times 12} = 497 E_c$$

Carry-over factor COF = 0.507

$$\text{Fixed-end moment FEM} = 0.0842 w_u \ell_2 \ell_1^2$$

PCA Notes on ACI 318-11 (Table A1)

PCA Notes on ACI 318-11 (Table A1)

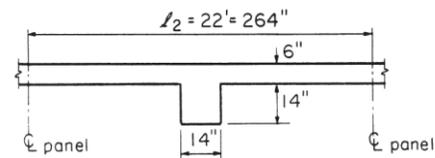


Figure 6 – Cross-Section of Slab-Beam

PCA Notes on ACI 318-11 (Table A1)

PCA Notes on ACI 318-11 (Table A1)

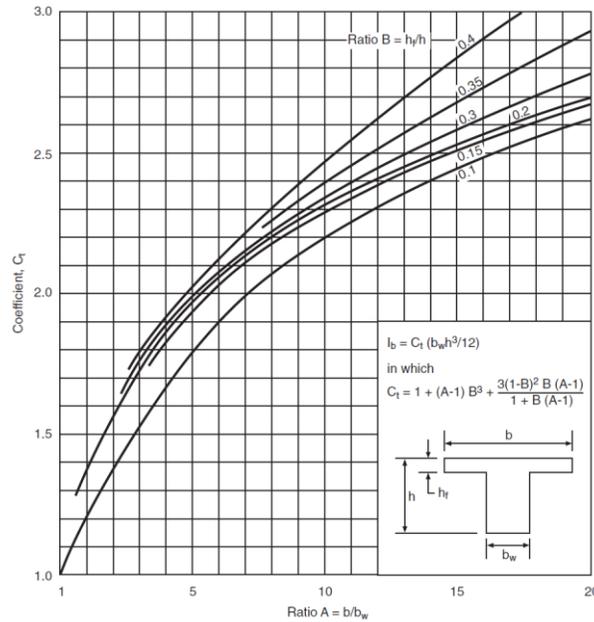


Figure 7 – Coefficient C_t for Gross Moment of Inertia of Flanged Sections

b. Flexural stiffness of column members at both ends, K_c .

Referring to **Table A7, Appendix 20A**:

For Interior Columns:

$$t_a = 20 - 6/2 = 17 \text{ in.}, t_b = 3 \text{ in.}$$

$$H = 12 \text{ ft} = 144 \text{ in.}, H_c = 144 - 17 - 3 = 124 \text{ in.}, \frac{t_a}{t_b} = 5.67, \frac{H}{H_c} = 1.16$$

Thus, $k_{c, \text{top}} = 6.82$ and $k_{c, \text{bottom}} = 4.99$ by interpolation.

$$I_c = \frac{c^4}{12} = \frac{(18)^4}{12} = 8,748 \text{ in.}^4$$

$$\ell_c = 12 \text{ ft} = 144 \text{ in.}$$

$$K_c = \frac{k_c E_c I_c}{\ell_c}$$

$$K_{c, \text{top}} = \frac{6.82 \times 8748 \times E_c}{144} = 414 E_c$$

$$K_{c, \text{bottom}} = \frac{4.99 \times 8748 \times E_c}{144} = 303 E_c$$

PCA Notes on ACI 318-11 (Table A7)

For Exterior Columns:

$$t_a = 27 - 6/2 = 24 \text{ in.}, t_b = 3 \text{ in.}$$

$$H = 12 \text{ ft} = 144 \text{ in.}, H_c = 144 - 24 - 3 = 117 \text{ in.}, \frac{t_a}{t_b} = 8.0, \frac{H}{H_c} = 1.23$$

Thus, $k_{c, top} = 8.57$ and $k_{c, bottom} = 5.31$ by interpolation.

$$I_c = \frac{c^4}{12} = \frac{(18)^4}{12} = 8,748 \text{ in.}^4$$

$$\ell_c = 12 \text{ ft} = 144 \text{ in.}$$

$$K_c = \frac{k_c E_c I_c}{\ell_c} \text{ PCA Notes on ACI 318-11 (Table A7)}$$

$$K_{c, top} = \frac{8.57 \times 8748 \times E_c}{144} = 521 E_c$$

$$K_{c, bottom} = \frac{5.31 \times 8748 \times E_c}{144} = 323 E_c$$

c. Torsional stiffness of torsional members, K_t .

$$K_t = \frac{9E_{cs}C}{[\ell_2(1 - \frac{c_2}{\ell_2})^3]} \quad \text{ACI 318-14 (R.8.11.5)}$$

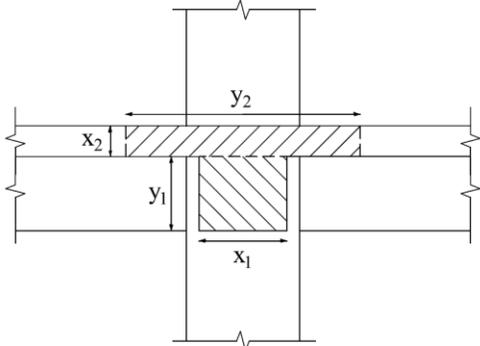
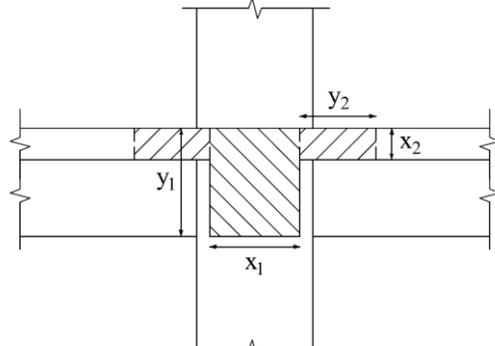
For Interior Columns:

$$K_t = \frac{9E_c \times 11,698}{264(0.932)^3} = 493E_c$$

Where:

$$1 - \frac{c_2}{\ell_2} = 1 - \frac{18}{22 \times 12} = 0.932$$

$$C = \sum(1 - 0.63 \frac{x}{y})(\frac{x^3 y}{3}) \quad \text{ACI 318-14 (Eq. 8.10.5.2b)}$$

| | | | |
|--|--|---|--|
| $x_1 = 14 \text{ in}$ $y_1 = 14 \text{ in}$ $C_1 = 4738$ | $x_2 = 6 \text{ in}$ $y_2 = 42 \text{ in}$ $C_2 = 2,752$ | $x_1 = 14 \text{ in}$ $y_1 = 20 \text{ in}$ $C_1 = 10,226$ | $x_2 = 6 \text{ in}$ $y_2 = 14 \text{ in}$ $C_2 = 736$ |
| $\sum C = 4738 + 2,752 = 7,490 \text{ in}^4$ | | $\sum C = 10,226 + 736 \times 2 = 11,698 \text{ in}^4$ | |
|  | |  | |

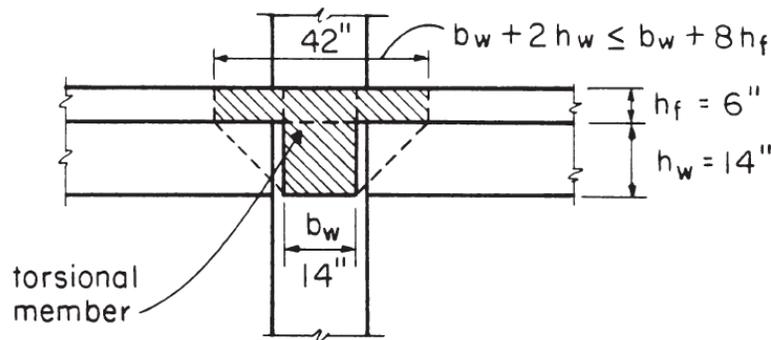


Figure 8 – Attached Torsional Member at Interior Column

For Exterior Columns:

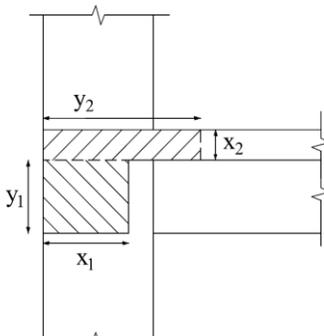
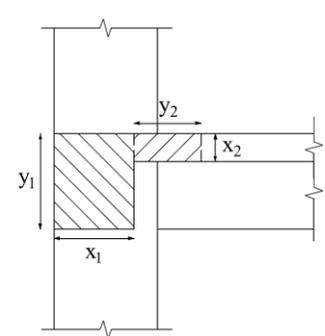
$$K_r = \frac{9E_c \times 17,868}{264(0.932)^3} = 752E_c$$

Where:

$$1 - \frac{c_2}{\ell_2} = 1 - \frac{18}{22 \times 12} = 0.932$$

$$C = \sum \left(1 - 0.63 \frac{x}{y}\right) \left(\frac{x^3 y}{3}\right)$$

ACI 318-14 (Eq. 8.10.5.2b)

| | | | |
|--|-----------------------|---|-----------------------|
| $x_1 = 14 \text{ in}$ | $x_2 = 6 \text{ in}$ | $x_1 = 14 \text{ in}$ | $x_2 = 6 \text{ in}$ |
| $y_1 = 21 \text{ in}$ | $y_2 = 35 \text{ in}$ | $y_1 = 27 \text{ in}$ | $y_2 = 21 \text{ in}$ |
| $C_1 = 11,141$ | $C_2 = 2,248$ | $C_1 = 16,628$ | $C_2 = 1,240$ |
| $\Sigma C = 11,141 + 2,248 = 13,389 \text{ in}^4$ | | $\Sigma C = 16,628 + 1,240 = 17,868 \text{ in}^4$ | |
|  | |  | |

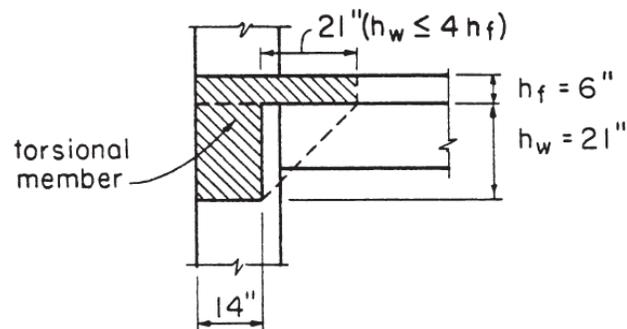


Figure 9 – Attached Torsional Member at Exterior Column

d. Increased torsional stiffness due to parallel beams, K_{ta} .

For Interior Columns:

$$K_{ta} = \frac{K_t I_{sb}}{I_s} = \frac{493E_c \times 25,387}{4752} = 2634E_c$$

Where:

$$I_{sb} = \frac{l_2 \times h^3}{12} = \frac{264 \times 6^3}{12} = 4752 \text{ in.}^4$$

For Exterior Columns:

$$K_{ta} = \frac{K_t I_{sb}}{I_s} = \frac{752E_c \times 25,387}{4752} = 4017E_c$$

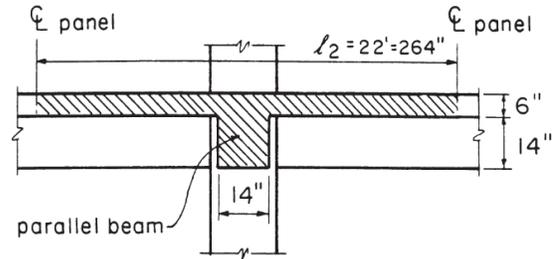


Figure 10 – Slab-Beam in the Direction of Analysis

e. Equivalent column stiffness K_{ec} .

$$K_{ec} = \frac{\sum K_c \times \sum K_{ta}}{\sum K_c + \sum K_{ta}}$$

Where $\sum K_{ta}$ is for two torsional members one on each side of the column, and $\sum K_c$ is for the upper and lower columns at the slab-beam joint of an intermediate floor.

For Interior Columns:

$$K_{ec} = \frac{(303E_c + 414E_c)(2 \times 2634E_c)}{(303E_c + 414E_c) + (2 \times 2634E_c)} = 631E_c$$

For Exterior Columns:

$$K_{ec} = \frac{(323E_c + 521E_c)(2 \times 4017E_c)}{(323E_c + 521E_c) + (2 \times 4017E_c)} = 764E_c$$

f. Slab-beam joint distribution factors, DF .

At exterior joint,

$$DF = \frac{497E_c}{(497E_c + 764E_c)} = 0.394$$

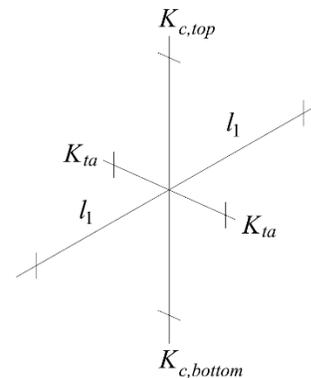


Figure 11 – Equivalent Column Stiffness

At interior joint,

$$DF = \frac{497E_c}{(497E_c + 497E_c + 631E_c)} = 0.306$$

COF for slab-beam = 0.507

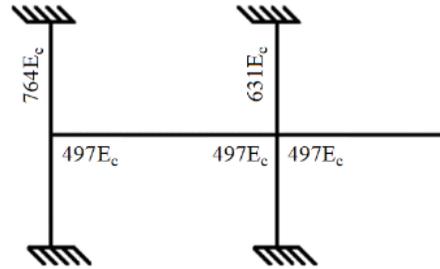


Figure 12 – Slab and Column Stiffness

2.3. Equivalent frame analysis

Determine negative and positive moments for the slab-beams using the moment distribution method.

With an unfactored live-to-dead load ratio:

$$\frac{L}{D} = \frac{100}{(150 \times 6 / 12)} = 1.33 > \frac{3}{4}$$

The frame will be analyzed for five loading conditions with pattern loading and partial live load as allowed by ACI 318-14 (6.4.3.3).

- a. Factored load and Fixed-End Moments (FEM's).

$$\text{Factored dead load } q_{Du} = 1.2(75 + 9.3) = 101 \text{ psf}$$

Where (9.3 psf = (14 x 14) / 144 x 150 / 22 is the weight of beam stem per foot divided by l_2)

$$\text{Factored live load } q_{Lu} = 1.6(100) = 160 \text{ psf}$$

$$\text{Factored load } q_u = q_{Du} + q_{Lu} = 261 \text{ psf}$$

$$\text{FEM's for slab-beam} = m_{NF} q_u \ell_2 \ell_1^2$$

PCA Notes on ACI 318-11 (Table A1)

$$\text{FEM due to } q_{Du} + q_{Lu} = 0.0842 \times (0.261 \times 22) \times 17.5^2 = 148.1 \text{ ft-kip}$$

$$\text{FEM due to } q_{Du} + \frac{3}{4} q_{Lu} = 0.0842 \times (0.221 \times 22) \times 17.5^2 = 125.4 \text{ ft-kip}$$

$$\text{FEM due to } q_{Du} = 0.0842 \times (0.101 \times 22) \times 17.5^2 = 57.3 \text{ ft-kip}$$

- b. Moment distribution.

Moment distribution for the five loading conditions is shown in Table 1. Counter-clockwise rotational moments acting on member ends are taken as positive. Positive span moments are determined from the following equation:

$$M_{u(\text{midspan})} = M_o - \frac{(M_{uL} + M_{uR})}{2}$$

Where M_o is the moment at the midspan for a simple beam.

When the end moments are not equal, the maximum moment in the span does not occur at the midspan, but its value is close to that midspan for this example.

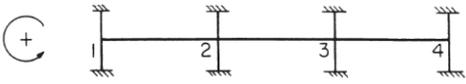
Positive moment in span 1-2 for loading (1):

$$M_u^+ = (0.261 \times 22) \frac{17.5^2}{8} - \frac{(93.1 + 167.7)}{2} = 89.4 \text{ ft-kip}$$

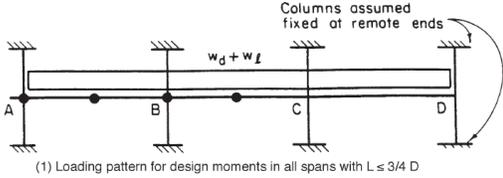
Positive moment span 2-3 for loading (1):

$$M_u^+ = (0.261 \times 22) \frac{17.5^2}{8} - \frac{(153.6 + 153.6)}{2} = 66.2 \text{ ft-kip}$$

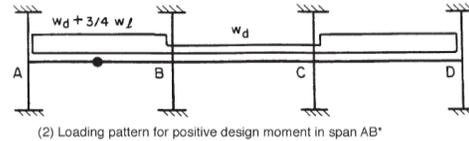
| Table 1 – Moment Distribution for Partial Frame (Transverse Direction) | | | | | | |
|--|-------|-------|-------|-------|-------|-------|
| Joint | 1 | 2 | | 3 | | 4 |
| Member | 1-2 | 2-1 | 2-3 | 3-2 | 3-4 | 4-3 |
| DF | 0.394 | 0.306 | 0.306 | 0.306 | 0.306 | 0.394 |
| COF | 0.507 | 0.507 | 0.507 | 0.507 | 0.507 | 0.507 |



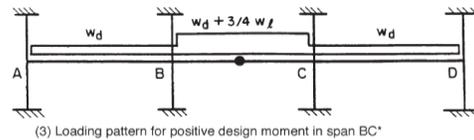
| Loading (1) All spans loaded with full factored live load | | | | | | |
|---|-------|--------|-------|--------|-------|--------|
| FEM | 148.1 | -148.1 | 148.1 | -148.1 | 148.1 | -148.1 |
| Dist | -58.4 | 0 | 0 | 0 | 0 | 58.4 |
| CO | 0 | -29.6 | 0 | 0 | 29.6 | 0 |
| Dist | 0 | 9.1 | 9.1 | -9.1 | -9.1 | 0 |
| CO | 4.6 | 0 | -4.6 | 4.6 | 0 | -4.6 |
| Dist | -1.8 | 1.4 | 1.4 | -1.4 | -1.4 | 1.8 |
| CO | 0.7 | -0.9 | -0.7 | 0.7 | 0.9 | -0.7 |
| Dist | -0.3 | 0.5 | 0.5 | -0.5 | -0.5 | 0.3 |
| CO | 0.3 | -0.1 | -0.3 | 0.3 | 0.1 | -0.3 |
| Dist | -0.1 | 0.1 | 0.1 | -0.1 | -0.1 | 0.1 |
| M | 93.1 | -167.6 | 153.6 | -153.6 | 167.6 | -93.1 |
| Midspan M | 89.5 | | 66.2 | | 89.5 | |



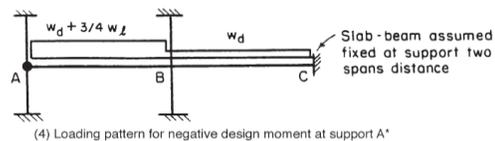
| Loading (2) First and third spans loaded with 3/4 factored live load | | | | | | |
|--|-------|--------|-------|-------|-------|--------|
| FEM | 125.4 | -125.4 | 57.3 | -57.3 | 125.4 | -125.4 |
| Dist | -49.4 | 20.8 | 20.8 | -20.8 | -20.8 | 49.4 |
| CO | 10.6 | -25.1 | -10.6 | 10.6 | 25.1 | -10.6 |
| Dist | -4.2 | 10.9 | 10.9 | -10.9 | -10.9 | 4.2 |
| CO | 5.5 | -2.1 | -5.5 | 5.5 | 2.1 | -5.5 |
| Dist | -2.2 | 2.3 | 2.3 | -2.3 | -2.3 | 2.2 |
| CO | 1.2 | -1.1 | -1.2 | 1.2 | 1.1 | -1.2 |
| Dist | -0.5 | 0.7 | 0.7 | -0.7 | -0.7 | 0.5 |
| CO | 0.4 | -0.2 | -0.4 | 0.4 | 0.2 | -0.4 |
| Dist | -0.1 | 0.2 | 0.2 | -0.2 | -0.2 | 0.1 |
| M | 86.7 | -119 | 74.5 | -74.5 | 119 | -86.7 |
| Midspan M | 83.3 | | 10.6 | | 83.3 | |



| Loading (3) Center span loaded with 3/4 factored live load | | | | | | |
|--|-------|-------|-------|--------|------|-------|
| FEM | 57.3 | -57.3 | 125.4 | -125.4 | 57.3 | -57.3 |
| Dist | -22.6 | -20.8 | -20.8 | 20.8 | 20.8 | 22.6 |
| CO | -10.6 | -11.4 | 10.6 | -10.6 | 11.4 | 10.6 |
| Dist | 4.2 | 0.3 | 0.3 | -0.3 | -0.3 | -4.2 |
| CO | 0.1 | 2.1 | -0.1 | 0.1 | -2.1 | -0.1 |
| Dist | -0.1 | -0.6 | -0.6 | 0.6 | 0.6 | 0.1 |
| CO | -0.3 | 0 | 0.3 | -0.3 | 0 | 0.3 |
| Dist | 0.1 | -0.1 | -0.1 | 0.1 | 0.1 | -0.1 |
| CO | 0 | 0.1 | 0 | 0 | -0.1 | 0 |
| Dist | 0 | 0 | 0 | 0 | 0 | 0 |
| M | 28.1 | -87.7 | 115 | -115 | 87.7 | -28.1 |
| Midspan M | 27.2 | | 71.3 | | 27.2 | |

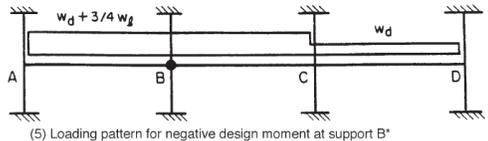


| Loading (4) First span loaded with 3/4 factored live load and beam-slab assumed fixed at support two spans away | | | | |
|---|-------|--------|------|-------|
| FEM | 125.4 | -125.4 | 57.3 | -57.3 |
| Dist | -49.4 | 20.8 | 20.8 | 0 |
| CO | 10.6 | -25 | 0 | 10.6 |
| Dist | -4.2 | 7.7 | 7.7 | 0 |
| CO | 3.9 | -2.1 | 0 | 3.9 |
| Dist | -1.5 | 0.6 | 0.6 | 0 |
| CO | 0.3 | -0.8 | 0 | 0.3 |
| Dist | -0.1 | 0.2 | 0.2 | 0 |
| CO | 0.1 | -0.1 | 0 | 0.1 |
| Dist | 0 | 0 | 0 | 0 |
| M | 85.1 | -124.1 | 86.6 | -42.4 |

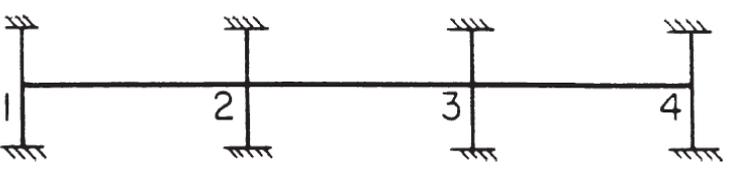


| | | | | |
|-----------|------|------|--|--|
| Midspan M | 81.5 | 20.6 | | |
|-----------|------|------|--|--|

| Loading (5) First and second spans loaded with 3/4 factored live load | | | | | | |
|---|-------|--------|-------|--------|------|-------|
| FEM | 125.4 | -125.4 | 125.4 | -125.4 | 57.3 | -57.3 |
| Dist | -49.4 | 0.0 | 0.0 | 20.8 | 20.8 | 22.6 |
| CO | 0.0 | -25.1 | 10.6 | 0.0 | 11.4 | 10.6 |
| Dist | 0.0 | 4.4 | 4.4 | -3.5 | -3.5 | -4.2 |
| CO | 2.2 | 0.0 | -1.8 | 2.2 | -2.1 | -1.8 |
| Dist | -0.9 | 0.5 | 0.5 | 0.0 | 0.0 | 0.7 |
| CO | 0.3 | -0.4 | 0.0 | 0.3 | 0.4 | 0.0 |
| Dist | -0.1 | 0.1 | 0.1 | -0.2 | -0.2 | 0.0 |
| CO | 0.1 | -0.1 | -0.1 | 0.1 | 0.0 | -0.1 |
| Dist | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| M | 77.6 | -146.0 | 139.1 | -105.7 | 84.1 | -29.5 |
| Midspan M | 74.3 | | 63.7 | | 28.3 | |



(5) Loading pattern for negative design moment at support B*

| | | | | | | |
|--|---|--------|-------|--------|-------|-------|
|  |  | | | | | |
| Max M ⁻ | 93.1 | -167.7 | 153.6 | -153.6 | 167.7 | -93.1 |
| Max M ⁺ | 89.4 | | 71.3 | | 89.4 | |

2.4. Design moments

Positive and negative factored moments for the slab system in the direction of analysis are plotted in Figure 13. The negative design moments are taken at the faces of rectilinear supports but not at distances greater than $0.175\ell_1$ from the centers of supports. ACI 318-14 (8.11.6.1)

$$\frac{18\text{in.}}{2} = 0.75 \text{ ft} < 0.175 \times 17.5 = 3.1 \text{ ft (use face of support location)}$$

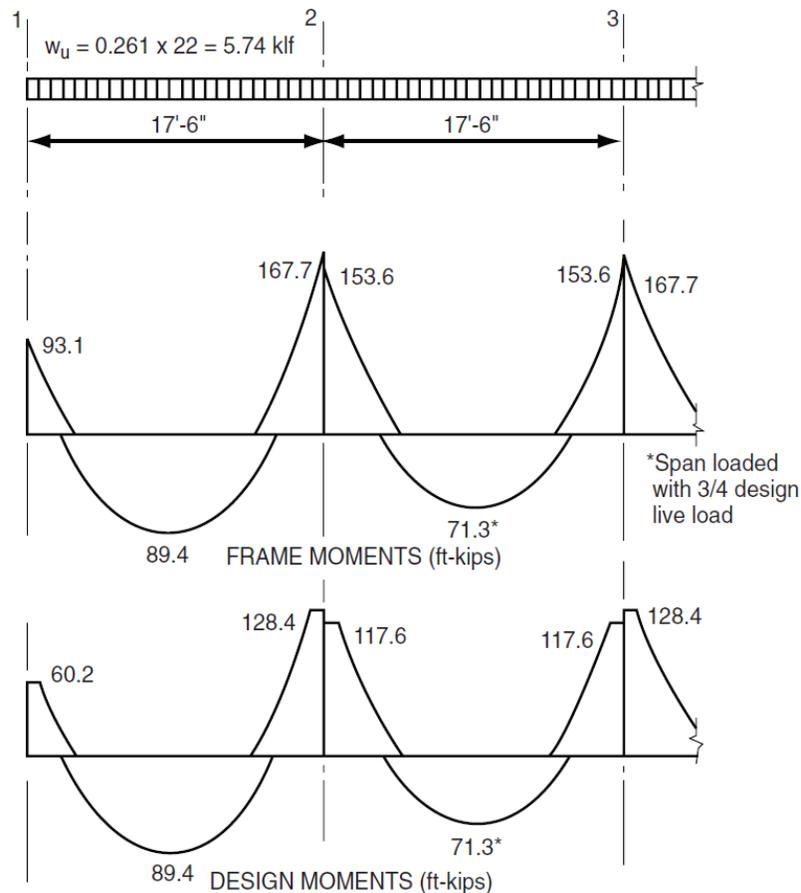


Figure 13 – Positive and Negative Design Moments for Slab-Beam (All Spans Loaded with Full Factored Live Load
Except as Noted)

2.5. Distribution of design moments

- a. Check whether the moments calculated above can take advantage of the reduction permitted by ACI 318-14 (8.11.6.5):

Slab systems within the limitations of ACI 318-14 (8.10.2) may have the resulting reduced in such proportion that the numerical sum of the positive and average negative moments not be greater than the total static moment M_o given by Equation 8.10.3.2 in the ACI 318-14:

ACI 318-14 (8.11.6.5)

Check Applicability of Direct Design Method:

1. There is a minimum of three continuous spans in each direction ACI 318-14 (8.10.2.1)
2. Successive span lengths are equal ACI 318-14 (8.10.2.2)
3. Long-to-Short ratio is $22/17.5 = 1.26 < 2.0$ ACI 318-14 (8.10.2.3)
4. Column are not offset ACI 318-14 (8.10.2.4)
5. Loads are gravity and uniformly distributed with service live-to-dead ratio of $1.33 < 2.0$ ACI 318-14 (8.10.2.5 and 6)

6. Check relative stiffness for slab panel:

ACI 318-14 (8.10.2.7)

Interior Panel:

$$\alpha_{f1} = 3.16, l_2 = 22 \times 12 = 264 \text{ in.}$$

$$\alpha_{f2} = 3.98, l_1 = 17.5 \times 12 = 210 \text{ in.}$$

$$\frac{\alpha_{f1} l_2^2}{\alpha_{f2} l_1^2} = \frac{3.16 \times 264^2}{3.98 \times 210^2} = 1.25 \rightarrow 0.2 < 1.25 < 5.0 \quad \text{O.K.} \quad \text{ACI 318-14 (Eq. 8.10.2.7a)}$$

Interior Panel:

$$\alpha_{f1} = 3.16, l_2 = 22 \times 12 = 264 \text{ in.}$$

$$\alpha_{f2} = 16.45, l_1 = 17.5 \times 12 = 210 \text{ in.}$$

$$\frac{\alpha_{f1} l_2^2}{\alpha_{f2} l_1^2} = \frac{3.16 \times 264^2}{16.45 \times 210^2} = 0.30 \rightarrow 0.2 < 0.30 < 5.0 \quad \text{O.K.} \quad \text{ACI 318-14 (Eq. 8.10.2.7a)}$$

All limitation of ACI 318-14 (8.10.2) are satisfied and the provisions of ACI 318-14 (8.11.6.5) may be applied:

$$M_o = \frac{q_u \ell_2 \ell_n^2}{8} = 0.261 \times 22 \times \frac{(16)^2}{8} = 183.7 \text{ ft-kip} \quad \text{ACI 318-14 (Eq. 8.10.3.2)}$$

$$\text{End spans: } 89.4 + \frac{(60.2 + 128.4)}{2} = 183.7 \text{ ft-kip}$$

$$\text{Interior span: } 71.2 + \frac{(117.6 + 117.6)}{2} = 188.8 \text{ ft-kip}$$

To illustrate proper procedure, the interior span factored moments may be reduced as follows:

$$\text{Permissible reduction} = 183.7 / 188.8 = 0.973$$

$$\text{Adjusted negative design moment} = 117.6 \times 0.973 = 114.3 \text{ ft-kip}$$

$$\text{Adjusted positive design moment} = 71.2 \times 0.973 = 69.3 \text{ ft-kip}$$

$$M_o = 183.7 \text{ ft-kip}$$

b. Distribute factored moments to column and middle strips:

The negative and positive factored moments at critical sections may be distributed to the column strip and the two half-middle strips of the slab-beam according to the Direct Design Method (DDM) in 8.10, provided that Eq. 8.10.2.7(a) is satisfied. ACI 318-14 (8.11.6.6)

Since the relative stiffness of beams are between 0.2 and 5.0 (see step 2.4.1.6), the moments can be distributed across slab-beams as specified in ACI 318-14 (8.10.5 and 6) where:

$$\frac{\ell_2}{\ell_1} = \frac{22}{17.5} = 1.257$$

$$\frac{\alpha_{f1} \ell_2}{\ell_1} = 3.16 \times 1.257 = 3.97$$

$$\beta_t = \frac{C}{2I_s} = \frac{17,868}{2 \times 4,752} = 1.88$$

$$\text{Where } I_s = \frac{22 \times 12 \times 6^3}{12} = 4,752 \text{ in.}^4$$

$$C = 17,868 \text{ in.}^4 \text{ (see Figure 9)}$$

Factored moments at critical sections are summarized in Table 2.

| Table 2 - Lateral distribution of factored moments | | | | | | | |
|--|-------------------|----------------------------|--------------|------------------|-----------------------------|-------------------------------|---|
| | | Factored Moments (ft-kips) | Column Strip | | | | Moments in Two Half-Middle Strips** (ft-kips) |
| | | | Percent* | Moment (ft-kips) | Beam Strip Moment (ft-kips) | Column Strip Moment (ft-kips) | |
| End Span | Exterior Negative | 60.2 | 75 | 45.2 | 38.4 | 6.8 | 15 |
| | Positive | 89.4 | 67 | 59.9 | 50.9 | 9.0 | 29.5 |
| | Interior Negative | 128.4 | 67 | 86 | 73.1 | 12.9 | 42.4 |
| Interior Span | Negative | 117.6 | 67 | 78.8 | 67.0 | 11.8 | 38.8 |
| | Positive | 71.3 | 67 | 47.8 | 40.6 | 7.2 | 23.5 |

*Since $\alpha_1 \ell_2 / \ell_1 > 1.0$ beams must be proportioned to resist 85 percent of column strip per **ACI 318-14 (8.10.5.7)**

**That portion of the factored moment not resisted by the column strip is assigned to the two half-middle strips

2.6. Flexural reinforcement requirements

- a. Determine flexural reinforcement required for strip moments

The flexural reinforcement calculation for the column strip of end span – interior negative location is provided below:

$$M_u = 12.9 \text{ ft-kip}$$

Assume tension-controlled section ($\phi = 0.9$)

Column strip width, $b = (17.5 \times 12) / 2 = 91 \text{ in.}$

Use average $d = 6 - 0.75 - 0.5/2 = 5 \text{ in.}$

$$A_s = \frac{0.85 \times f'_c \times b}{f_y} \left(d - \sqrt{d^2 - \frac{2 \times M_u}{\phi \times 0.85 \times f'_c \times b}} \right)$$

$$A_s = \frac{0.85 \times 4000 \times 91}{60,000} \left(5 - \sqrt{5^2 - \frac{2 \times 12.9 \times 12,000}{0.9 \times 0.85 \times 4000 \times 91}} \right) = 0.580 \text{ in.}^2$$

$$A_{s,min} = \max \begin{bmatrix} 0.0018 \times b \times h \\ 0.0014 \times b \times h \end{bmatrix} = \max \begin{bmatrix} 0.0018 (14)(19) \\ 0.0014 (14)(19) \end{bmatrix} = \max \begin{bmatrix} 0.983 \\ 0.764 \end{bmatrix} = 0.983 \text{ in.}^2 < 0.580 \text{ in.}^2 \text{ in}^2$$

$$\therefore A_s = 0.983 \text{ in.}^2$$

Maximum spacing $s_{max} = 2h = 2 \times 6 = 12 \text{ in.} < 18 \text{ in.}$

ACI 318-14 (8.7.2.2)

Provide 8 - #4 bars with $A_s = 1.60 \text{ in.}^2$ and $s = 91/8 = 11.37 \text{ in.} \leq s_{max}$

The flexural reinforcement calculation for the beam strip of end span – interior negative location is provided below:

$$M_u = 73.1 \text{ ft-kip}$$

Assume tension-controlled section ($\phi = 0.9$)

Beam strip width, $b = 14 \text{ in.}$

Use average $d = 20 - 0.75 - 0.5/2 = 19 \text{ in.}$

$$A_s = \frac{0.85 \times f'_c \times b}{f_y} \left(d - \sqrt{d^2 - \frac{2 \times M_u}{\phi \times 0.85 \times f'_c \times b}} \right)$$

$$A_s = \frac{0.85 \times 4000 \times 14}{60,000} \left(18.25 - \sqrt{19^2 - \frac{2 \times 73.1 \times 12,000}{0.9 \times 0.85 \times 4000 \times 14}} \right) = 0.881 \text{ in.}^2$$

$$A_{s,min} = \max \begin{bmatrix} \frac{3\sqrt{f'_c}}{f_y} bd \\ \frac{200}{f_y} bd \end{bmatrix} = \max \begin{bmatrix} \frac{3\sqrt{4000}}{60,000} (14)(19) \\ \frac{200}{60,000} (14)(19) \end{bmatrix} = \max \begin{bmatrix} 0.841 \\ 0.887 \end{bmatrix} = 0.887 \text{ in.}^2 < 0.881 \text{ in.}^2$$

$$\therefore A_s = 0.887 \text{ in.}^2$$

Provide 5 - #4 bars with $A_s = 1.00 \text{ in.}^2$

All the values on Table 3 are calculated based on the procedure outlined above.

| Table 3 - Required Slab Reinforcement for Flexure [Equivalent Frame Method (EFM)] | | | | | | | | |
|---|-------------------|----------------------------|--------------|---------------|--|--|---------------------------|--|
| Span Location | | M _u (ft-kip) | b * (in.) | d ** (in.) | A _s Req'd for flexure (in. ²) | Min A _s [†] ‡‡ (in. ²) | Reinforcement Provided | A _s Prov. for flexure (in. ²) |
| End Span | | | | | | | | |
| Beam Strip | Exterior Negative | 38.4 | 14 | 19.00 | 0.456 | 0.608 | 4 - #4 | 0.8 |
| | Positive | 50.9 | 14 | 18.25 | 0.634 | 0.852 | 5 - #4 | 1.0 |
| | Interior Negative | 73.1 | 14 | 19.00 | 0.881 | 0.887 | 5 - #4 | 1.0 |
| Column Strip | Exterior Negative | 6.8 | 91 | 5.00 | 0.304 | 0.983 | 8 - #4 | 1.6 |
| | Positive | 9.0 | 91 | 5.00 | 0.403 | 0.983 | 8 - #4 | 1.6 |
| | Interior Negative | 12.9 | 91 | 5.00 | 0.580 | 0.983 | 8 - #4 | 1.6 |
| Middle Strip | Exterior Negative | 15.0 | 159 | 5.00 | 0.672 | 1.717 | 14 - #4 | 2.8 |
| | Positive | 29.5 | 159 | 5.00 | 1.331 | 1.717 | 14 - #4 | 2.8 |
| | Interior Negative | 42.4 | 159 | 5.00 | 1.926 | 1.717 | 14 - #4 | 2.8 |
| Interior Span | | | | | | | | |
| Beam Strip | Positive | 40.6 | 14 | 18.25 | 0.503 | 0.671 | 4 - #4 | 0.8 |
| Column Strip | Positive | 7.2 | 91 | 5.00 | 0.322 | 0.983 | 8 - #4 | 1.6 |
| Middle Strip | Positive | 23.5 | 159 | 5.00 | 1.057 | 1.717 | 14 - #4 | 2.8 |
| * Column strip width, b = (17.5 × 12)/2 - 14 = 91 in. * Middle strip width, b = 22*12-(17.5*12)/2 = 159 in. * Beam strip width, b = 14 in. ** Use average d = 6 - 0.75 - 0.5/2 = 5.00 in. for Column and Middle strips ** Use average d = 20 - 1.5 - 0.5/2 = 18.25 in. for Beam strip Positive moment regions ** Use average d = 20 - 0.75 - 0.5/2 = 19 in. for Beam strip Negative moment regions † Min. A _s = 0.0018 × b × h = 0.0108 × b for Column and Middle strips ACI 318-14 (7.6.1.1) † Min. A _s = min (3(fc') ^{0.5} /f _y *b*d , 200/f _y *b*d) for Beam strip ACI 318-14 (9.6.1.2) ‡‡ Min. A _s = 1.333 × A _s Req'd if A _s provided >= 1.333 × A _s Req'd for Beam strip ACI 318-14 (9.6.1.3) s _{max} = 2 × h = 12 in. < 18 in. ACI 318-14 (8.7.2.2) | | | | | | | | |

b. Calculate additional slab reinforcement at columns for moment transfer between slab and column by flexure

Portion of the unbalanced moment transferred by flexure is $\gamma_f \times M_u$

Where:

$$\gamma_f = \frac{1}{1 + (2/3) \times \sqrt{b_1 / b_2}} \quad \text{ACI 318-14 (8.4.2.3.2)}$$

b_1 = Dimension of the critical section b_o measured in the direction of the span for which moments are determined in ACI 318, Chapter 8.

b_2 = Dimension of the critical section b_o measured in the direction perpendicular to b_1 in ACI 318, Chapter 8.

b_o = Perimeter of critical section for two-way shear in slabs and footings.

b_b = Effective slab width = $c_2 + 3 \times h$

ACI 318-14 (8.4.2.3.3)

For Exterior Column:

$$b_1 = c_1 + \frac{d}{2} = 18 + \frac{5}{2} = 20.5 \text{ in.}, \quad b_2 = c_2 + d = 18 + 5 = 23 \text{ in.}, \quad b_b = c_2 + 3h = 18 + 3(6) = 36 \text{ in.}$$

$$\gamma_f = \frac{1}{1 + (2/3) \times \sqrt{20.5/23}} = 0.614$$

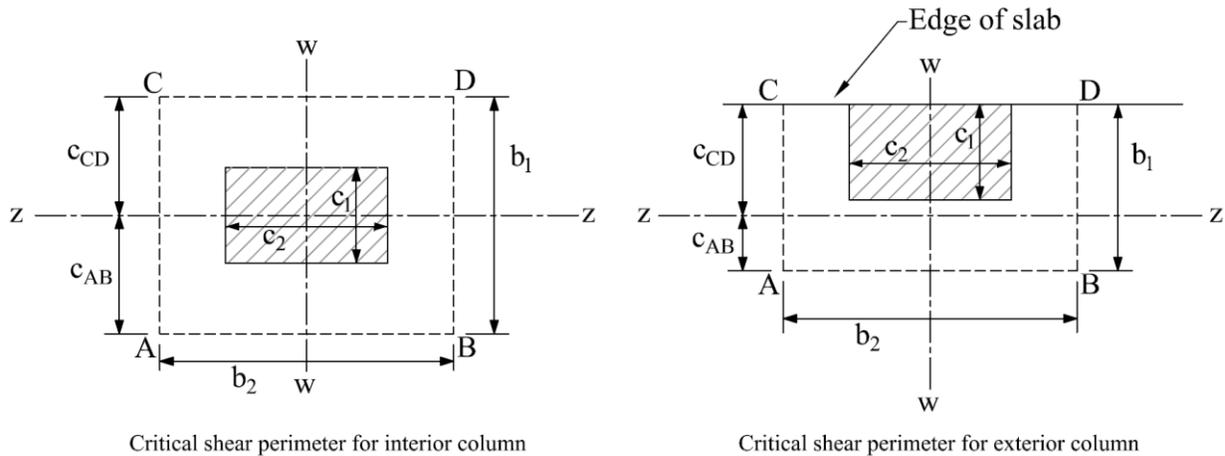


Figure 14 – Critical Shear Perimeters for Columns

$$\gamma_f M_{u,net} = 0.614 \times 93.1 = 57.14 \text{ ft-kip}$$

$$A_{s,req'd} = \frac{0.85 \times f'_c \times b_b}{f_y} \left(d - \sqrt{d^2 - \frac{2 \times \gamma_f M_{u,net}}{\phi \times 0.85 \times f'_c \times b_b}} \right)$$

$$A_{s,req'd} = \frac{0.85 \times 4000 \times 36}{60,000} \left(5 - \sqrt{5^2 - \frac{2 \times 57.14 \times 12,000}{0.9 \times 0.85 \times 4000 \times 36}} \right) = 2.973 \text{ in.}^2$$

$$A_{s,min} = \max \begin{bmatrix} 0.0018 \times b \times h \\ 0.0014 \times b \times h \end{bmatrix} = \max \begin{bmatrix} 0.0018 (14)(19) \\ 0.0014 (14)(19) \end{bmatrix} = \max \begin{bmatrix} 0.983 \\ 0.764 \end{bmatrix} = 0.983 \text{ in.}^2 > 2.973 \text{ in.}^2$$

$$\therefore A_{s,req'd} = 2.973 \text{ in.}^2$$

$$A_{s,provided} = (A_{s,provided})_{(beam)} + (A_{s,provided})_{(b_b - b_{beam})}$$

$$A_{s,provided} = 4 \times 0.2 + 8 \times 0.2 \times \frac{36 - 14}{91} = 1.187 \text{ in.}^2 < A_{s,req'd} = 2.973 \text{ in.}^2$$

\therefore Additional slab reinforcement at the exterior column is required.

$$A_{req'd,add} = 2.973 - 1.187 = 1.786 \text{ in.}^2$$

Use 10 - #4 $\rightarrow A_{provided, add} = 10 \times 0.2 = 2.0 \text{ in.}^2 < A_{req'd, add} = 1.786 \text{ in.}^2$

| Table 4 - Additional Slab Reinforcement at columns for moment transfer between slab and column [Equivalent Frame Method (EFM)] | | | | | | | | | |
|--|-------------------|-----------------------------------|-----------|------------|------------------|-------------------------|--|--|--------------|
| Span Location | | Effective slab width, b_b (in.) | d (in.) | γ_r | M_u^* (ft-kip) | $\gamma_r M_u$ (ft-kip) | A_s req'd within b_b (in. ²) | A_s prov. for flexure within b_b (in. ²) | Add'l Reinf. |
| End Span | | | | | | | | | |
| Column Strip | Exterior Negative | 36 | 5 | 0.614 | 93.1 | 57.14 | 2.973 | 1.187 | 10-#4 |
| | Interior Negative | 36 | 5 | 0.600 | 44.5 | 26.70 | 1.265 | 1.387 | - |

* M_u is taken at the centerline of the support in Equivalent Frame Method solution.

b. Determine transverse reinforcement required for beam strip shear

The transverse reinforcement calculation for the beam strip of end span – exterior location is provided below.

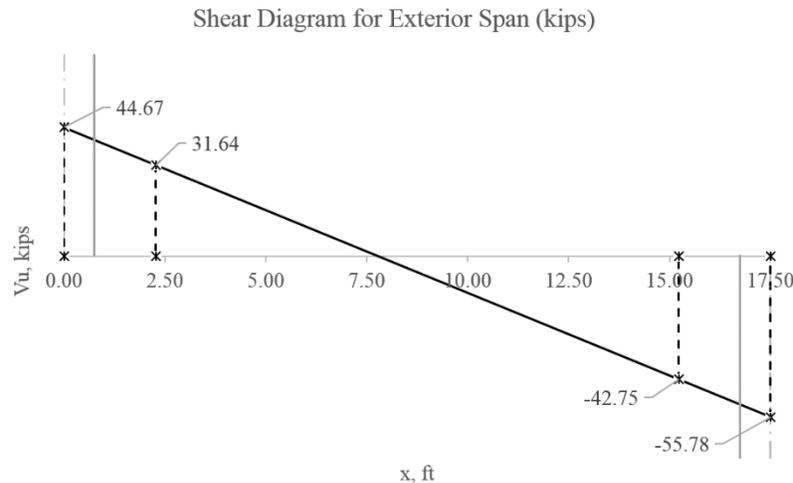


Figure 15 – Shear at critical sections for the end span (at distance d from the face of the column)

$$d = h - c_{clear} - \frac{d_{stirrup}}{2} = 20 - 1.5 - \frac{0.5}{2} = 18.25 \text{ in. (using #4 stirrups)}$$

The required shear at a distance d from the face of the supporting column $V_{u-d} = 31.64$ kips (Figure 15).

$$\phi_v V_c = \phi_v \times 2 \times \sqrt{f_c'} \times b \times d \quad \text{ACI 318-14 (22.5.5.1)}$$

$$\phi_v V_c = 0.75 \times 2 \times \sqrt{4000} \times 14 \times 18.25 = 24.25 \text{ kips} < V_{u-d} = 31.64 \text{ kip} \quad \therefore \text{Stirrups are required.}$$

Distance from the column face beyond which minimum reinforcement is required:

$$V_s = \frac{V_{u-d} - \phi_v V_c}{\phi_v} \quad \text{ACI 318-14 (22.5.10.1)}$$

$$V_s = \frac{31.64 - 24.25}{0.75} = 9.85 \text{ kip} < V_{s,max} = 129.31 \text{ kip} \quad \text{O.K.}$$

$$V_{s,max} = 8 \times \sqrt{f'_c} \times b \times d = 8 \times \sqrt{4000} \times 14 \times 18.25 = 129.31 \text{ kip}$$

ACI 318-14 (22.5.10.1)

$$\frac{A_{v,req'd}}{s} = \frac{V_s}{f_{yt} \times d} = \frac{9.85 \times 1000}{60,000 \times 18.25} = 0.009 \text{ in.}^2/\text{in.}$$

ACI 318-14 (22.5.10.5.3)

$$\frac{A_{v,min}}{s} = \max \left[\begin{array}{l} \frac{0.75 \sqrt{f'_c}}{f_{yt}} b \\ \frac{50}{f_{yt}} b \end{array} \right]$$

ACI 318-14 (9.6.3.3)

$$\frac{A_{v,min}}{s} = \max \left[\begin{array}{l} \frac{0.75 \sqrt{4000}}{60,000} (14) \\ \frac{50}{60,000} (14) \end{array} \right] = \max \left[\begin{array}{l} 0.0111 \\ 0.0117 \end{array} \right] = 0.0117 \text{ in.}^2/\text{in.}$$

$$\frac{A_{v,req'd}}{s} < \frac{A_{v,min}}{s} \rightarrow \therefore \text{ use } \frac{A_{s,req'd}}{s} = \frac{A_{v,min}}{s}$$

$$s_{req'd} = \frac{n \times A_{stirrup}}{\frac{A_{v,req'd}}{s}} = \frac{2 \times 0.2}{0.0117} = 34.28 \text{ in.}$$

$$V_s = 9.85 \text{ kips} < 4 \times \sqrt{f'_c} \times b \times d = 4 \times \sqrt{4000} \times 14 \times 18.25 = 64.66 \text{ kips}$$

$$\therefore s_{max} = \text{Lesser of } \left[\frac{d}{2} \right] = \text{Lesser of } \left[\frac{18.25}{2} \right] = \text{Lesser of } \left[\frac{9.13}{24} \right] = 9.13 \text{ in.}$$

ACI 318-14 (9.7.6.2.2)

Since $s_{req'd} > s_{max} \rightarrow$ use s_{max}

Select $s_{provided} = 8 \text{ in.}$ #4 stirrups with first stirrup located at distance 3 in. from the column face.

The distance where the shear is zero is calculated as follows:

$$x = \frac{l}{V_{u,L} + V_{u,R}} \times V_{u,L} = \frac{17.5}{44.67 + 55.78} \times 44.67 = 7.78 \text{ ft} = 93.4 \text{ in.}$$

The distance from support beyond which minimum reinforcement is required is calculated as follows:

$$x_1 = x - \frac{x}{V_u} \times \phi_v V_c = 7.78 - \frac{7.78}{44.67} \times 24.25 = 3.56 \text{ ft} = 43 \text{ in.}$$

The distance at which no shear reinforcement is required is calculated as follows:

$$x_2 = x - \frac{x}{V_u} \times \frac{\phi_v V_c}{2} = 7.78 - \frac{7.78}{44.67} \times \frac{24.25}{2} = 5.67 \text{ ft} = 68 \text{ in.}$$

$$\# \text{ of stirrups} = \frac{x_2 - 3 - \frac{c_1}{2} - \frac{s_{provided}}{2}}{s_{provided}} + 1 = \frac{68 - 3 - \frac{18}{2} - \frac{8}{2}}{8} + 1 = 7.5 \rightarrow \text{ use 8 stirrups}$$

All the values on Table 5 are calculated based on the procedure outlined above.

| Table 5 - Required Beam Reinforcement for Shear | | | | | |
|--|---|---|--------------------------------------|------------------------------------|-----------------------------------|
| Span Location | $A_{v,min}/S$ in²/in | $A_{v,req'd}/S$ in²/in | $S_{req'd}$ in | S_{max} in | Reinforcement Provided |
| End Span | | | | | |
| Exterior | 0.0117 | 0.0090 | 34.28 | 9.13 | 8 - #4 @ 8 in* |
| Interior | 0.0117 | 0.0225 | 17.76 | 9.13 | 10 - #4 @ 8.6 in |
| Interior Span | | | | | |
| Interior | 0.0117 | 0.0158 | 25.37 | 9.13 | 9 - #4 @ 8.6 in |
| * Minimum transverse reinforcement governs | | | | | |

2.7. Column design moments

The unbalanced moment from the slab-beams at the supports of the equivalent frame are distributed to the actual columns above and below the slab-beam in proportion to the relative stiffness of the actual columns. Referring to Fig. 9, the unbalanced moment at joints 1 and 2 are:

Joint 1 = +93.1 ft-kip

Joint 2 = -119 + 74.5 = -44.5 ft-kip

The stiffness and carry-over factors of the actual columns and the distribution of the unbalanced moments to the exterior and interior columns are shown in Fig 9.

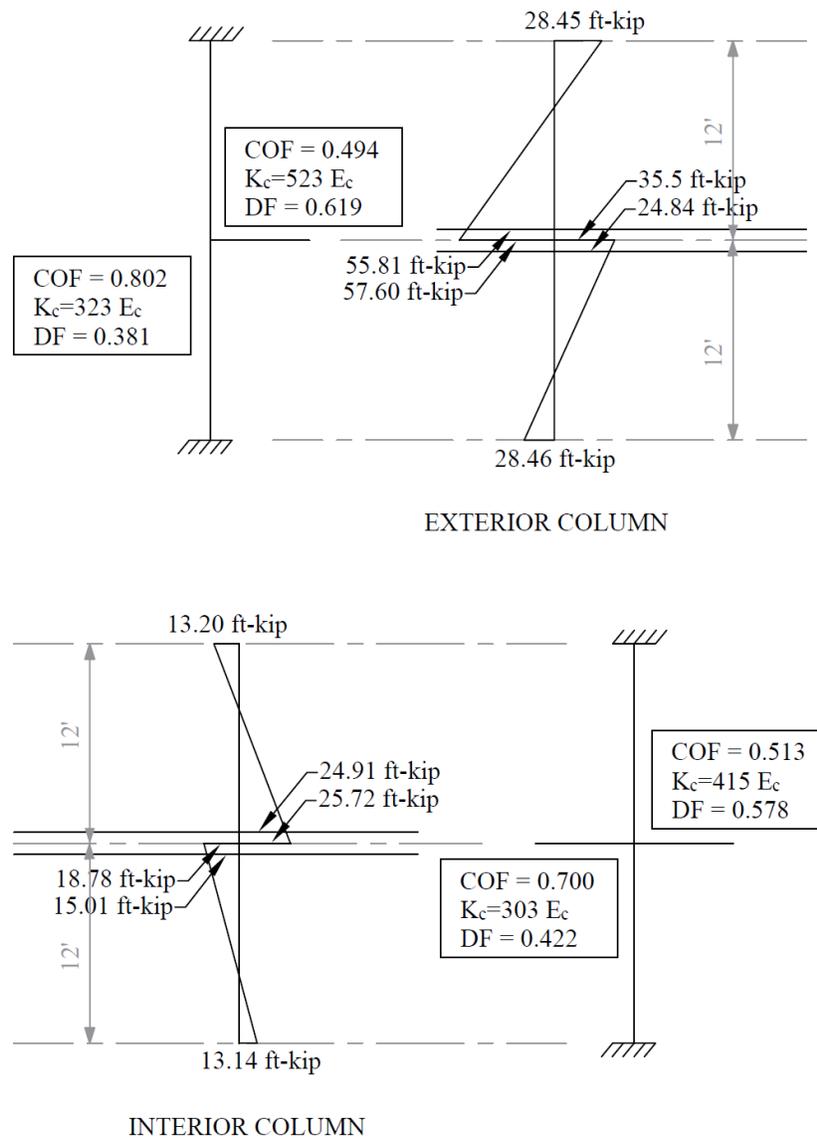


Figure 16 - Column Moments (Unbalanced Moments from Slab-Beam)

In summary:

Design moment in exterior column = 55.81 ft-kip

Design moment in interior column = 24.91 ft-kip

The moments determined above are combined with the factored axial loads (for each story) and factored moments in the transverse direction for design of column sections. A detailed analysis to obtain the moment values at the face of interior, exterior, and corner columns from the unbalanced moment values can be found in the “[Two-Way Flat Plate Concrete Floor Slab Design](#)” example.

3. Design of Interior, Edge, and Corner Columns

The design of interior, edge, and corner columns is explained in the “[Two-Way Flat Plate Concrete Floor Slab Design](#)” example.

4. Two-Way Slab Shear Strength

Shear strength of the slab in the vicinity of columns/supports includes an evaluation of one-way shear (beam action) and two-way shear (punching) in accordance with ACI 318 Chapter 22.

4.1. One-Way (Beam action) Shear Strength

One-way shear is critical at a distance d from the face of the column. Figure 17 shows the V_u at the critical sections around each column. Since there is no shear reinforcement, the design shear capacity of the section equals to the design shear capacity of the concrete:

$$\phi V_n = \phi V_c + \phi V_s = \phi V_c \quad \text{ACI 318-14 (Eq. 22.5.1.1)}$$

Where:

$$\phi V_c = \phi 2\lambda \sqrt{f'_c} b_w d \quad \text{ACI 318-14 (Eq. 22.5.5.1)}$$

$\lambda = 1$ for normal weight concrete

$$\phi V_c = 0.75 \times 2 \times 1.0 \times \sqrt{4000} \times (22 \times 12 - 14) \times \frac{5}{1000} = 118.59 \text{ kips}$$

Because $\phi V_c > V_u$ at all the critical sections, the slab is **o.k.** in one-way shear.

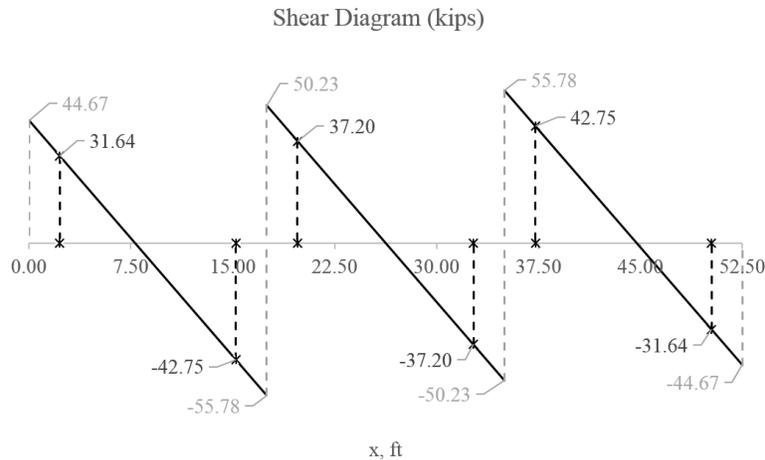


Figure 17 – One-way shear at critical sections (at distance d from the face of the supporting column)

4.2. Two-Way (Punching) Shear Strength

Two-way shear is critical on a rectangular section located at $d_{slab}/2$ away from the face of the column. The factored shear force V_u in the critical section is calculated as the reaction at the centroid of the critical section minus the self-weight and any superimposed surface dead and live load acting within the critical section.

The factored unbalanced moment used for shear transfer, M_{unb} , is calculated as the sum of the joint moments to the left and right. Moment of the vertical reaction with respect to the centroid of the critical section is also taken into account.

For the exterior column:

$$V_u = 44.67 - 0.340 \left(\frac{20.5 \times 23}{144} \right) = 43.56 \text{ kips}$$

$$M_{unb} = 93.1 - 43.56 \left(\frac{20.5 - 9.09 - 18/2}{12} \right) = 84.37 \text{ ft-kip}$$

For the exterior column in Figure 18, the location of the centroidal axis z - z is:

$$c_{AB} = \frac{\text{moment of area of the sides about AB}}{\text{area of the sides}}$$

$$c_{AB} = \frac{2(14 \times 26 \times (6.5 + 14/2)) + 6.5 \times 5 \times (6.5/2)}{2 \times (14 \times 26 + 6.5 \times 5) + 14 \times 19 + 2 \times 4.5 \times 5} = 9.09 \text{ in.}$$

$$A_c = 2 \times (14 \times 26 + 6.5 \times 5) + 14 \times 19 + 2 \times 4.5 \times 5 = 1104 \text{ in.}^2$$

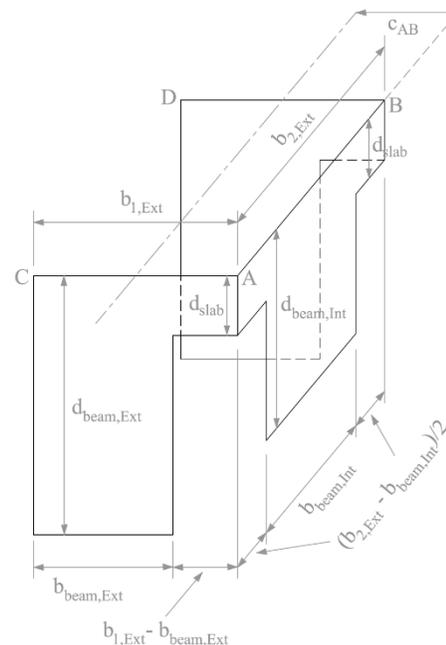


Figure 18 – Critical section of exterior support of interior frame

The polar moment J_c of the shear perimeter is:

$$J_c = 2 \left[\frac{b_{beam,Ext} d_{beam,Ext}^3}{12} + \frac{d_{beam,Ext} b_{beam,Ext}^3}{12} + [b_{beam,Ext} d_{beam,Ext}] \left[\frac{b_{beam,Ext}}{2} + (b_1 - b_{beam,Ext}) - c_{AB} \right]^2 \right]$$

$$+ 2 \left[\frac{(b_1 - b_{beam,Ext}) d_{slab,Ext}^3}{12} + \frac{d_{slab} (b_1 - b_{beam,Ext})^3}{12} + [(b_1 - b_{beam,Ext}) d_{slab}] \left[c_{AB} - \frac{b_1 - b_{beam,Ext}}{2} \right]^2 \right]$$

$$+ [b_{beam,Int} d_{beam,Int} + (b_2 - b_{beam,Int}) d_{slab}] c_{AB}^2$$

$$J_c = 2 \left[\frac{14 \times 26^3}{12} + \frac{26 \times 14^3}{12} + [14 \times 26] \left[\frac{14}{2} + (20.5 - 14) - 9.09 \right]^2 \right]$$

$$+ 2 \left[\frac{(20.5 - 14) \times 5^3}{12} + \frac{5 \times (20.5 - 14)^3}{12} + [(20.5 - 14) \times 5] \left[9.09 - \frac{20.5 - 14}{2} \right]^2 \right]$$

$$+ [14 \times 19 + (23 - 14) \times 5] \times 9.09^2$$

$$J_c = 95,338 \text{ in.}^4$$

$$\gamma_v = 1 - \gamma_f = 1 - 0.614 = 0.386$$

ACI 318-14 (Eq. 8.4.4.2.2)

The length of the critical perimeter for the exterior column:

$$b_o = 2 \times (18 + 5/2) + (18 + 5) = 64 \text{ in.}$$

$$v_u = \frac{V_u}{A_c} + \frac{\gamma_v M_{unb} c_{AB}}{J_c}$$

ACI 318-14 (R.8.4.4.2.3)

$$v_u = \frac{43.56 \times 1000}{1104} + \frac{0.386 \times 84.37 \times 12 \times 1000 \times 9.09}{95,338} = 76.8 \text{ psi}$$

$$v_c = \min \left[4\lambda\sqrt{f'_c}, \left(2 + \frac{4}{\beta} \right) \lambda\sqrt{f'_c}, \left(\frac{\alpha_s d}{b_o} + 2 \right) \lambda\sqrt{f'_c} \right]$$

ACI 318-14 (Table 22.6.5.2)

$$v_c = \min \left[4 \times 1 \times \sqrt{4000}, \left(2 + \frac{4}{1} \right) \times 1 \times \sqrt{4000}, \left(\frac{30 \times 5}{64} + 2 \right) \times 1 \times \sqrt{4000} \right]$$

$$v_c = \min [253, 379.5, 274.7] \text{ psi} = 253 \text{ psi}$$

$$\phi v_c = 0.75 \times 253 = 189.7 \text{ psi} > v_u = 76.8 \text{ psi}$$

O.K.

For the interior column:

$$V_u = 55.78 + 50.23 - 0.340 \left(\frac{23 \times 23}{144} \right) = 104.76 \text{ kips}$$

$$M_{umb} = 167.7 - 153.6 - 104.76(0) = 14.10 \text{ ft-kip}$$

For the interior column in Figure 19, the location of the centroidal axis z-z is:

$$c_{AB} = \frac{b_{1,Int}}{2} = \frac{23}{2} = 11.5 \text{ in.}$$

$$A_c = 4 \times (14 \times 19 + 9 \times 5) = 1244 \text{ in.}^2$$

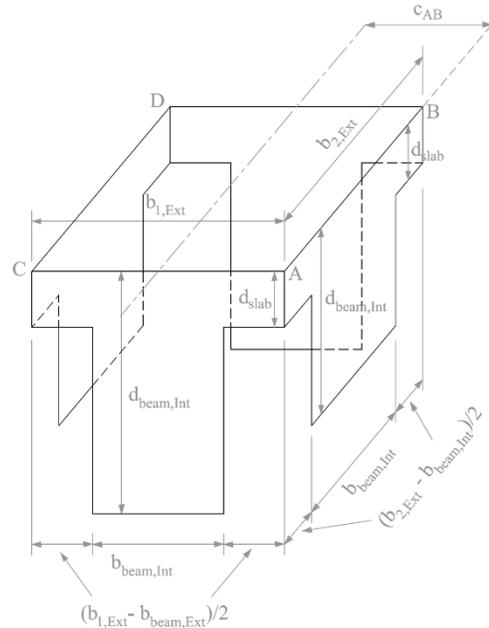


Figure 19 – Critical section of interior support of interior frame

The polar moment J_c of the shear perimeter is:

$$J_c = 2 \left[\frac{b_{beam,Int} d_{beam,Int}^3}{12} + \frac{d_{beam,Int} b_{beam,Int}^3}{12} + [b_{beam,Int} d_{beam,Int}] \left[\frac{b_{beam,Int}}{2} + \left(\frac{b_1 - b_{beam,Int}}{2} \right) - c_{AB} \right]^2 \right]$$

$$+ 4 \left[\frac{\left(\frac{b_1 - b_{beam,Int}}{2} \right) d_{slab}^3}{12} + \frac{d_{slab} \left(\frac{b_1 - b_{beam,Int}}{2} \right)^3}{12} + \left[\left(\frac{b_1 - b_{beam,Int}}{2} \right) d_{slab} \right] \left[c_{AB} - \frac{b_1 - b_{beam,Int}}{2 \times 2} \right]^2 \right]$$

$$+ [b_{beam,Int} d_{beam,Int} + (b_2 - b_{beam,Int}) d_{slab}] c_{AB}^2$$

$$J_c = 2 \left[\frac{14 \times 19^3}{12} + \frac{19 \times 14^3}{12} + [14 \times 19] \left[\frac{14}{2} + \left(\frac{23 - 14}{2} \right) - 11.5 \right]^2 \right]$$

$$+ 4 \left[\frac{\left(\frac{23 - 14}{2} \right) \times 5^3}{12} + \frac{5 \times \left(\frac{23 - 14}{2} \right)^3}{12} + \left[\left(\frac{23 - 14}{2} \right) \times 5 \right] \left[11.5 - \frac{23 - 14}{2 \times 2} \right]^2 \right]$$

$$+ [14 \times 19 + (23 - 14) \times 5] \times 11.5^2$$

$$J_c = 114,993 \text{ in.}^4$$

$$\gamma_v = 1 - \gamma_f = 1 - 0.600 = 0.400$$

ACI 318-14 (Eq. 8.4.4.2.2)

The length of the critical perimeter for the exterior column:

$$b_o = 4 \times (18 + 5) = 92 \text{ in.}$$

$$v_u = \frac{V_u}{A_c} + \frac{\gamma_v M_{\text{unb}} C_{AB}}{J_c}$$

$$v_u = \frac{104.76 \times 1000}{1244} + \frac{0.4 \times 14.10 \times 12 \times 1000 \times 11.5}{114,993} = 91.0 \text{ psi}$$

$$v_c = \min \left[4\lambda\sqrt{f'_c}, \left(2 + \frac{4}{\beta} \right) \lambda\sqrt{f'_c}, \left(\frac{\alpha_s d}{b_o} + 2 \right) \lambda\sqrt{f'_c} \right]$$

ACI 318-14 (Table 22.6.5.2)

$$v_c = \min \left[4 \times 1 \times \sqrt{4000}, \left(2 + \frac{4}{1} \right) \times 1 \times \sqrt{4000}, \left(\frac{40 \times 5}{92} + 2 \right) \times 1 \times \sqrt{4000} \right]$$

$$v_c = \min [253, 379.5, 274.7] \text{ psi} = 253 \text{ psi}$$

$$\phi v_c = 0.75 \times 253 = 189.7 \text{ psi} > v_u = 91.0 \text{ psi}$$

O.K.

5. Two-Way Slab Deflection Control (Serviceability Requirements)

Since the slab thickness was selected based on the minimum slab thickness tables in ACI 318-14, the deflection calculations are not required. However, the calculations of immediate and time-dependent deflections are covered in this section for illustration and comparison with [spSlab](#) model results.

5.1. Immediate (Instantaneous) Deflections

The calculation of deflections for two-way slabs is challenging even if linear elastic behavior can be assumed. Elastic analysis for three service load levels (D , $D + L_{\text{sustained}}$, $D + L_{\text{Full}}$) is used to obtain immediate deflections of the two-way slab in this example. However, other procedures may be used if they result in predictions of deflection in reasonable agreement with the results of comprehensive tests. ACI 318-14 (24.2.3)

The effective moment of inertia (I_e) is used to account for the cracking effect on the flexural stiffness of the slab. I_e for uncracked section ($M_{cr} > M_a$) is equal to I_g . When the section is cracked ($M_{cr} < M_a$), then the following equation should be used:

$$I_e = \left(\frac{M_{cr}}{M_a} \right)^3 I_g + \left[1 - \left(\frac{M_{cr}}{M_a} \right)^3 \right] I_{cr} \leq I_g$$

ACI 318-14 (Eq. 24.2.3.5a)

Where:

M_a = Maximum moment in member due to service loads at stage deflection is calculated.

The values of the maximum moments for the three service load levels are calculated from structural analysis as shown previously in this document. These moments are shown in Figure 20.

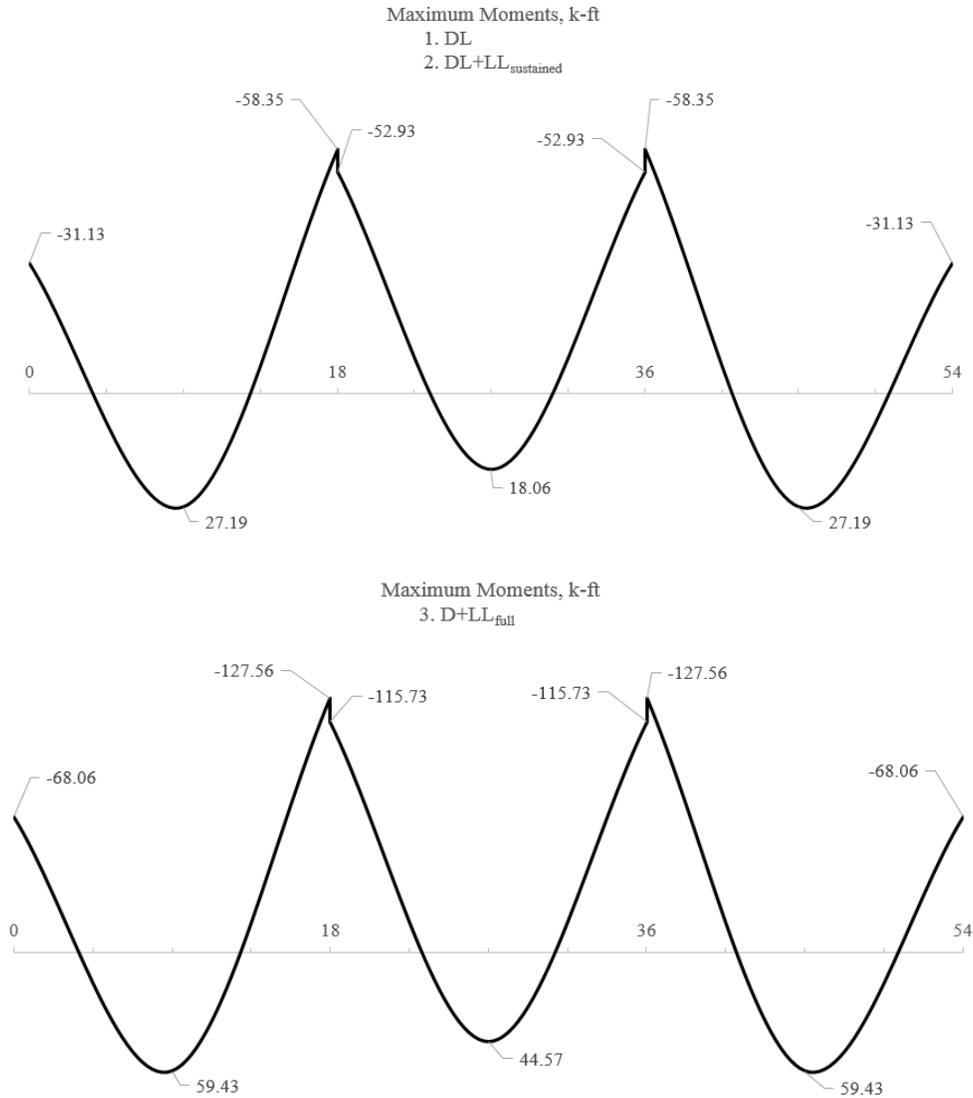


Figure 20 – Maximum Moments for the Three Service Load Levels

For positive moment (midspan) section of the exterior span:

M_{cr} = Cracking moment.

$$M_{cr} = \frac{f_r I_g}{y_t} = \frac{474.3 \times 25395}{5} \times \frac{1}{12 \times 1000} = 63.14 \text{ ft-kips} \quad \text{ACI 318-14 (Eq. 24.2.3.5b)}$$

f_r = Modulus of rupture of concrete.

$$f_r = 7.5 \lambda \sqrt{f'_c} = 7.5 \times 1.0 \times \sqrt{4000} = 474.3 \text{ psi} \quad \text{ACI 318-14 (Eq. 19.2.3.1)}$$

I_g = Moment of inertia of the gross uncracked concrete section.

$$I_g = 25395 \text{ in.}^2 \text{ for T-section (see Figure 21)}$$

y_t = Distance from centroidal axis of gross section, neglecting reinforcement, to tension face, in.

$y_t = 15.9$ in. (see Figure 21)

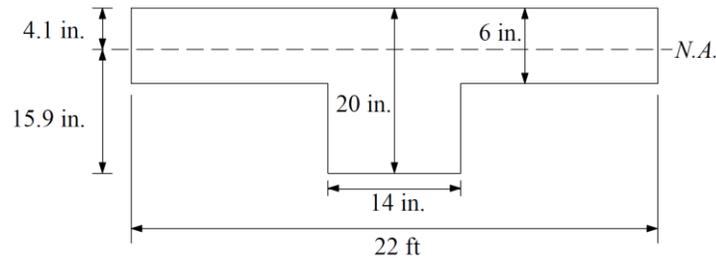


Figure 21 – I_g calculations for slab section near support

I_{cr} = Moment of inertia of the cracked section transformed to concrete. **PCA Notes on ACI 318-11 (9.5.2.2)**

As calculated previously, the positive reinforcement for the end span frame strip is 22 #4 bars located at 1.0 in. along the slab section from the bottom of the slab and 4 #4 bars located at 1.75 in. along the beam section from the bottom of the beam. Five of the slab section bars are not continuous and will be excluded from the calculation of I_{cr} . Figure 22 shows all the parameters needed to calculate the moment of inertia of the cracked section transformed to concrete at midspan.

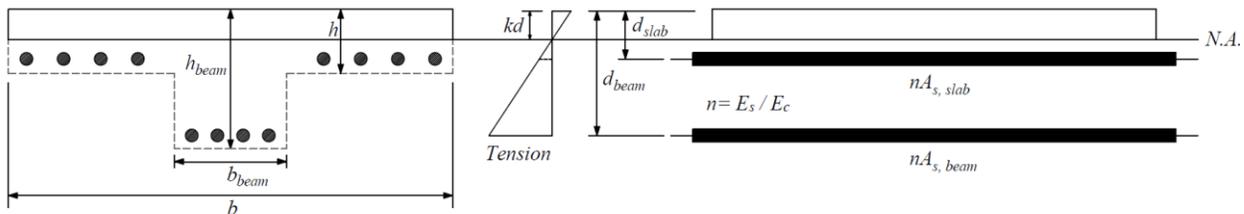


Figure 22 – Cracked Transformed Section (positive moment section)

E_{cs} = Modulus of elasticity of slab concrete.

$$E_{cs} = w_c^{1.5} 33 \sqrt{f'_c} = 150^{1.5} \times 33 \times \sqrt{4000} = 3834 \times 10^3 \text{ psi}$$

ACI 318-14 (19.2.2.1.a)

$$n = \frac{E_s}{E_{cs}} = \frac{29000000}{3834000} = 7.56$$

PCA Notes on ACI 318-11 (Table 10-2)

$$a = \frac{b}{2} = \frac{22 \times 12}{2} = 132 \text{ in.}$$

$$b = n A_{s,beam} + n A_{s,slab} = 7.56 \times (4 \times 0.20) + 7.56 \times (17 \times 0.20) = 31.77 \text{ in.}^2$$

$$c = -1 \times (n A_{s,beam} d_{s,beam} + n A_{s,slab} d_{s,slab}) = -1 \times (7.56 \times (4 \times 0.20) \times 18.25 + 7.56 \times (17 \times 0.20) \times 5.0) = -239 \text{ in.}^3$$

$$kd = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-31.77 \pm \sqrt{31.77^2 - 4 \times 132 \times -239}}{2 \times 132} = 3.999 \text{ in.}$$

$$I_{cr} = \frac{b(kd)^3}{3} + nA_{s,slab}(d_{slab} - kd)^2 + nA_{s,beam}(d_{beam} - kd)^2$$

$$I_{cr} = \frac{22 \times 12 \times (3.999)^3}{3} + 7.56 \times (17 \times 0.20)(5 - 3.999)^2 + 7.56 \times (4 \times 0.20)(18.25 - 3.999)^2 = 2282 \text{ in.}^4$$

For negative moment section (near the interior support of the end span):

The negative reinforcement for the end span frame strip near the interior support is 27 #4 bars located at 1.0 in. along the section from the top of the slab.

$$M_{cr} = \frac{f_r I_g}{y_t} = \frac{474.3 \times 9333}{10.0} \times \frac{1}{12 \times 1000} = 36.89 \text{ ft-kips}$$

ACI 318-14 (Eq. 24.2.3.5b)

$$f_r = 7.5 \lambda \sqrt{f'_c} = 7.5 \times 1.0 \times \sqrt{4000} = 474.3 \text{ psi}$$

ACI 318-14 (Eq. 19.2.3.1)

$$I_g = 9333 \text{ in.}^2$$

$$y_t = 10.0 \text{ in.}$$

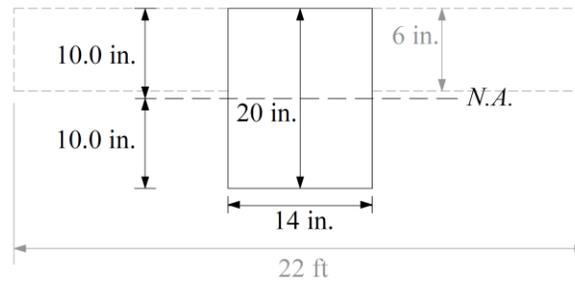


Figure 23 – I_g calculations for slab section near support

$$E_{cs} = w_c^{1.5} 33 \sqrt{f'_c} = 150^{1.5} \times 33 \times \sqrt{4000} = 3834 \times 10^3 \text{ psi}$$

ACI 318-14 (19.2.2.1.a)

$$n = \frac{E_s}{E_{cs}} = \frac{29000000}{3834000} = 7.56$$

PCA Notes on ACI 318-11 (Table 10-2)

$$B = \frac{b_{beam}}{n A_{s,total}} = \frac{14}{7.56 \times (27 \times 0.20)} = 0.34 \text{ in.}^{-1}$$

PCA Notes on ACI 318-11 (Table 10-2)

$$kd = \frac{\sqrt{2dB+1}-1}{B} = \frac{\sqrt{2 \times 19 \times 0.34+1}-1}{0.34} = 8.03 \text{ in.}$$

PCA Notes on ACI 318-11 (Table 10-2)

$$I_{cr} = \frac{b_{beam} (kd)^3}{3} + nA_{s,total} (d - kd)^2$$

PCA Notes on ACI 318-11 (Table 10-2)

$$I_{cr} = \frac{14 \times (8.03)^3}{3} + 7.56 \times (27 \times 0.20) (19 - 8.03)^2 = 7331 \text{ in.}^4$$

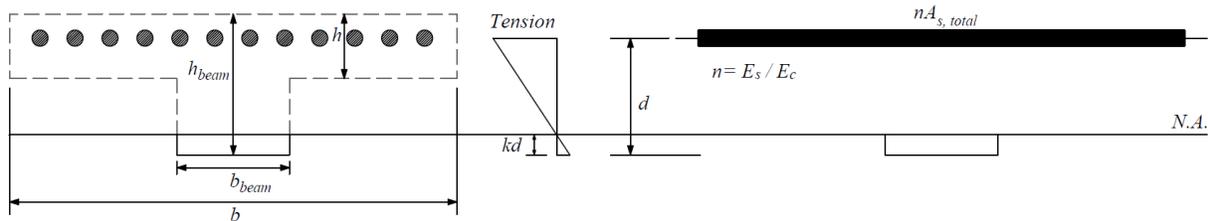


Figure 24 – Cracked Transformed Section (interior negative moment section for end span)

The effective moment of inertia procedure described in the Code is considered sufficiently accurate to estimate deflections. The effective moment of inertia, I_e , was developed to provide a transition between the upper and lower bounds of I_g and I_{cr} as a function of the ratio M_{cr}/M_a . For conventionally reinforced (nonprestressed) members, the effective moment of inertia, I_e , shall be calculated by Eq. (24.2.3.5a) unless obtained by a more comprehensive analysis.

I_e shall be permitted to be taken as the value obtained from Eq. (24.2.3.5a) at midspan for simple and continuous spans, and at the support for cantilevers. ACI 318-14 (24.2.3.7)

For continuous one-way slabs and beams, I_e shall be permitted to be taken as the average of values obtained from Eq. (24.2.3.5a) for the critical positive and negative moment sections. ACI 318-14 (24.2.3.6)

For the exterior span (span with one end continuous) with service load level ($D+LL_{full}$):

$$I_e^- = \left(\frac{M_{cr}}{M_a} \right)^3 I_g + \left[1 - \left(\frac{M_{cr}}{M_a} \right)^3 \right] I_{cr}, \text{ since } M_{cr} = 36.89 \text{ ft-kips} < M_a = 127.56 \text{ ft-kips}$$

ACI 318-14 (24.2.3.5a)

Where I_e^- is the effective moment of inertia for the critical negative moment section (near the support).

$$I_e^- = \left(\frac{36.89}{127.56} \right)^3 \times 9333 + \left[1 - \left(\frac{36.89}{127.56} \right)^3 \right] \times 7331 = 7380 \text{ in.}^4$$

$$I_e^+ = I_g = 25395 \text{ in.}^4, \text{ since } M_{cr} = 63.14 \text{ ft-kips} > M_a = 59.43 \text{ ft-kips}$$

Where I_e^+ is the effective moment of inertia for the critical positive moment section (midspan).

Since midspan stiffness (including the effect of cracking) has a dominant effect on deflections, midspan section is heavily represented in calculation of I_e and this is considered satisfactory in approximate deflection calculations. The averaged effective moment of inertia ($I_{e,avg}$) is given by:

$$I_{e,avg} = 0.85 I_e^+ + 0.15 I_e^- \text{ for end span} \quad \text{PCA Notes on ACI 318-11 (9.5.2.4(1))}$$

$$I_{e,avg} = 0.85 (25395) + 0.15 (7380) = 22693 \text{ in.}^4$$

Where:

I_e^- = The effective moment of inertia for the critical negative moment section near the support.

I_e^+ = The effective moment of inertia for the critical positive moment section (midspan).

For the interior span (span with both ends continuous) with service load level ($D+LL_{full}$):

$$I_e^- = \left(\frac{M_{cr}}{M_a} \right)^3 I_g + \left[1 - \left(\frac{M_{cr}}{M_a} \right)^3 \right] I_{cr}, \text{ since } M_{cr} = 36.89 \text{ ft-kips} < M_a = 115.73 \text{ ft-kips}$$

ACI 318-14 (24.2.3.5a)

$$I_e^- = \left(\frac{36.89}{115.73} \right)^3 \times 9333 + \left[1 - \left(\frac{36.89}{115.73} \right)^3 \right] \times 7331 = 7396 \text{ in.}^4$$

$$I_e^+ = I_g = 25395 \text{ in.}^4, \text{ since } M_{cr} = 63.14 \text{ ft-kips} > M_a = 44.57 \text{ ft-kips}$$

The averaged effective moment of inertia ($I_{e,avg}$) is given by:

$$I_{e,avg} = 0.70 I_e^+ + 0.15 (I_{e,l}^- + I_{e,r}^-) \text{ for interior span} \quad \text{PCA Notes on ACI 318-11 (9.5.2.4(2))}$$

$$I_{e,avg} = 0.70 (25395) + 0.15 (7396 + 7396) = 19995 \text{ in.}^4$$

Where:

$I_{e,l}^-$ = The effective moment of inertia for the critical negative moment section near the left support.

$I_{e,r}^-$ = The effective moment of inertia for the critical negative moment section near the right support.

Table 6 provides a summary of the required parameters and calculated values needed for deflections for exterior and interior equivalent frame. It also provides a summary of the same values for column strip and middle strip to facilitate calculation of panel deflection.

| Table 6 – Averaged Effective Moment of Inertia Calculations | | | | | | | | | | | | | |
|---|---------|------------------------------|------------------------------|----------------|----------------|----------------|------------------|--------------------------|----------------|----------------|------------------------------|----------------|----------------|
| For Frame Strip | | | | | | | | | | | | | |
| Span | zone | I_{gs} in. ⁴ | I_{cr} in. ⁴ | M_a , ft-kip | | | M_{cr} k-ft | I_{e} in. ⁴ | | | $I_{e,avg}$ in. ⁴ | | |
| | | | | D | D + LL_{Sus} | D + L_{full} | | D | D + LL_{Sus} | D + L_{full} | D | D + LL_{Sus} | D + L_{full} |
| Ext | Left | 9333 | 7147 | -30.61 | -30.61 | -66.92 | 36.89 | 9333 | 9333 | 7513 | 22761 | 22761 | 22693 |
| | Midspan | 25395 | 2282 | 27.19 | 27.19 | 59.43 | 63.14 | 25395 | 25395 | 25395 | | | |
| | Right | 9333 | 7331 | -58.35 | -58.35 | -127.56 | 36.89 | 7837 | 7837 | 7380 | | | |
| Int | Left | 9333 | 7331 | -52.93 | -52.93 | -115.73 | 36.89 | 8009 | 8009 | 7396 | 20179 | 20179 | 19995 |
| | Mid | 25395 | 1553 | 18.06 | 18.06 | 44.57 | 63.14 | 25395 | 25395 | 25395 | | | |
| | Right | 9333 | 7331 | -52.93 | -52.93 | -115.73 | 36.89 | 8009 | 8009 | 7396 | | | |

Deflections in two-way slab systems shall be calculated taking into account size and shape of the panel, conditions of support, and nature of restraints at the panel edges. For immediate deflections two-way slab systems the midpanel deflection is computed as the sum of deflection at midspan of the column strip or column line in one direction (Δ_{cx} or Δ_{cy}) and deflection at midspan of the middle strip in the orthogonal direction (Δ_{mx} or Δ_{my}). Figure 25 shows the deflection computation for a rectangular panel. The average Δ for panels that have different properties in the two direction is calculated as follows:

$$\Delta = \frac{(\Delta_{cx} + \Delta_{my}) + (\Delta_{cy} + \Delta_{mx})}{2}$$

PCA Notes on ACI 318-11 (9.5.3.4 Eq. 8)

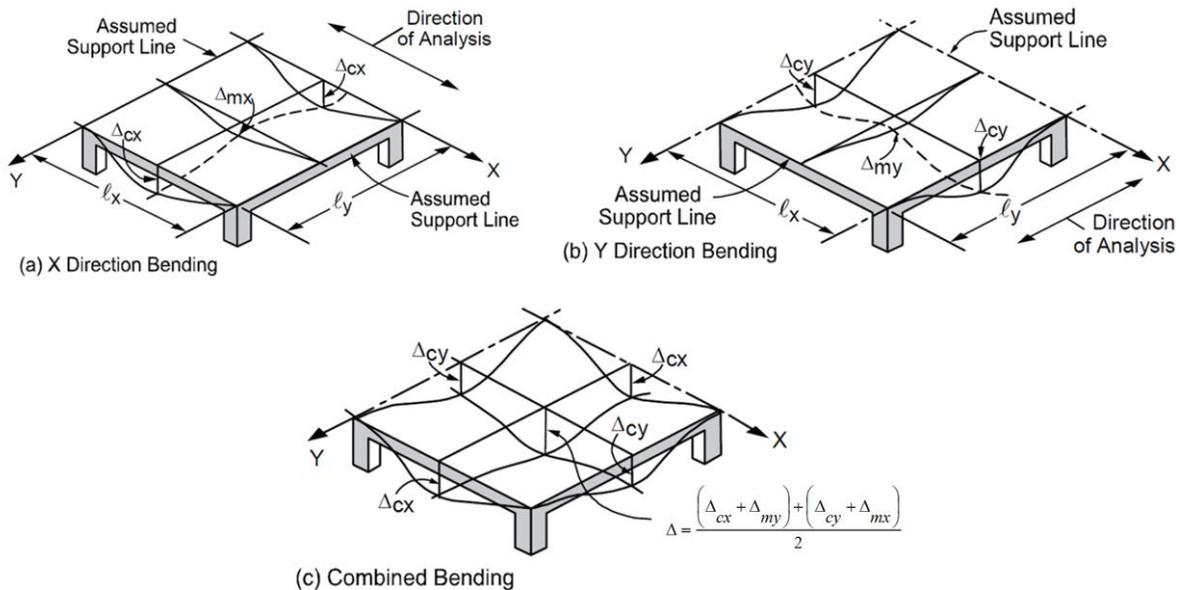


Figure 25 – Deflection Computation for a rectangular Panel

To calculate each term of the previous equation, the following procedure should be used. Figure 26 shows the procedure of calculating the term Δ_{cx} . same procedure can be used to find the other terms.

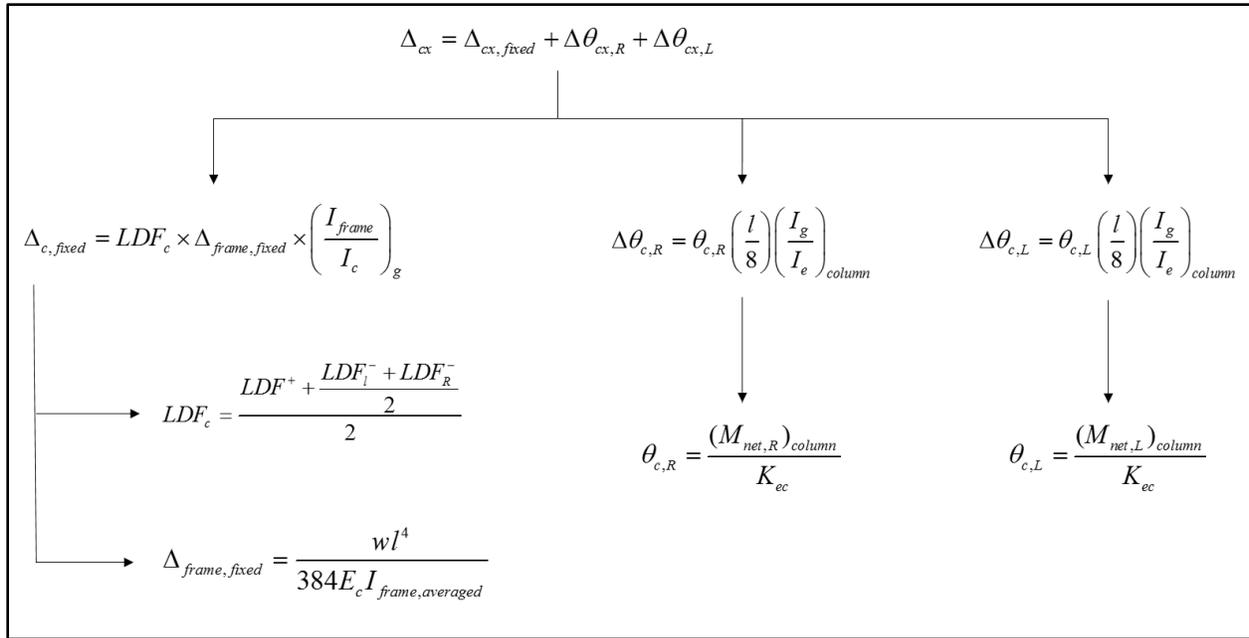


Figure 26 – Δ_{cx} calculation procedure

For exterior span - service dead load case:

$$\Delta_{frame, fixed} = \frac{wl^4}{384E_c I_{c, frame, averaged}}$$

PCA Notes on ACI 318-11 (9.5.3.4 Eq. 10)

Where:

$\Delta_{frame, fixed}$ = Deflection of column strip assuming fixed end condition.

$$w = \text{slab weight} + \text{beam weight} = \left(\frac{150 \times 6}{12} + \frac{150 \times (20 - 6) \times 14}{22 \times 144} \right) (22) = 1854 \text{ lb/ft}$$

$$E_c = w_c^{1.5} 33 \sqrt{f'_c} = 150^{1.5} \times 33 \times \sqrt{4000} = 3834 \times 10^3 \text{ psi}$$

ACI 318-14 (19.2.2.1.a)

$I_{frame, averaged}$ = The averaged effective moment of inertia ($I_{e, avg}$) for the frame strip for service dead load case from Table 6 = 22761 in.⁴

$$\Delta_{frame, fixed} = \frac{(1854)(17.5 - 18/12)^4 (12)^3}{384(3834 \times 10^3)(22761)} = 0.0063 \text{ in.}$$

$$\Delta_{c, fixed} = LDF_c \times \Delta_{frame, fixed} \times \left(\frac{I_{frame}}{I_c} \right)_g$$

PCA Notes on ACI 318-11 (9.5.3.4 Eq. 11)

Where LDF_c is the load distribution factor for the column strip. The load distribution factor for the column strip can be found from the following equation:

$$LDF_c = \frac{LDF^+ + \frac{LDF_l^- + LDF_R^-}{2}}{2}$$

And the load distribution factor for the middle strip can be found from the following equation:

$$LDF_m = 1 - LDF_c$$

For the end span, LDF for exterior negative region (LDF_L^-), interior negative region (LDF_R^-), and positive region (LDF_L^+) are 0.75, 0.67, and 0.67, respectively (From Table 2 of this document). Thus, the load distribution factor for the column strip for the end span is given by:

$$LDF_c = \frac{0.67 + \frac{0.75 + 0.67}{2}}{2} = 0.690$$

$I_{c,g}$ = The gross moment of inertia (I_g) for the column strip (for T section) = 20040 in.⁴

$I_{frame,g}$ = The gross moment of inertia (I_g) for the frame strip (for T section) = 25395 in.⁴

$$\Delta_{c, fixed} = 0.690 \times 0.0063 \times \frac{25395}{20040} = 0.0055 \text{ in.}$$

$$\theta_{c,L} = \frac{(M_{net,L})_{frame}}{K_{ec}}$$

PCA Notes on ACI 318-11 (9.5.3.4 Eq. 12)

Where:

$\theta_{c,L}$ = Rotation of the span left support.

$(M_{net,L})_{frame}$ = 31.13 ft-kips = Net frame strip negative moment of the left support.

K_{ec} = effective column stiffness for exterior column.
= 764 x E_c = 2929 x 10⁶ in.-lb (calculated previously).

$$\theta_{c,L} = \frac{31.13 \times 12 \times 1000}{2929 \times 10^6} = 0.00012 \text{ rad}$$

$$\Delta\theta_{c,L} = \theta_{c,L} \left(\frac{l}{8} \right) \left(\frac{I_g}{I_e} \right)_{frame}$$

PCA Notes on ACI 318-11 (9.5.3.4 Eq. 14)

Where:

$\Delta\theta_{c,L}$ = Midspan deflection due to rotation of left support.

$$\left(\frac{I_g}{I_e}\right)_{frame} = \text{Gross-to-effective moment of inertia ratio for frame strip.}$$

$$\Delta\theta_{c,L} = 0.00012 \times \frac{(17.5 - 18/12) \times 12}{8} \times \frac{25395}{22761} = 0.0033 \text{ in.}$$

$$\theta_{c,R} = \frac{(M_{net,R})_{frame}}{K_{ec}} = \frac{(58.35 - 52.93) \times 12 \times 1000}{2419 \times 10^6} = 0.00003 \text{ rad}$$

Where

$\theta_{c,R}$ = Rotation of the end span right support.

$(M_{net,R})_{frame}$ = Net frame strip negative moment of the right support.

K_{ec} = effective column stiffness for interior column.

= $631 \times E_c = 2419 \times 10^6$ in.-lb (calculated previously).

$$\Delta\theta_{c,R} = \theta_{c,R} \left(\frac{l}{8}\right) \left(\frac{I_g}{I_e}\right)_{frame} = 0.00003 \times \frac{(17.5 - 18/12) \times 12}{8} \times \frac{25395}{22761} = 0.00072 \text{ in.}$$

Where:

$\Delta\theta_{c,R}$ = Midspan deflection due to rotation of right support.

$$\Delta_{cx} = \Delta_{cx, fixed} + \Delta\theta_{cx,R} + \Delta\theta_{cx,L}$$

PCA Notes on ACI 318-11 (9.5.3.4 Eq. 9)

$$\Delta_{cx} = 0.0055 + 0.0033 + 0.00072 = 0.009 \text{ in.}$$

Following the same procedure, Δ_{mx} can be calculated for the middle strip. This procedure is repeated for the equivalent frame in the orthogonal direction to obtain Δ_{cy} , and Δ_{my} for the end and middle spans for the other load levels ($D+LL_{sus}$ and $D+LL_{full}$).

Assuming square panel, $\Delta_{cx} = \Delta_{cy} = 0.009$ in. and $\Delta_{mx} = \Delta_{my} = 0.021$ in.

The average Δ for the corner panel is calculated as follows:

$$\Delta = \frac{(\Delta_{cx} + \Delta_{my}) + (\Delta_{cy} + \Delta_{mx})}{2} = (\Delta_{cx} + \Delta_{my}) = (\Delta_{cy} + \Delta_{mx}) = 0.009 + 0.021 = 0.030 \text{ in.}$$

Table 7 - Instantaneous Deflections

| Column Strip | | | | | | | | | Middle Strip | | | | | | | |
|--------------|------|---------------------------------------|-----------------------------------|-------------------------------|-------------------------------|------------------------------------|------------------------------------|------------------------------|--------------|---------------------------------------|-----------------------------------|-------------------------------|-------------------------------|------------------------------------|------------------------------------|------------------------------|
| Span | LDF | D | | | | | | | LDF | D | | | | | | |
| | | $\Delta_{\text{frame-fixed}}$, in | $\Delta_{\text{c-fixed}}$, in | θ_{c1} , rad | θ_{c2} , rad | $\Delta\theta_{\text{c1}}$, in | $\Delta\theta_{\text{c2}}$, in | Δ_{cx} , in | | $\Delta_{\text{frame-fixed}}$, in | $\Delta_{\text{m-fixed}}$, in | θ_{m1} , rad | θ_{m2} , rad | $\Delta\theta_{\text{m1}}$, in | $\Delta\theta_{\text{m2}}$, in | Δ_{mx} , in |
| Ext | 0.69 | 0.0063 | 0.0055 | 0.00012 | 0.00003 | 0.0033 | 0.0007 | 0.009 | 0.31 | 0.0063 | 0.0172 | 0.00012 | 0.00003 | 0.0033 | 0.0007 | 0.021 |
| Int | 0.67 | 0.0071 | 0.0060 | 0.00003 | 0.00003 | -0.0008 | -0.0008 | 0.004 | 0.33 | 0.0071 | 0.0207 | 0.00003 | 0.00003 | -0.0008 | -0.0008 | 0.019 |
| Span | LDF | D+LL _{sus} | | | | | | | LDF | D+LL _{sus} | | | | | | |
| | | $\Delta_{\text{frame-fixed}}$, in | $\Delta_{\text{c-fixed}}$, in | θ_{c1} , rad | θ_{c2} , rad | $\Delta\theta_{\text{c1}}$, in | $\Delta\theta_{\text{c2}}$, in | Δ_{cx} , in | | $\Delta_{\text{frame-fixed}}$, in | $\Delta_{\text{m-fixed}}$, in | θ_{m1} , rad | θ_{m2} , rad | $\Delta\theta_{\text{m1}}$, in | $\Delta\theta_{\text{m2}}$, in | Δ_{mx} , in |
| Ext | 0.69 | 0.0063 | 0.0055 | 0.00012 | 0.00003 | 0.0033 | 0.0007 | 0.009 | 0.31 | 0.00627 | 0.01724 | 0.00012 | 0.00003 | 0.00330 | 0.00072 | 0.021 |
| Int | 0.67 | 0.0071 | 0.0060 | 0.00003 | 0.00003 | -0.0008 | -0.0008 | 0.004 | 0.33 | 0.00707 | 0.02069 | 0.00003 | 0.00003 | -0.00081 | -0.00081 | 0.019 |
| Span | LDF | D+LL _{full} | | | | | | | LDF | D+LL _{full} | | | | | | |
| | | $\Delta_{\text{frame-fixed}}$, in | $\Delta_{\text{c-fixed}}$, in | θ_{c1} , rad | θ_{c2} , rad | $\Delta\theta_{\text{c1}}$, in | $\Delta\theta_{\text{c2}}$, in | Δ_{cx} , in | | $\Delta_{\text{frame-fixed}}$, in | $\Delta_{\text{m-fixed}}$, in | θ_{m1} , rad | θ_{m2} , rad | $\Delta\theta_{\text{m1}}$, in | $\Delta\theta_{\text{m2}}$, in | Δ_{mx} , in |
| Ext | 0.69 | 0.0137 | 0.0120 | 0.00027 | 0.00006 | 0.0072 | 0.0016 | 0.021 | 0.31 | 0.01374 | 0.03780 | 0.00027 | 0.00006 | 0.00724 | 0.00158 | 0.047 |
| Int | 0.67 | 0.0156 | 0.0132 | 0.00006 | 0.00006 | -0.0018 | -0.0018 | 0.010 | 0.33 | 0.01559 | 0.04566 | 0.00006 | 0.00006 | -0.00179 | -0.00179 | 0.042 |
| Span | LDF | LL | LDF | LL | | | | | | | | | | | | |
| | | Δ_{cx} , in | | Δ_{mx} , in | | | | | | | | | | | | |
| Ext | 0.69 | 0.011 | 0.31 | 0.025 | | | | | | | | | | | | |
| Int | 0.67 | 0.005 | 0.33 | 0.023 | | | | | | | | | | | | |

5.2. Time-Dependent (Long-Term) Deflections (Δ_{lt})

The additional time-dependent (long-term) deflection resulting from creep and shrinkage (Δ_{cs}) may be estimated as follows:

$$\Delta_{cs} = \lambda_{\Delta} \times (\Delta_{sust})_{Inst} \quad \text{PCA Notes on ACI 318-11 (9.5.2.5 Eq. 4)}$$

The total time-dependent (long-term) deflection is calculated as:

$$(\Delta_{total})_{lt} = (\Delta_{sust})_{Inst} \times (1 + \lambda_{\Delta}) + [(\Delta_{total})_{Inst} - (\Delta_{sust})_{Inst}] \quad \text{CSA A23.3-04 (N9.8.2.5)}$$

Where:

$(\Delta_{sust})_{Inst}$ = Immediate (instantaneous) deflection due to sustained load, in.

$$\lambda_{\Delta} = \frac{\xi}{1 + 50\rho'} \quad \text{ACI 318-14 (24.2.4.1.1)}$$

$(\Delta_{total})_{lt}$ = Time-dependent (long-term) total deflection, in.

$(\Delta_{total})_{Inst}$ = Total immediate (instantaneous) deflection, in.

For the exterior span

$\xi = 2$, consider the sustained load duration to be 60 months or more. ACI 318-14 (Table 24.2.4.1.3)

$\rho' = 0$, conservatively.

$$\lambda_{\Delta} = \frac{2}{1 + 50 \times 0} = 2$$

$$\Delta_{cs} = 2 \times 0.009 = 0.019 \text{ in.}$$

$$(\Delta_{total})_{lt} = 0.009 \times (1 + 2) + (0.021 - 0.009) = 0.040 \text{ in.}$$

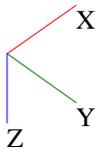
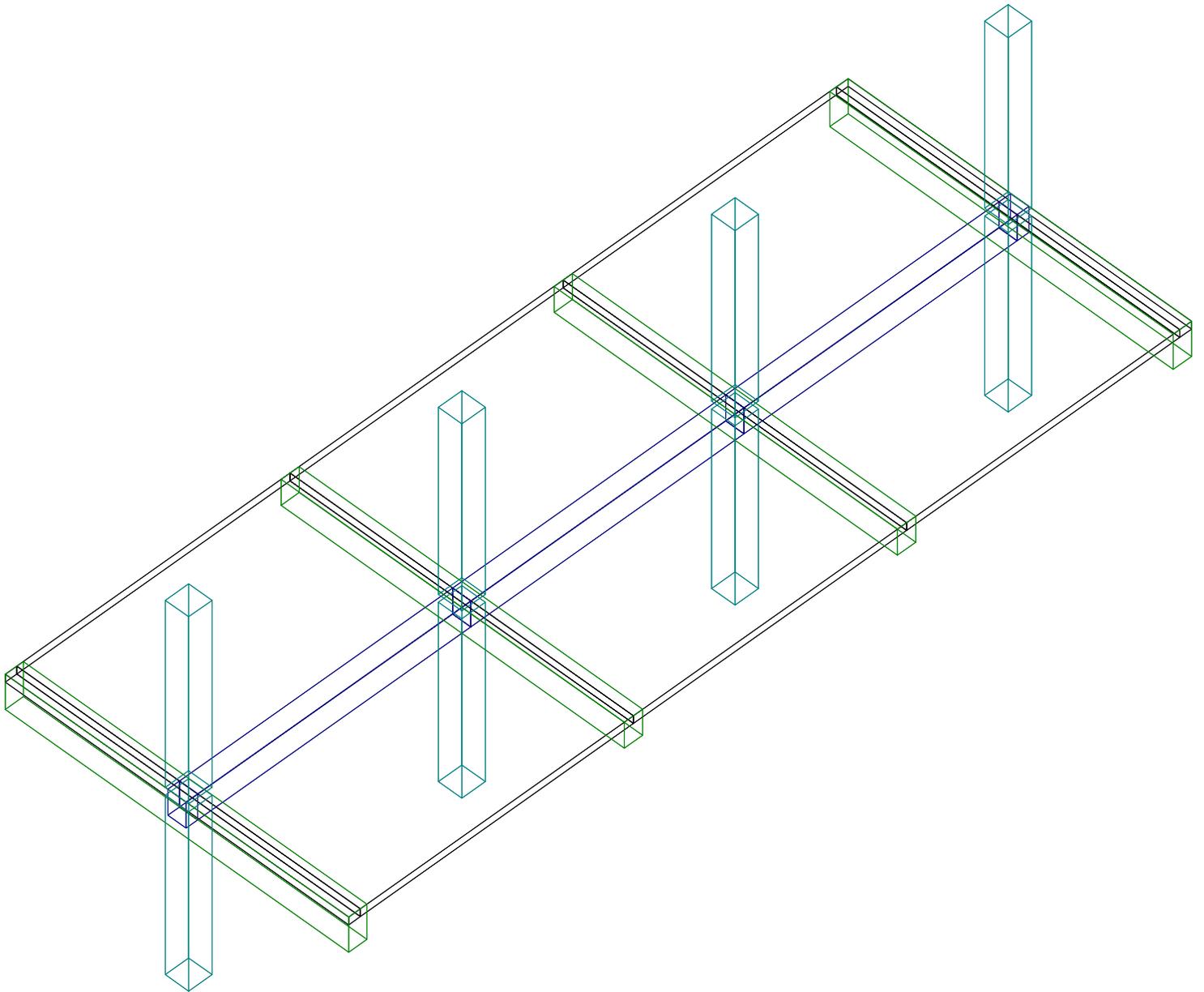
Table 8 shows long-term deflections for the exterior and interior spans for the analysis in the x-direction, for column and middle strips.

| Table 8 - Long-Term Deflections | | | | | |
|--|--|--------------------------------------|--|---|---|
| Column Strip | | | | | |
| Span | $(\Delta_{\text{sust}})_{\text{Inst}}$, in | λ_{Δ} | Δ_{cs}, in | $(\Delta_{\text{total}})_{\text{Inst}}$, in | $(\Delta_{\text{total}})_{\text{lt}}$, in |
| Exterior | 0.009 | 2.000 | 0.019 | 0.021 | 0.040 |
| Interior | 0.004 | 2.000 | 0.009 | 0.010 | 0.018 |
| Middle Strip | | | | | |
| Exterior | 0.021 | 2.000 | 0.043 | 0.047 | 0.089 |
| Interior | 0.019 | 2.000 | 0.038 | 0.042 | 0.080 |

6. spSlab Software Program Model Solution

[spSlab](#) program utilizes the Equivalent Frame Method described and illustrated in details here for modeling, analysis and design of two-way concrete floor slab systems. [spSlab](#) uses the exact geometry and boundary conditions provided as input to perform an elastic stiffness (matrix) analysis of the equivalent frame taking into account the torsional stiffness of the slabs framing into the column. It also takes into account the complications introduced by a large number of parameters such as vertical and torsional stiffness of transverse beams, the stiffening effect of drop panels, column capitals, and effective contribution of columns above and below the floor slab using the of equivalent column concept (*ACI 318-14 (R8.11.4)*).

[spSlab](#) Program models the equivalent frame as a design strip. The design strip is, then, separated by [spSlab](#) into column and middle strips. The program calculates the internal forces (Shear Force & Bending Moment), moment and shear capacity vs. demand diagrams for column and middle strips, instantaneous and long-term deflection results, and required flexural reinforcement for column and middle strips. The graphical and text results will be provided from the [spSlab](#) model in a future revision to this document. For a sample output refer to “[Two-Way Flat Plate Concrete Floor Slab Design](#)” example.



spSlab v5.00. Licensed to: StructurePoint. License ID: 66184-1055152-4-2C6B6-2C6B6

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Project: Two-Way Slab With Beams Spanning Between Supports

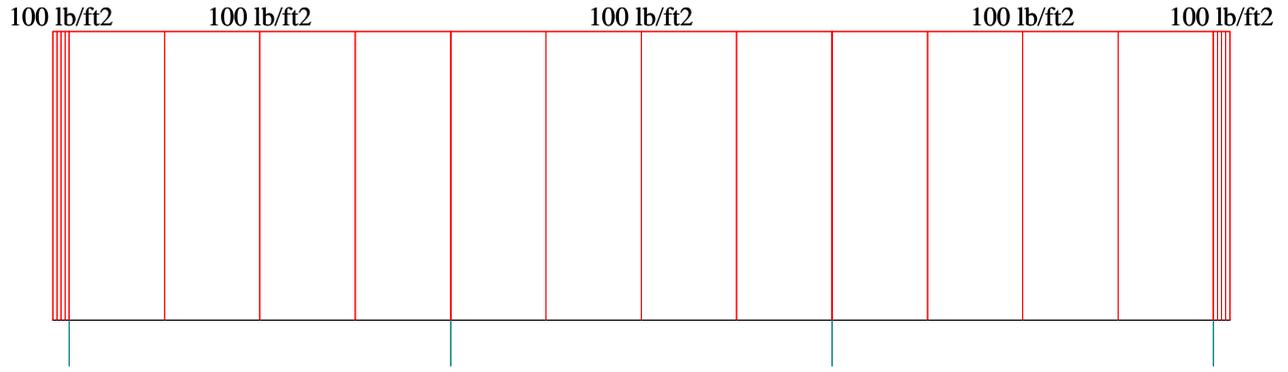
Frame: Interior Frame

Engineer: SP

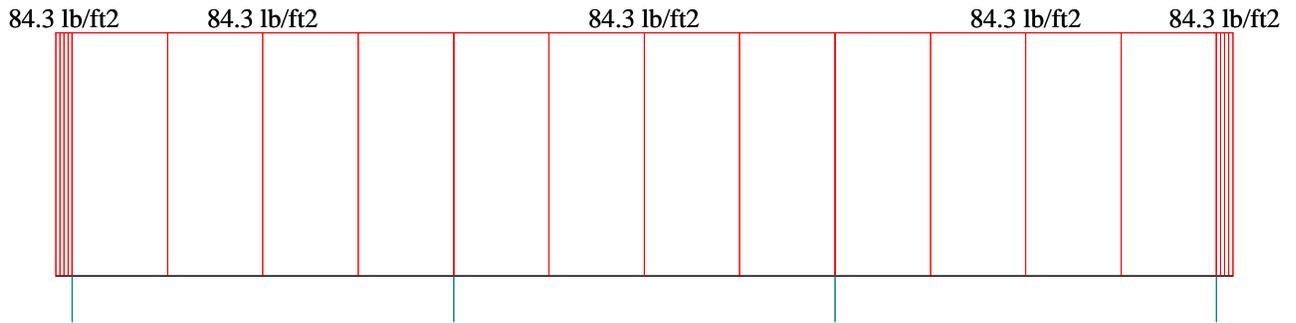
Code: ACI 318-14

Date: 03/31/17

Time: 14:47:17



CASE/PATTERN: Live/All



spSlab v5.00. Licensed to: StructurePoint. License ID: 66184-1055152-4-2C6B6-2C6B6

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Project: Two-Way Slab With Beams Spanning Between Supports

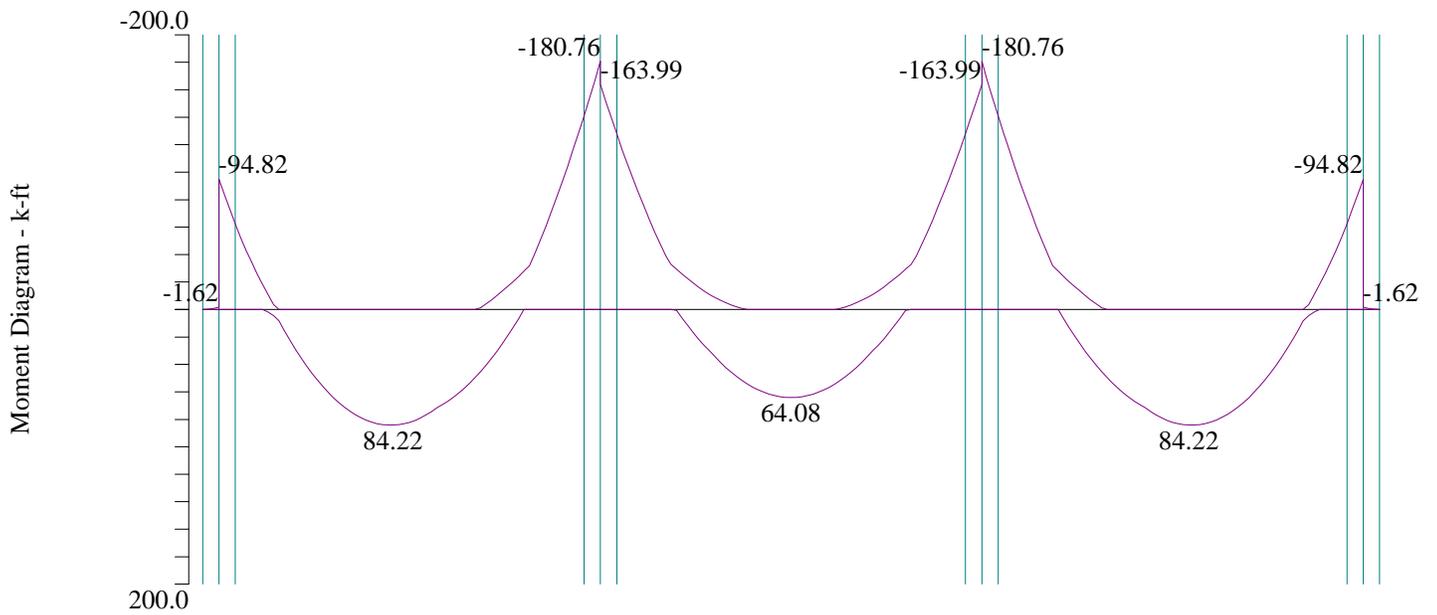
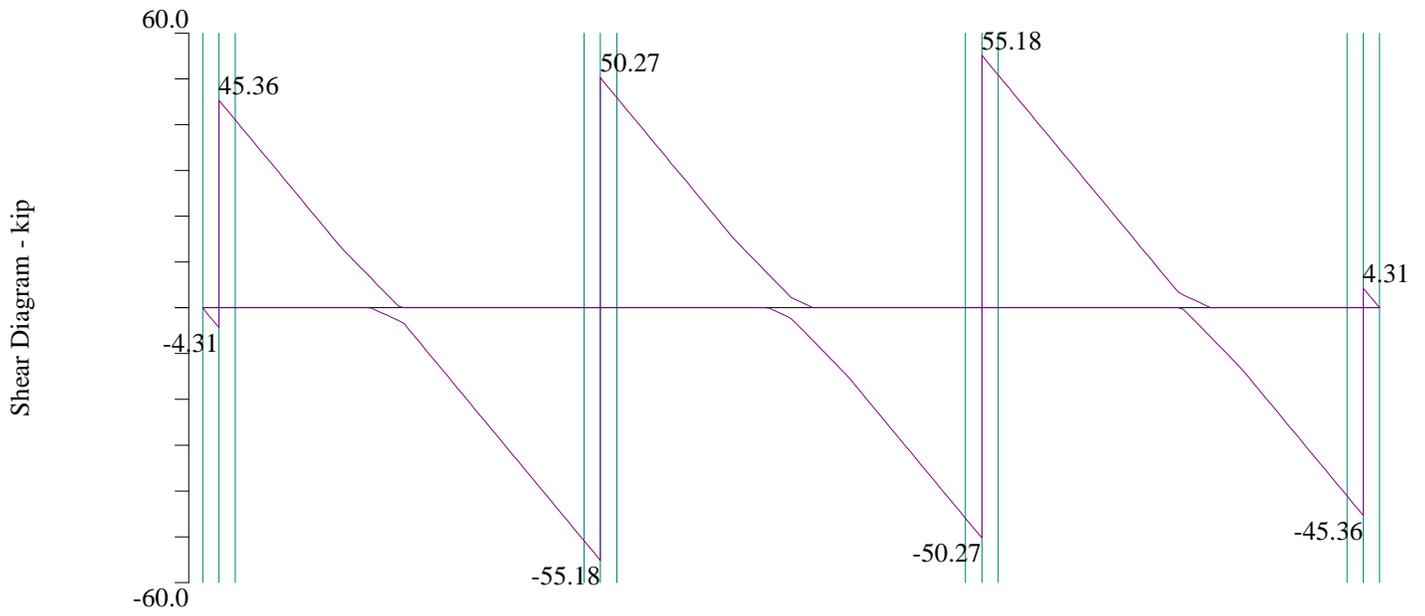
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Engineer: SP

Code: ACI 318-14

Date: 03/31/17

Time: 14:48:17



spSlab v5.00. Licensed to: StructurePoint. License ID: 66184-1055152-4-2C6B6-2C6B6

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Project: Two-Way Slab With Beams Spanning Between Supports

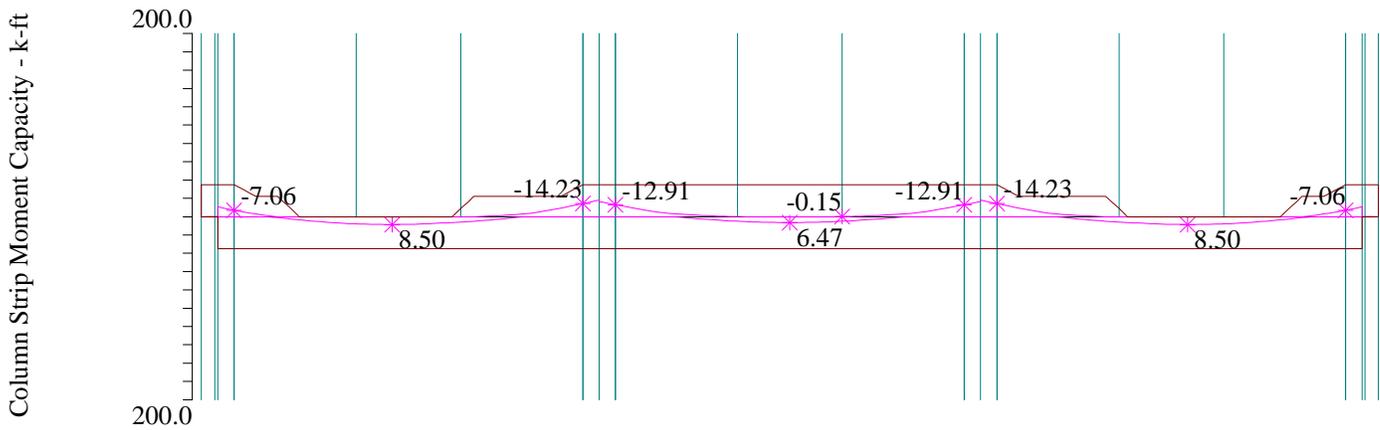
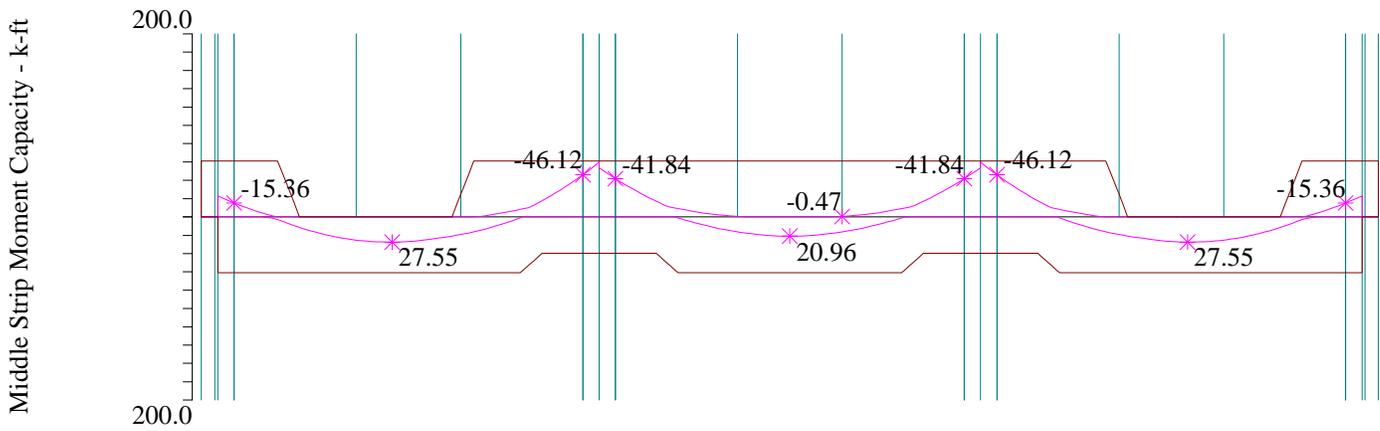
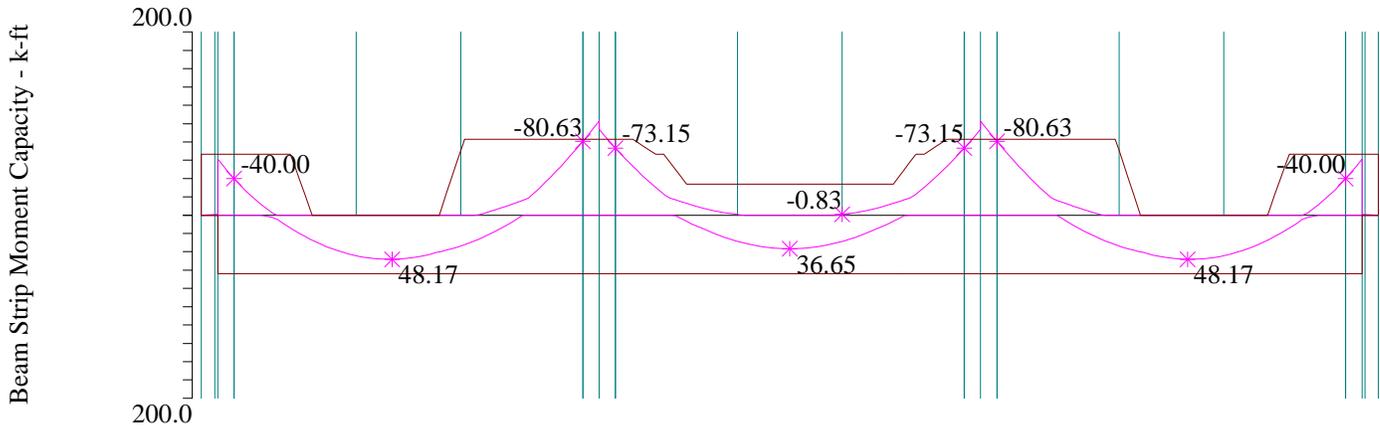
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Engineer: SP

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Project: Two-Way Slab With Beams Spanning Between Supports

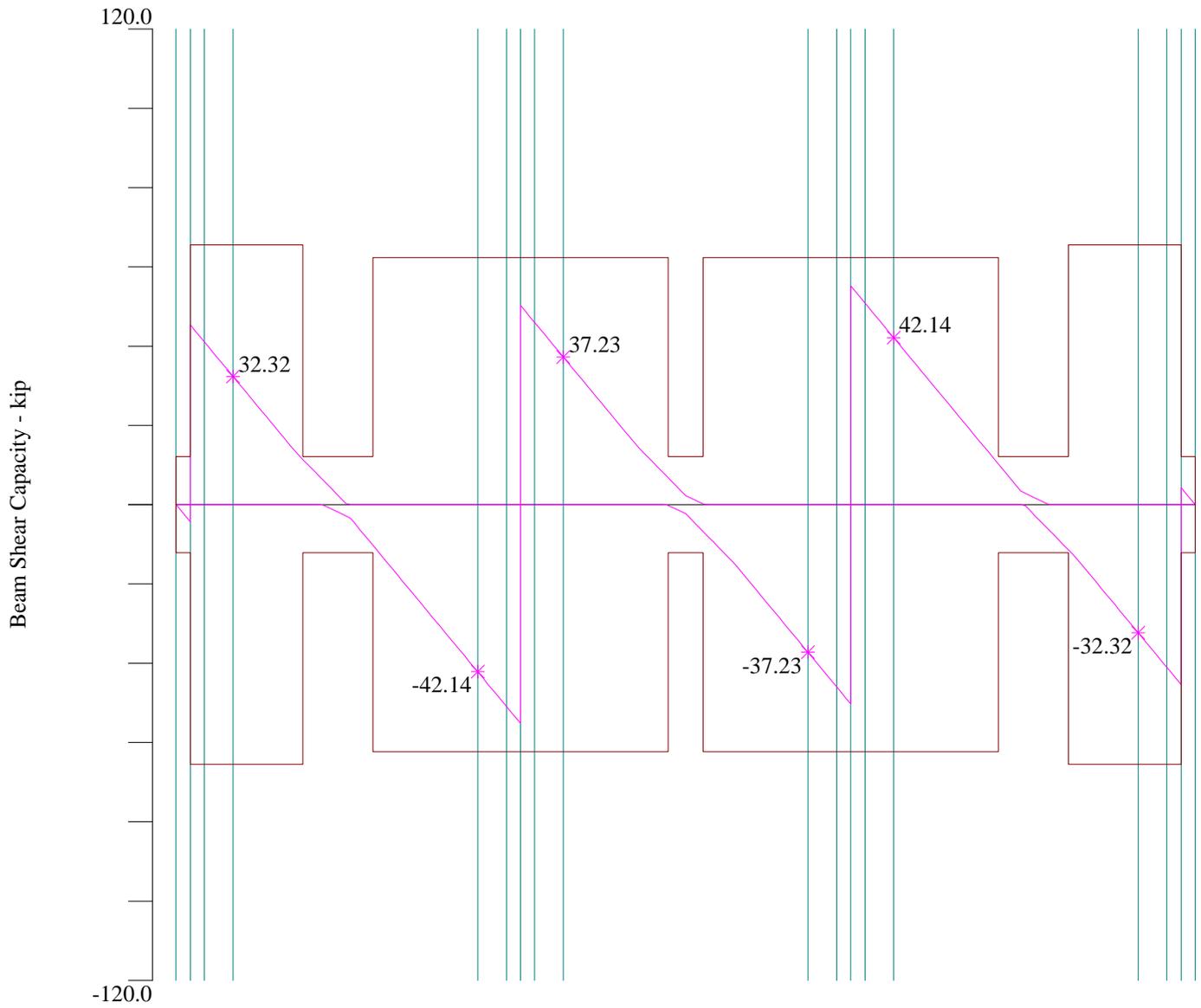
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Engineer: SP

Code: ACI 318-14

Date: 03/31/17

Time: 14:51:28



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Project: Two-Way Slab With Beams Spanning Between Supports

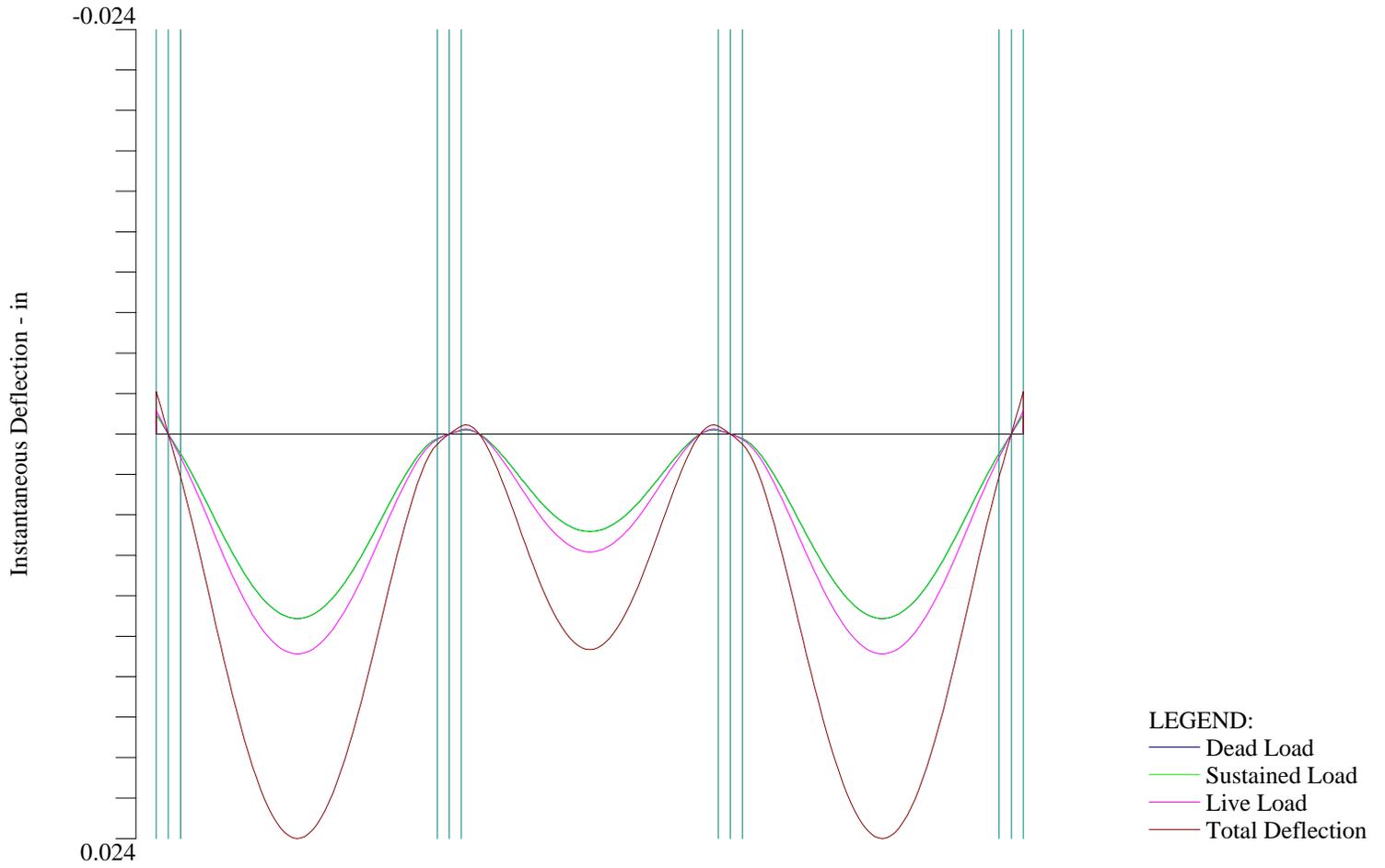
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Code: ACI 318-14

Date: 03/31/17

Time: 14:54:08



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Project: Two-Way Slab With Beams Spanning Between Supports

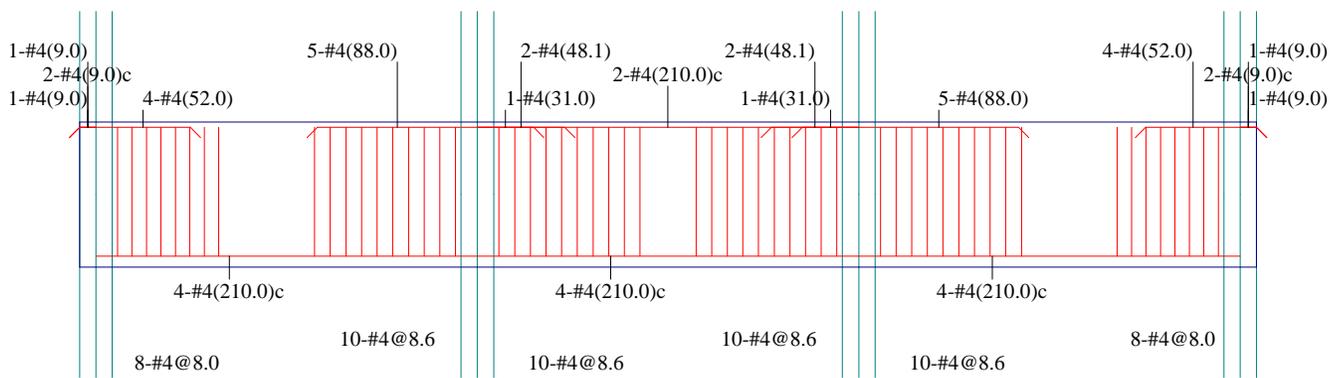
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Engineer: SP

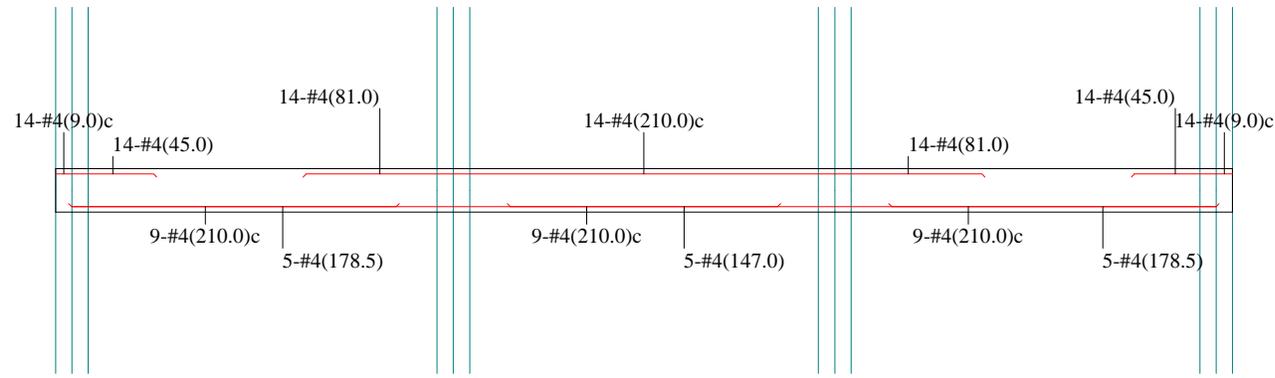
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Date: 03/31/17

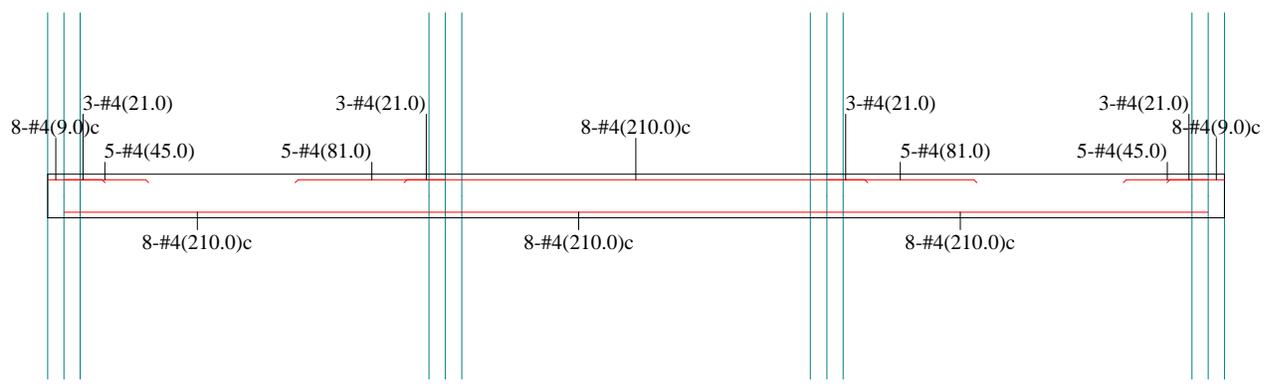
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Beam Strip Flexural and Transverse Reinforcement



Middle Strip Flexural Reinforcement



Column Strip Flexural Reinforcement

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File: C:\TSDA\TSDA-spSlab-Two-Way Slab with Beams Spanning Between Supports.slb

Project: Two-Way Slab With Beams Spanning Between Supports

Frame: Interior Frame

Engineer: SP

Code: ACI 318-14

Date: 03/31/17

Time: 14:56:22

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    oooooo   oo   oooooo   ooo   oooooo   o   oooooo   (TM)
    
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=====
                        spSlab v5.00 (TM)
    A Computer Program for Analysis, Design, and Investigation of
    Reinforced Concrete Beams, One-way and Two-way Slab Systems
    Copyright © 2003-2015, STRUCTUREPOINT, LLC
    All rights reserved
=====
    
```

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[1] INPUT ECHO
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General Information
 =====

File name: C:\TSDA\TSDA-spSlab-Two-Way Slab with Beams Spanning Between Supports.slb
 Project: Two-Way Slab With Beams Spanning Between Supports
 Frame: Interior Frame
 Engineer: SP
 Code: ACI 318-14
 Reinforcement Database: ASTM A615
 Mode: Design
 Number of supports = 4 + Left cantilever + Right cantilever
 Floor System: Two-Way

Live load pattern ratio = 75%
 Minimum free edge distance for punching shear = 4 times slab thickness.
 Circular critical section around circular supports used (if possible).
 Deflections are based on cracked section properties.
 In negative moment regions, Ig and Mcr DO NOT include flange/slab contribution (if available)
 Long-term deflections are calculated for load duration of 60 months.
 0% of live load is sustained.
 Compression reinforcement calculations NOT selected.
 Default incremental rebar design selected.
 User-defined slab strip widths NOT selected.
 User-defined distribution factors NOT selected.
 One-way shear in drop panel NOT selected.
 Distribution of shear to strips NOT selected.
 Beam T-section design NOT selected.
 Longitudinal beam contribution in negative reinforcement design over support NOT selected.
 Transverse beam contribution in negative reinforcement design over support NOT selected.

Material Properties
 =====

| | Slabs Beams | Columns |
|-----|-------------------------------------|-------------|
| wc | = 150 | 150 lb/ft3 |
| f'c | = 4 | 4 ksi |
| Ec | = 3834.3 | 3834.3 ksi |
| fr | = 0.47434 | 0.47434 ksi |
| fy | = 60 ksi, Bars are not epoxy-coated | |
| fyt | = 60 ksi | |
| Es | = 29000 ksi | |

Reinforcement Database
 =====

Units: Db (in), Ab (in^2), Wb (lb/ft)

| Size | Db | Ab | Wb | Size | Db | Ab | Wb |
|------|------|------|------|------|------|------|------|
| #3 | 0.38 | 0.11 | 0.38 | #4 | 0.50 | 0.20 | 0.67 |
| #5 | 0.63 | 0.31 | 1.04 | #6 | 0.75 | 0.44 | 1.50 |
| #7 | 0.88 | 0.60 | 2.04 | #8 | 1.00 | 0.79 | 2.67 |
| #9 | 1.13 | 1.00 | 3.40 | #10 | 1.27 | 1.27 | 4.30 |

| | | | | | | | |
|-----|------|------|-------|-----|------|------|------|
| #11 | 1.41 | 1.56 | 5.31 | #14 | 1.69 | 2.25 | 7.65 |
| #18 | 2.26 | 4.00 | 13.60 | | | | |

Span Data

=====

Slabs

Units: L1, wL, wR, L2L, L2R (ft); t, Hmin (in)

| Span | Loc | L1 | t | wL | wR | L2L | L2R | Hmin |
|------|-----|--------|------|--------|--------|--------|--------|-----------|
| 1 | Int | 0.750 | 6.00 | 11.000 | 11.000 | 22.000 | 22.000 | --- LC *i |
| 2 | Int | 17.500 | 6.00 | 11.000 | 11.000 | 22.000 | 22.000 | 5.81 |
| 3 | Int | 17.500 | 6.00 | 11.000 | 11.000 | 22.000 | 22.000 | 5.79 |
| 4 | Int | 17.500 | 6.00 | 11.000 | 11.000 | 22.000 | 22.000 | 5.81 |
| 5 | Int | 0.750 | 6.00 | 11.000 | 11.000 | 22.000 | 22.000 | --- RC *i |

NOTES:

Deflection check required for panels where code-specified Hmin for two-way construction doesn't apply due to:
 *i - cantilever end span (LC, RC) support condition

Ribs and Longitudinal Beams

Units: b, h, Sp (in)

| Span | Ribs | | | Beams | | |
|------|------|------|------|-------|-------|--------|
| | b | h | Sp | b | h | Offset |
| 1 | 0.00 | 0.00 | 0.00 | 14.00 | 20.00 | 0.00 |
| 2 | 0.00 | 0.00 | 0.00 | 14.00 | 20.00 | 0.00 |
| 3 | 0.00 | 0.00 | 0.00 | 14.00 | 20.00 | 0.00 |
| 4 | 0.00 | 0.00 | 0.00 | 14.00 | 20.00 | 0.00 |
| 5 | 0.00 | 0.00 | 0.00 | 14.00 | 20.00 | 0.00 |

Support Data

=====

Columns

Units: c1a, c2a, c1b, c2b (in); Ha, Hb (ft)

| Supp | c1a | c2a | Ha | c1b | c2b | Hb | Red% |
|------|-------|-------|--------|-------|-------|--------|------|
| 1 | 18.00 | 18.00 | 12.000 | 18.00 | 18.00 | 12.000 | 100 |
| 2 | 18.00 | 18.00 | 12.000 | 18.00 | 18.00 | 12.000 | 100 |
| 3 | 18.00 | 18.00 | 12.000 | 18.00 | 18.00 | 12.000 | 100 |
| 4 | 18.00 | 18.00 | 12.000 | 18.00 | 18.00 | 12.000 | 100 |

Transverse Beams

Units: b, h, Ecc (in)

| Supp | b | h | Ecc |
|------|-------|-------|-------|
| 1 | 14.00 | 27.00 | -2.00 |
| 2 | 14.00 | 20.00 | 0.00 |
| 3 | 14.00 | 20.00 | 0.00 |
| 4 | 14.00 | 27.00 | 2.00 |

Boundary Conditions

Units: Kz (kip/in); Kry (kip-in/rad)

| Supp | Spring Kz | Spring Kry | Far End A | Far End B |
|------|-----------|------------|-----------|-----------|
| 1 | 0 | 0 | Fixed | Fixed |
| 2 | 0 | 0 | Fixed | Fixed |
| 3 | 0 | 0 | Fixed | Fixed |
| 4 | 0 | 0 | Fixed | Fixed |

Load Data

=====

Load Cases and Combinations

| Case Type | Dead DEAD | Live LIVE |
|-----------|-----------|-----------|
| U1 | 1.200 | 1.600 |

Area Loads

Units: Wa (lb/ft2)

| Case/Patt | Span | Wa |
|-----------|------|--------|
| Dead | 1 | 84.30 |
| | 2 | 84.30 |
| | 3 | 84.30 |
| | 4 | 84.30 |
| | 5 | 84.30 |
| Live | 1 | 100.00 |
| | 2 | 100.00 |
| | 3 | 100.00 |
| | 4 | 100.00 |
| | 5 | 100.00 |

| | | |
|-----------|---|-------|
| Live/Odd | 1 | 75.00 |
| | 3 | 75.00 |
| | 5 | 75.00 |
| Live/Even | 2 | 75.00 |
| | 4 | 75.00 |
| Live/S1 | 1 | 75.00 |
| | 2 | 75.00 |
| Live/S2 | 2 | 75.00 |
| | 3 | 75.00 |
| Live/S3 | 3 | 75.00 |
| | 4 | 75.00 |
| Live/S4 | 4 | 75.00 |
| | 5 | 75.00 |

Reinforcement Criteria

=====

Slabs and Ribs

| | Top bars | | Bottom bars | | |
|-------------|----------|-------|-------------|-------|----|
| | Min | Max | Min | Max | |
| Bar Size | #4 | #8 | #4 | #8 | |
| Bar spacing | 1.00 | 18.00 | 1.00 | 18.00 | in |
| Reinf ratio | 0.14 | 5.00 | 0.14 | 5.00 | % |
| Cover | 0.75 | | 0.75 | | in |

There is NOT more than 12 in of concrete below top bars.

Beams

| | Top bars | | Bottom bars | | Stirrups | | |
|-------------|----------|-------|-------------|-------|----------|-------|----|
| | Min | Max | Min | Max | Min | Max | |
| Bar Size | #4 | #8 | #4 | #8 | #4 | #5 | |
| Bar spacing | 1.00 | 18.00 | 1.00 | 18.00 | 6.00 | 18.00 | in |
| Reinf ratio | 0.14 | 5.00 | 0.14 | 5.00 | | | % |
| Cover | 0.75 | | 1.51 | | | | in |
| Layer dist. | 1.00 | | 1.00 | | | | in |
| No. of legs | | | | | 2 | 6 | |
| Side cover | | | | | 1.50 | | in |
| 1st StIRRUP | | | | | 3.00 | | in |

There is NOT more than 12 in of concrete below top bars.

| | | | | | | | | | | | |
|----------|---------|-------|-------|--------|-------|--------|-------|--------|-------|----|----|
| Middle | Left | 13.25 | 15.36 | 0.750 | 1.717 | 14.360 | 0.688 | 11.357 | 14-#4 | *3 | *5 |
| | Midspan | 13.25 | 0.00 | 8.750 | 0.000 | 14.360 | 0.000 | 0.000 | --- | | |
| | Right | 13.25 | 46.12 | 16.750 | 1.717 | 14.360 | 2.099 | 11.357 | 14-#4 | *5 | |
| Beam | Left | 1.17 | 40.00 | 0.750 | 0.632 | 4.805 | 0.475 | 2.888 | 4-#4 | *3 | |
| | Midspan | 1.17 | 0.00 | 8.750 | 0.000 | 4.805 | 0.000 | 0.000 | --- | | |
| | Right | 1.17 | 80.63 | 16.750 | 0.887 | 4.805 | 0.975 | 2.166 | 5-#4 | | |
| 3 Column | Left | 7.58 | 12.91 | 0.750 | 0.983 | 8.218 | 0.580 | 11.375 | 8-#4 | *3 | *5 |
| | Midspan | 7.58 | 0.15 | 11.150 | 0.983 | 8.218 | 0.007 | 11.375 | 8-#4 | *3 | *5 |
| | Right | 7.58 | 12.91 | 16.750 | 0.983 | 8.218 | 0.580 | 11.375 | 8-#4 | *3 | *5 |
| Middle | Left | 13.25 | 41.84 | 0.750 | 1.717 | 14.360 | 1.900 | 11.357 | 14-#4 | *5 | |
| | Midspan | 13.25 | 0.47 | 11.150 | 1.717 | 14.360 | 0.021 | 11.357 | 14-#4 | *3 | *5 |
| | Right | 13.25 | 41.84 | 16.750 | 1.717 | 14.360 | 1.900 | 11.357 | 14-#4 | *5 | |
| Beam | Left | 1.17 | 73.15 | 0.750 | 0.887 | 4.805 | 0.881 | 2.166 | 5-#4 | *3 | |
| | Midspan | 1.17 | 0.83 | 11.150 | 0.372 | 4.805 | 0.010 | 8.664 | 2-#4 | *3 | |
| | Right | 1.17 | 73.15 | 16.750 | 0.887 | 4.805 | 0.881 | 2.166 | 5-#4 | *3 | |
| 4 Column | Left | 7.58 | 14.23 | 0.750 | 0.983 | 8.218 | 0.640 | 11.375 | 8-#4 | *3 | *5 |
| | Midspan | 7.58 | 0.00 | 8.750 | 0.000 | 8.218 | 0.000 | 0.000 | --- | | |
| | Right | 7.58 | 7.06 | 16.750 | 0.983 | 8.218 | 0.316 | 11.375 | 8-#4 | *3 | *5 |
| Middle | Left | 13.25 | 46.12 | 0.750 | 1.717 | 14.360 | 2.099 | 11.357 | 14-#4 | *5 | |
| | Midspan | 13.25 | 0.00 | 8.750 | 0.000 | 14.360 | 0.000 | 0.000 | --- | | |
| | Right | 13.25 | 15.36 | 16.750 | 1.717 | 14.360 | 0.688 | 11.357 | 14-#4 | *3 | *5 |
| Beam | Left | 1.17 | 80.63 | 0.750 | 0.887 | 4.805 | 0.975 | 2.166 | 5-#4 | | |
| | Midspan | 1.17 | 0.00 | 8.750 | 0.000 | 4.805 | 0.000 | 0.000 | --- | | |
| | Right | 1.17 | 40.00 | 16.750 | 0.632 | 4.805 | 0.475 | 2.888 | 4-#4 | *3 | |
| 5 Column | Left | 7.58 | 0.14 | 0.131 | 0.983 | 8.218 | 0.006 | 11.375 | 8-#4 | *3 | *5 |
| | Midspan | 7.58 | 0.06 | 0.348 | 0.983 | 8.218 | 0.003 | 11.375 | 8-#4 | *3 | *5 |
| | Right | 7.58 | 0.02 | 0.533 | 0.983 | 8.218 | 0.001 | 11.375 | 8-#4 | *3 | *5 |
| Middle | Left | 13.25 | 0.22 | 0.131 | 1.717 | 14.360 | 0.010 | 11.357 | 14-#4 | *3 | *5 |
| | Midspan | 13.25 | 0.10 | 0.348 | 1.717 | 14.360 | 0.004 | 11.357 | 14-#4 | *3 | *5 |
| | Right | 13.25 | 0.03 | 0.533 | 1.717 | 14.360 | 0.001 | 11.357 | 14-#4 | *3 | *5 |
| Beam | Left | 1.17 | 0.79 | 0.131 | 0.372 | 4.805 | 0.009 | 2.888 | 4-#4 | *3 | |
| | Midspan | 1.17 | 0.35 | 0.348 | 0.372 | 4.805 | 0.004 | 8.664 | 2-#4 | *3 | |
| | Right | 1.17 | 0.11 | 0.533 | 0.372 | 4.805 | 0.001 | 8.664 | 2-#4 | *3 | |

NOTES:

- *3 - Design governed by minimum reinforcement.
- *5 - Number of bars governed by maximum allowable spacing.

Top Bar Details

=====

Units: Length (ft)

| Span | Strip | Left | | Continuous | | Right | | | | | |
|----------|--------|-------|--------|------------|--------|-------|--------|-------|--------|-------|------|
| | | Bars | Length | Bars | Length | Bars | Length | Bars | Length | | |
| 1 Column | Middle | --- | --- | 8-#4 | 0.75 | --- | --- | --- | --- | | |
| | Beam | --- | --- | 2-#4 | 0.75 | 1-#4 | 0.75 | 1-#4 | 0.75 | | |
| | Middle | --- | --- | 14-#4 | 0.75 | --- | --- | --- | --- | | |
| 2 Column | Beam | 5-#4 | 3.75 | 3-#4 | 1.75 | --- | --- | 5-#4 | 6.75 | 3-#4 | 1.75 |
| | Middle | 14-#4 | 3.75 | --- | --- | --- | --- | 14-#4 | 6.75 | --- | --- |
| | Beam | 4-#4 | 4.33 | --- | --- | --- | --- | 5-#4 | 7.33 | --- | --- |
| 3 Column | Beam | --- | --- | --- | --- | 8-#4 | 17.50 | --- | --- | --- | --- |
| | Middle | --- | --- | --- | --- | 14-#4 | 17.50 | --- | --- | --- | --- |
| | Beam | 2-#4* | 4.01 | 1-#4* | 2.59 | 2-#4 | 17.50 | 2-#4* | 4.01 | 1-#4* | 2.59 |
| 4 Column | Beam | 5-#4 | 6.75 | 3-#4 | 1.75 | --- | --- | 5-#4 | 3.75 | 3-#4 | 1.75 |
| | Middle | 14-#4 | 6.75 | --- | --- | --- | --- | 14-#4 | 3.75 | --- | --- |
| | Beam | 5-#4 | 7.33 | --- | --- | --- | --- | 4-#4 | 4.33 | --- | --- |
| 5 Column | Beam | --- | --- | --- | --- | 8-#4 | 0.75 | --- | --- | --- | --- |
| | Middle | --- | --- | --- | --- | 14-#4 | 0.75 | --- | --- | --- | --- |
| | Beam | 1-#4 | 0.75 | 1-#4 | 0.75 | 2-#4 | 0.75 | --- | --- | --- | --- |

NOTES:

- * - Bar cut-off location does not meet ACI 318, 12.10.5.1. Revise location, unless the requirements of either 12.10.5.2 or 12.10.5.3 are manually checked and satisfied.

Top Bar Development Lengths

=====

Units: Length (in)

| Span | Strip | Left | | Continuous | | Right | | | | | |
|----------|--------|------|--------|------------|--------|-------|--------|------|--------|------|-------|
| | | Bars | DevLen | Bars | DevLen | Bars | DevLen | Bars | DevLen | | |
| 1 Column | Beam | --- | --- | --- | --- | 8-#4 | 12.00 | --- | --- | --- | --- |
| | Middle | --- | --- | --- | --- | 14-#4 | 12.00 | --- | --- | --- | --- |
| | Beam | --- | --- | --- | --- | 2-#4 | 12.00 | 1-#4 | 12.00 | 1-#4 | 12.00 |
| 2 Column | Beam | 5-#4 | 12.00 | 3-#4 | 12.00 | --- | --- | 5-#4 | 12.00 | 3-#4 | 12.00 |

| | | | | | | | | | |
|----------------------|-------|-------|------------|-------------|-----|-------|-------|------------|-----|
| Middle Beam | 14-#4 | 12.00 | --- | --- | --- | 14-#4 | 12.00 | --- | --- |
| | 4-#4 | 12.00 | --- | --- | --- | 5-#4 | 13.87 | --- | --- |
| 3 Column Middle Beam | --- | --- | --- | 8-#4 12.00 | --- | --- | --- | --- | --- |
| | --- | --- | --- | 14-#4 12.00 | --- | --- | --- | --- | --- |
| | 2-#4 | 12.54 | 1-#4 12.54 | 2-#4 12.00 | --- | 2-#4 | 12.54 | 1-#4 12.54 | --- |
| 4 Column Middle Beam | 5-#4 | 12.00 | 3-#4 12.00 | --- | --- | 5-#4 | 12.00 | 3-#4 12.00 | --- |
| | 14-#4 | 12.00 | --- | --- | --- | 14-#4 | 12.00 | --- | --- |
| | 5-#4 | 13.87 | --- | --- | --- | 4-#4 | 12.00 | --- | --- |
| 5 Column Middle Beam | --- | --- | --- | 8-#4 12.00 | --- | --- | --- | --- | --- |
| | --- | --- | --- | 14-#4 12.00 | --- | --- | --- | --- | --- |
| | 1-#4 | 12.00 | 1-#4 12.00 | 2-#4 12.00 | --- | --- | --- | --- | --- |

Bottom Reinforcement

=====

Units: Width (ft), Mmax (k-ft), Xmax (ft), As (in^2), Sp (in)

| Span Strip | Width | Mmax | Xmax | AsMin | AsMax | AsReq | SpProv | Bars |
|----------------------|-----------------------|------------------------|-------------------------|-------------------------|--------------------------|-------------------------|---------------------------|--------------------------------------|
| 1 Column Middle Beam | 7.58 13.25 1.17 | 0.00 0.00 0.00 | 0.309 0.309 0.309 | 0.000 0.000 0.000 | 8.218 14.360 4.613 | 0.000 0.000 0.000 | 0.000 0.000 0.000 | --- |
| 2 Column Middle Beam | 7.58 13.25 1.17 | 8.50 27.55 48.17 | 8.000 8.000 8.000 | 0.983 1.717 0.797 | 8.218 14.360 4.613 | 0.381 1.242 0.599 | 11.375 11.357 2.888 | 8-#4 *3 *5 14-#4 *3 *5 4-#4 *3 |
| 3 Column Middle Beam | 7.58 13.25 1.17 | 6.47 20.96 36.65 | 8.750 8.750 8.750 | 0.983 1.717 0.603 | 8.218 14.360 4.613 | 0.289 0.942 0.454 | 11.375 11.357 2.888 | 8-#4 *3 *5 14-#4 *3 *5 4-#4 *3 |
| 4 Column Middle Beam | 7.58 13.25 1.17 | 8.50 27.55 48.17 | 9.500 9.500 9.500 | 0.983 1.717 0.797 | 8.218 14.360 4.613 | 0.381 1.242 0.599 | 11.375 11.357 2.888 | 8-#4 *3 *5 14-#4 *3 *5 4-#4 *3 |
| 5 Column Middle Beam | 7.58 13.25 1.17 | 0.00 0.00 0.00 | 0.441 0.441 0.441 | 0.000 0.000 0.000 | 8.218 14.360 4.613 | 0.000 0.000 0.000 | 0.000 0.000 0.000 | --- |

NOTES:

- *3 - Design governed by minimum reinforcement.
- *5 - Number of bars governed by maximum allowable spacing.

Bottom Bar Details

=====

Units: Start (ft), Length (ft)

| Span Strip | Long Bars | | | Short Bars | | |
|----------------------|-----------|-------|--------|------------|-------|--------|
| | Bars | Start | Length | Bars | Start | Length |
| 1 Column Middle Beam | --- | --- | --- | --- | --- | --- |
| 2 Column Middle Beam | 8-#4 | 0.00 | 17.50 | --- | --- | --- |
| | 9-#4 | 0.00 | 17.50 | 5-#4 | 0.00 | 14.88 |
| | 4-#4 | 0.00 | 17.50 | --- | --- | --- |
| 3 Column Middle Beam | 8-#4 | 0.00 | 17.50 | --- | --- | --- |
| | 9-#4 | 0.00 | 17.50 | 5-#4 | 2.63 | 12.25 |
| | 4-#4 | 0.00 | 17.50 | --- | --- | --- |
| 4 Column Middle Beam | 8-#4 | 0.00 | 17.50 | --- | --- | --- |
| | 9-#4 | 0.00 | 17.50 | 5-#4 | 2.63 | 14.88 |
| | 4-#4 | 0.00 | 17.50 | --- | --- | --- |
| 5 Column Middle Beam | --- | --- | --- | --- | --- | --- |

Bottom Bar Development Lengths

=====

Units: DevLen (in)

| Span Strip | Long Bars | | Short Bars | |
|----------------------|-----------|--------|------------|--------|
| | Bars | DevLen | Bars | DevLen |
| 1 Column Middle Beam | --- | --- | --- | --- |
| 2 Column Middle Beam | 8-#4 | 12.00 | --- | --- |
| | 9-#4 | 12.00 | 5-#4 | 12.00 |
| | 4-#4 | 12.00 | --- | --- |
| 3 Column Middle Beam | 8-#4 | 12.00 | --- | --- |
| | 9-#4 | 12.00 | 5-#4 | 12.00 |
| | 4-#4 | 12.00 | --- | --- |

4 Column 8-#4 12.00 ---
 Middle 9-#4 12.00 5-#4 12.00
 Beam 4-#4 12.00 ---

 5 Column --- ---
 Middle --- ---
 Beam --- ---

Flexural Capacity

=====

Units: x (ft), As (in^2), PhiMn, Mu (k-ft)

| Span | Strip | Top | | | | | | Bottom | | | | | | | |
|--------|--------|--------|--------|---------|--------|--------|------|--------|-------|--------|-------|------|------|--------|-----|
| | | x | AsTop | PhiMn- | Mu- | Comb | Pat | Status | AsBot | PhiMn+ | Mu+ | Comb | Pat | Status | |
| 1 | Column | 0.000 | 1.60 | -34.88 | 0.00 | U1 | All | OK | 0.00 | 0.00 | 0.00 | U1 | All | OK | |
| | | 0.217 | 1.60 | -34.88 | -0.02 | U1 | All | OK | 0.00 | 0.00 | 0.00 | U1 | All | OK | |
| | | 0.375 | 1.60 | -34.88 | -0.05 | U1 | All | OK | 0.00 | 0.00 | 0.00 | U1 | All | OK | |
| | | 0.402 | 1.60 | -34.88 | -0.06 | U1 | All | OK | 0.00 | 0.00 | 0.00 | U1 | All | OK | |
| | | 0.619 | 1.60 | -34.88 | -0.14 | U1 | All | OK | 0.00 | 0.00 | 0.00 | U1 | All | OK | |
| | Middle | 0.750 | 1.60 | -34.88 | -0.20 | U1 | All | --- | 0.00 | 0.00 | 0.00 | U1 | All | --- | |
| | | 0.000 | 2.80 | -61.04 | 0.00 | U1 | All | OK | 0.00 | 0.00 | 0.00 | U1 | All | OK | |
| | | 0.217 | 2.80 | -61.04 | -0.03 | U1 | All | OK | 0.00 | 0.00 | 0.00 | U1 | All | OK | |
| | | 0.375 | 2.80 | -61.04 | -0.08 | U1 | All | OK | 0.00 | 0.00 | 0.00 | U1 | All | OK | |
| | | 0.402 | 2.80 | -61.04 | -0.10 | U1 | All | OK | 0.00 | 0.00 | 0.00 | U1 | All | OK | |
| | | 0.619 | 2.80 | -61.04 | -0.22 | U1 | All | OK | 0.00 | 0.00 | 0.00 | U1 | All | OK | |
| | | 0.750 | 2.80 | -61.04 | -0.30 | U1 | All | --- | 0.00 | 0.00 | 0.00 | U1 | All | --- | |
| | | Beam | 0.000 | 0.80 | -66.58 | 0.00 | U1 | All | OK | 0.00 | 0.00 | 0.00 | U1 | All | OK |
| | | | 0.217 | 0.80 | -66.58 | -0.11 | U1 | All | OK | 0.00 | 0.00 | 0.00 | U1 | All | OK |
| | | | 0.375 | 0.80 | -66.58 | -0.31 | U1 | All | OK | 0.00 | 0.00 | 0.00 | U1 | All | OK |
| | | | 0.402 | 0.80 | -66.58 | -0.35 | U1 | All | OK | 0.00 | 0.00 | 0.00 | U1 | All | OK |
| | | | 0.619 | 0.80 | -66.58 | -0.79 | U1 | All | OK | 0.00 | 0.00 | 0.00 | U1 | All | OK |
| | | | 0.750 | 0.80 | -66.58 | -1.12 | U1 | All | --- | 0.00 | 0.00 | 0.00 | U1 | All | --- |
| 2 | Column | | 0.000 | 1.60 | -34.88 | -10.78 | U1 | All | --- | 1.60 | 34.88 | 0.00 | U1 | All | --- |
| | | 0.750 | 1.60 | -34.88 | -7.06 | U1 | All | OK | 1.60 | 34.88 | 0.00 | U1 | All | OK | |
| | | 1.750 | 1.00 | -22.06 | -2.95 | U1 | Even | OK | 1.60 | 34.88 | 0.00 | U1 | All | OK | |
| | | 2.750 | 1.00 | -22.06 | 0.00 | U1 | All | OK | 1.60 | 34.88 | 0.83 | U1 | All | OK | |
| | | 3.750 | 0.00 | 0.00 | 0.00 | U1 | All | OK | 1.60 | 34.88 | 3.52 | U1 | All | OK | |
| | | 6.350 | 0.00 | 0.00 | 0.00 | U1 | All | OK | 1.60 | 34.88 | 7.81 | U1 | All | OK | |
| | | 8.000 | 0.00 | 0.00 | 0.00 | U1 | All | OK | 1.60 | 34.88 | 8.50 | U1 | All | OK | |
| | | 8.750 | 0.00 | 0.00 | 0.00 | U1 | All | OK | 1.60 | 34.88 | 8.29 | U1 | All | OK | |
| | | 10.750 | 0.00 | 0.00 | 0.00 | U1 | All | OK | 1.60 | 34.88 | 6.46 | U1 | Even | OK | |
| | | 11.150 | 0.40 | -8.93 | 0.00 | U1 | All | OK | 1.60 | 34.88 | 5.94 | U1 | Even | OK | |
| | | 11.750 | 1.00 | -22.06 | 0.00 | U1 | All | OK | 1.60 | 34.88 | 5.02 | U1 | Even | OK | |
| | | 15.750 | 1.00 | -22.06 | -9.46 | U1 | All | OK | 1.60 | 34.88 | 0.00 | U1 | All | OK | |
| | | 16.750 | 1.60 | -34.88 | -14.23 | U1 | All | OK | 1.60 | 34.88 | 0.00 | U1 | All | OK | |
| | | 17.500 | 1.60 | -34.88 | -18.14 | U1 | All | --- | 1.60 | 34.88 | 0.00 | U1 | All | --- | |
| | | Middle | 0.000 | 2.80 | -61.04 | -22.97 | U1 | All | --- | 2.80 | 61.04 | 0.00 | U1 | All | --- |
| | | | 0.750 | 2.80 | -61.04 | -15.36 | U1 | All | OK | 2.80 | 61.04 | 0.00 | U1 | All | OK |
| | | | 2.750 | 2.80 | -61.04 | 0.00 | U1 | All | OK | 2.80 | 61.04 | 2.68 | U1 | All | OK |
| | 3.750 | | 0.00 | 0.00 | 0.00 | U1 | All | OK | 2.80 | 61.04 | 11.41 | U1 | All | OK | |
| | 6.350 | | 0.00 | 0.00 | 0.00 | U1 | All | OK | 2.80 | 61.04 | 25.30 | U1 | All | OK | |
| | 8.000 | | 0.00 | 0.00 | 0.00 | U1 | All | OK | 2.80 | 61.04 | 27.55 | U1 | All | OK | |
| | 8.750 | | 0.00 | 0.00 | 0.00 | U1 | All | OK | 2.80 | 61.04 | 26.88 | U1 | All | OK | |
| | 10.750 | | 0.00 | 0.00 | 0.00 | U1 | All | OK | 2.80 | 61.04 | 20.94 | U1 | Even | OK | |
| | 11.150 | | 1.12 | -24.89 | 0.00 | U1 | All | OK | 2.80 | 61.04 | 19.25 | U1 | Even | OK | |
| | 11.750 | | 2.80 | -61.04 | 0.00 | U1 | All | OK | 2.80 | 61.04 | 16.26 | U1 | Even | OK | |
| | 13.875 | | 2.80 | -61.04 | -8.12 | U1 | Odd | OK | 2.80 | 61.04 | 1.02 | U1 | Even | OK | |
| | 14.875 | | 2.80 | -61.04 | -17.71 | U1 | All | OK | 1.80 | 39.69 | 0.00 | U1 | All | OK | |
| | 16.750 | | 2.80 | -61.04 | -46.12 | U1 | All | OK | 1.80 | 39.69 | 0.00 | U1 | All | OK | |
| | 17.500 | | 2.80 | -61.04 | -59.82 | U1 | All | --- | 1.80 | 39.69 | 0.00 | U1 | All | --- | |
| | Beam | | 0.000 | 0.80 | -66.58 | -61.08 | U1 | All | --- | 0.80 | 63.86 | 0.00 | U1 | All | --- |
| | | | 0.750 | 0.80 | -66.58 | -40.00 | U1 | All | OK | 0.80 | 63.86 | 0.00 | U1 | All | OK |
| | | 3.333 | 0.80 | -66.58 | 0.00 | U1 | All | OK | 0.80 | 63.86 | 13.97 | U1 | All | OK | |
| | | 4.333 | 0.00 | 0.00 | 0.00 | U1 | All | OK | 0.80 | 63.86 | 27.32 | U1 | All | OK | |
| | | 6.350 | 0.00 | 0.00 | 0.00 | U1 | All | OK | 0.80 | 63.86 | 44.24 | U1 | All | OK | |
| 8.000 | | 0.00 | 0.00 | 0.00 | U1 | All | OK | 0.80 | 63.86 | 48.17 | U1 | All | OK | | |
| 8.750 | | 0.00 | 0.00 | 0.00 | U1 | All | OK | 0.80 | 63.86 | 46.99 | U1 | All | OK | | |
| 10.167 | | 0.00 | 0.00 | 0.00 | U1 | All | OK | 0.80 | 63.86 | 40.07 | U1 | Even | OK | | |
| 11.150 | | 0.85 | -70.69 | 0.00 | U1 | All | OK | 0.80 | 63.86 | 33.65 | U1 | Even | OK | | |
| 11.322 | | 1.00 | -82.66 | 0.00 | U1 | All | OK | 0.80 | 63.86 | 32.25 | U1 | Even | OK | | |
| 16.750 | | 1.00 | -82.66 | -80.63 | U1 | All | OK | 0.80 | 63.86 | 0.00 | U1 | All | OK | | |
| 17.000 | | 1.00 | -82.66 | -87.85 | U1 | All | --- | 0.80 | 63.86 | 0.00 | U1 | All | --- | | |
| 17.500 | | 1.00 | -82.66 | -102.80 | U1 | All | --- | 0.80 | 63.86 | 0.00 | U1 | All | --- | | |
| 3 | | Column | 0.000 | 1.60 | -34.88 | -16.55 | U1 | All | --- | 1.60 | 34.88 | 0.00 | U1 | All | --- |
| | | | 0.750 | 1.60 | -34.88 | -12.91 | U1 | All | OK | 1.60 | 34.88 | 0.00 | U1 | All | OK |
| | | | 6.350 | 1.60 | -34.88 | -0.15 | U1 | Even | OK | 1.60 | 34.88 | 5.05 | U1 | Odd | OK |
| | 8.750 | | 1.60 | -34.88 | 0.00 | U1 | All | OK | 1.60 | 34.88 | 6.47 | U1 | Odd | OK | |
| | 11.150 | | 1.60 | -34.88 | -0.15 | U1 | Even | OK | 1.60 | 34.88 | 5.05 | U1 | Odd | OK | |
| | 16.750 | | 1.60 | -34.88 | -12.91 | U1 | All | OK | 1.60 | 34.88 | 0.00 | U1 | All | OK | |
| | 17.500 | | 1.60 | -34.88 | -16.55 | U1 | All | --- | 1.60 | 34.88 | 0.00 | U1 | All | --- | |
| | Middle | 0.000 | 2.80 | -61.04 | -53.65 | U1 | All | --- | 1.80 | 39.69 | 0.00 | U1 | All | --- | |
| | | 0.750 | 2.80 | -61.04 | -41.84 | U1 | All | OK | 1.80 | 39.69 | 0.00 | U1 | All | OK | |
| | | 2.625 | 2.80 | -61.04 | -16.97 | U1 | All | OK | 1.80 | 39.69 | 0.00 | U1 | All | OK | |
| | | 3.625 | 2.80 | -61.04 | -9.01 | U1 | S1 | OK | 2.80 | 61.04 | 1.12 | U1 | S3 | OK | |
| | | 6.350 | 2.80 | -61.04 | -0.47 | U1 | Even | OK | 2.80 | 61.04 | 16.37 | U1 | Odd | OK | |

| | | | | | | | | | | | | |
|----------|--|--------|------|--------|---------|---------|-----|------|-------|-------|---------|-----|
| | | 8.750 | 2.80 | -61.04 | 0.00 | U1 All | OK | 2.80 | 61.04 | 20.96 | U1 Odd | OK |
| | | 11.150 | 2.80 | -61.04 | -0.47 | U1 Even | OK | 2.80 | 61.04 | 16.37 | U1 Odd | OK |
| | | 13.875 | 2.80 | -61.04 | -9.01 | U1 S4 | OK | 2.80 | 61.04 | 1.12 | U1 S2 | OK |
| | | 14.875 | 2.80 | -61.04 | -16.97 | U1 All | OK | 1.80 | 39.69 | 0.00 | U1 All | OK |
| | | 16.750 | 2.80 | -61.04 | -41.84 | U1 All | OK | 1.80 | 39.69 | 0.00 | U1 All | OK |
| | | 17.500 | 2.80 | -61.04 | -53.65 | U1 All | --- | 1.80 | 39.69 | 0.00 | U1 All | --- |
| Beam | | 0.000 | 1.00 | -82.66 | -93.79 | U1 All | --- | 0.80 | 63.86 | 0.00 | U1 All | --- |
| | | 0.250 | 1.00 | -82.66 | -86.71 | U1 All | --- | 0.80 | 63.86 | 0.00 | U1 All | --- |
| | | 0.750 | 1.00 | -82.66 | -73.15 | U1 All | OK | 0.80 | 63.86 | 0.00 | U1 All | OK |
| | | 1.542 | 1.00 | -82.66 | -53.37 | U1 All | OK | 0.80 | 63.86 | 0.00 | U1 All | OK |
| | | 2.587 | 0.80 | -66.58 | -30.42 | U1 All | OK | 0.80 | 63.86 | 0.00 | U1 All | OK |
| | | 2.963 | 0.80 | -66.58 | -23.03 | U1 All | OK | 0.80 | 63.86 | 0.00 | U1 All | OK |
| | | 4.008 | 0.40 | -33.75 | -12.84 | U1 S1 | OK | 0.80 | 63.86 | 6.74 | U1 S3 | OK |
| | | 6.350 | 0.40 | -33.75 | -0.83 | U1 Even | OK | 0.80 | 63.86 | 28.62 | U1 Odd | OK |
| | | 8.750 | 0.40 | -33.75 | 0.00 | U1 All | OK | 0.80 | 63.86 | 36.65 | U1 Odd | OK |
| | | 11.150 | 0.40 | -33.75 | -0.83 | U1 Even | OK | 0.80 | 63.86 | 28.62 | U1 Odd | OK |
| | | 13.492 | 0.40 | -33.75 | -12.84 | U1 S4 | OK | 0.80 | 63.86 | 6.74 | U1 S2 | OK |
| | | 14.537 | 0.80 | -66.58 | -23.03 | U1 All | OK | 0.80 | 63.86 | 0.00 | U1 All | OK |
| | | 14.913 | 0.80 | -66.58 | -30.42 | U1 All | OK | 0.80 | 63.86 | 0.00 | U1 All | OK |
| | | 15.958 | 1.00 | -82.66 | -53.37 | U1 All | OK | 0.80 | 63.86 | 0.00 | U1 All | OK |
| | | 16.750 | 1.00 | -82.66 | -73.15 | U1 All | OK | 0.80 | 63.86 | 0.00 | U1 All | OK |
| | | 17.250 | 1.00 | -82.66 | -86.71 | U1 All | --- | 0.80 | 63.86 | 0.00 | U1 All | --- |
| | | 17.500 | 1.00 | -82.66 | -93.79 | U1 All | --- | 0.80 | 63.86 | 0.00 | U1 All | --- |
| 4 Column | | 0.000 | 1.60 | -34.88 | -18.14 | U1 All | --- | 1.60 | 34.88 | 0.00 | U1 All | --- |
| | | 0.750 | 1.60 | -34.88 | -14.23 | U1 All | OK | 1.60 | 34.88 | 0.00 | U1 All | OK |
| | | 1.750 | 1.00 | -22.06 | -9.46 | U1 All | OK | 1.60 | 34.88 | 0.00 | U1 All | OK |
| | | 5.750 | 1.00 | -22.06 | 0.00 | U1 All | OK | 1.60 | 34.88 | 5.02 | U1 Even | OK |
| | | 6.350 | 0.40 | -8.93 | 0.00 | U1 All | OK | 1.60 | 34.88 | 5.94 | U1 Even | OK |
| | | 6.750 | 0.00 | 0.00 | 0.00 | U1 All | OK | 1.60 | 34.88 | 6.46 | U1 Even | OK |
| | | 8.750 | 0.00 | 0.00 | 0.00 | U1 All | OK | 1.60 | 34.88 | 8.29 | U1 All | OK |
| | | 9.500 | 0.00 | 0.00 | 0.00 | U1 All | OK | 1.60 | 34.88 | 8.50 | U1 All | OK |
| | | 11.150 | 0.00 | 0.00 | 0.00 | U1 All | OK | 1.60 | 34.88 | 7.81 | U1 All | OK |
| | | 13.750 | 0.00 | 0.00 | 0.00 | U1 All | OK | 1.60 | 34.88 | 3.52 | U1 All | OK |
| | | 14.750 | 1.00 | -22.06 | 0.00 | U1 All | OK | 1.60 | 34.88 | 0.83 | U1 All | OK |
| | | 15.750 | 1.00 | -22.06 | -2.95 | U1 Even | OK | 1.60 | 34.88 | 0.00 | U1 All | OK |
| | | 16.750 | 1.60 | -34.88 | -7.06 | U1 All | OK | 1.60 | 34.88 | 0.00 | U1 All | OK |
| | | 17.500 | 1.60 | -34.88 | -10.78 | U1 All | --- | 1.60 | 34.88 | 0.00 | U1 All | --- |
| Middle | | 0.000 | 2.80 | -61.04 | -59.82 | U1 All | --- | 1.80 | 39.69 | 0.00 | U1 All | --- |
| | | 0.750 | 2.80 | -61.04 | -46.12 | U1 All | OK | 1.80 | 39.69 | 0.00 | U1 All | OK |
| | | 2.625 | 2.80 | -61.04 | -17.71 | U1 All | OK | 1.80 | 39.69 | 0.00 | U1 All | OK |
| | | 3.625 | 2.80 | -61.04 | -8.12 | U1 Odd | OK | 2.80 | 61.04 | 1.02 | U1 Even | OK |
| | | 5.750 | 2.80 | -61.04 | 0.00 | U1 All | OK | 2.80 | 61.04 | 16.26 | U1 Even | OK |
| | | 6.350 | 1.12 | -24.89 | 0.00 | U1 All | OK | 2.80 | 61.04 | 19.25 | U1 Even | OK |
| | | 6.750 | 0.00 | 0.00 | 0.00 | U1 All | OK | 2.80 | 61.04 | 20.94 | U1 Even | OK |
| | | 8.750 | 0.00 | 0.00 | 0.00 | U1 All | OK | 2.80 | 61.04 | 26.88 | U1 All | OK |
| | | 9.500 | 0.00 | 0.00 | 0.00 | U1 All | OK | 2.80 | 61.04 | 27.55 | U1 All | OK |
| | | 11.150 | 0.00 | 0.00 | 0.00 | U1 All | OK | 2.80 | 61.04 | 25.30 | U1 All | OK |
| | | 13.750 | 0.00 | 0.00 | 0.00 | U1 All | OK | 2.80 | 61.04 | 11.41 | U1 All | OK |
| | | 14.750 | 2.80 | -61.04 | 0.00 | U1 All | OK | 2.80 | 61.04 | 2.68 | U1 All | OK |
| | | 16.750 | 2.80 | -61.04 | -15.36 | U1 All | OK | 2.80 | 61.04 | 0.00 | U1 All | OK |
| | | 17.500 | 2.80 | -61.04 | -22.97 | U1 All | --- | 2.80 | 61.04 | 0.00 | U1 All | --- |
| Beam | | 0.000 | 1.00 | -82.66 | -102.80 | U1 All | --- | 0.80 | 63.86 | 0.00 | U1 All | --- |
| | | 0.500 | 1.00 | -82.66 | -87.85 | U1 All | --- | 0.80 | 63.86 | 0.00 | U1 All | --- |
| | | 0.750 | 1.00 | -82.66 | -80.63 | U1 All | OK | 0.80 | 63.86 | 0.00 | U1 All | OK |
| | | 6.178 | 1.00 | -82.66 | 0.00 | U1 All | OK | 0.80 | 63.86 | 32.25 | U1 Even | OK |
| | | 6.350 | 0.85 | -70.69 | 0.00 | U1 All | OK | 0.80 | 63.86 | 33.65 | U1 Even | OK |
| | | 7.333 | 0.00 | 0.00 | 0.00 | U1 All | OK | 0.80 | 63.86 | 40.07 | U1 Even | OK |
| | | 8.750 | 0.00 | 0.00 | 0.00 | U1 All | OK | 0.80 | 63.86 | 46.99 | U1 All | OK |
| | | 9.500 | 0.00 | 0.00 | 0.00 | U1 All | OK | 0.80 | 63.86 | 48.17 | U1 All | OK |
| | | 11.150 | 0.00 | 0.00 | 0.00 | U1 All | OK | 0.80 | 63.86 | 44.24 | U1 All | OK |
| | | 13.167 | 0.00 | 0.00 | 0.00 | U1 All | OK | 0.80 | 63.86 | 27.32 | U1 All | OK |
| | | 14.167 | 0.80 | -66.58 | 0.00 | U1 All | OK | 0.80 | 63.86 | 13.97 | U1 All | OK |
| | | 16.750 | 0.80 | -66.58 | -40.00 | U1 All | OK | 0.80 | 63.86 | 0.00 | U1 All | OK |
| | | 17.500 | 0.80 | -66.58 | -61.08 | U1 All | --- | 0.80 | 63.86 | 0.00 | U1 All | --- |
| 5 Column | | 0.000 | 1.60 | -34.88 | -0.20 | U1 All | --- | 0.00 | 0.00 | 0.00 | U1 All | --- |
| | | 0.131 | 1.60 | -34.88 | -0.14 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |
| | | 0.348 | 1.60 | -34.88 | -0.06 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |
| | | 0.375 | 1.60 | -34.88 | -0.05 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |
| | | 0.533 | 1.60 | -34.88 | -0.02 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |
| Middle | | 0.750 | 1.60 | -34.88 | 0.00 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |
| | | 0.000 | 2.80 | -61.04 | -0.30 | U1 All | --- | 0.00 | 0.00 | 0.00 | U1 All | --- |
| | | 0.131 | 2.80 | -61.04 | -0.22 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |
| | | 0.348 | 2.80 | -61.04 | -0.10 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |
| | | 0.375 | 2.80 | -61.04 | -0.08 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |
| | | 0.533 | 2.80 | -61.04 | -0.03 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |
| | | 0.750 | 2.80 | -61.04 | 0.00 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |
| Beam | | 0.000 | 0.80 | -66.58 | -1.12 | U1 All | --- | 0.00 | 0.00 | 0.00 | U1 All | --- |
| | | 0.131 | 0.80 | -66.58 | -0.79 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |
| | | 0.348 | 0.80 | -66.58 | -0.35 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |
| | | 0.375 | 0.80 | -66.58 | -0.31 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |
| | | 0.533 | 0.80 | -66.58 | -0.11 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |
| | | 0.750 | 0.80 | -66.58 | 0.00 | U1 All | OK | 0.00 | 0.00 | 0.00 | U1 All | OK |

Section Properties

Units: d (in), Av/s (in²/in), PhiVc (kip)

| Span | d (Av/s)min | PhiVc |
|------|-------------|--------|
| 1 | 18.24 | 0.0117 |
| 2 | 18.24 | 0.0117 |
| 3 | 18.24 | 0.0117 |
| 4 | 18.24 | 0.0117 |
| 5 | 18.24 | 0.0117 |

Beam Transverse Reinforcement Demand

Units: Start, End, Xu (in), Vu (ft), Av/s (kip/in²)

| Span | Start | End | Required | | | Av/s | Demand |
|--------|--------|--------|----------|--------------|---------|-----------|-----------|
| | | | Xu | Vu Comb/Patt | Av/s | | Av/s |
| 1 | 0.000 | 0.000 | 0.000 | 0.00 | U1/All | 0.0000 | 0.0000 |
| 2 | 1.000 | 4.122 | 2.270 | 32.32 | U1/All | 0.0099 | 0.0117 *8 |
| | 4.122 | 5.973 | 4.122 | 21.68 | U1/All | 0.0000 | 0.0117 *8 |
| | 5.973 | 7.824 | 5.973 | 11.37 | U1/Even | 0.0000 | 0.0000 |
| | 7.824 | 9.676 | 9.676 | 10.23 | U1/All | 0.0000 | 0.0000 |
| | 9.676 | 11.527 | 11.527 | 20.87 | U1/All | 0.0000 | 0.0117 *8 |
| | 11.527 | 13.378 | 13.378 | 31.50 | U1/All | 0.0089 | 0.0117 *8 |
| 13.378 | 16.500 | 15.230 | 42.14 | U1/All | 0.0218 | 0.0218 | |
| 3 | 1.000 | 4.122 | 2.270 | 37.23 | U1/All | 0.0158 | 0.0158 |
| | 4.122 | 5.973 | 4.122 | 26.59 | U1/All | 0.0029 | 0.0117 *8 |
| | 5.973 | 7.824 | 5.973 | 15.96 | U1/All | 0.0000 | 0.0117 *8 |
| | 7.824 | 9.676 | 9.676 | 6.78 | U1/S3 | 0.0000 | 0.0000 |
| | 9.676 | 11.527 | 11.527 | 15.96 | U1/All | 0.0000 | 0.0117 *8 |
| | 11.527 | 13.378 | 13.378 | 26.59 | U1/All | 0.0029 | 0.0117 *8 |
| 13.378 | 16.500 | 15.230 | 37.23 | U1/All | 0.0158 | 0.0158 | |
| 4 | 1.000 | 4.122 | 2.270 | 42.14 | U1/All | 0.0218 | 0.0218 |
| | 4.122 | 5.973 | 4.122 | 31.50 | U1/All | 0.0089 | 0.0117 *8 |
| | 5.973 | 7.824 | 5.973 | 20.87 | U1/All | 0.0000 | 0.0117 *8 |
| | 7.824 | 9.676 | 7.824 | 10.23 | U1/All | 0.0000 | 0.0000 |
| | 9.676 | 11.527 | 11.527 | 11.37 | U1/Even | 0.0000 | 0.0000 |
| | 11.527 | 13.378 | 13.378 | 21.68 | U1/All | 0.0000 | 0.0117 *8 |
| 13.378 | 16.500 | 15.230 | 32.32 | U1/All | 0.0099 | 0.0117 *8 | |
| 5 | 0.750 | 0.750 | 0.750 | 0.00 | U1/All | 0.0000 | 0.0000 |

NOTES:

*8 - Minimum transverse (stirrup) reinforcement governs.

Beam Transverse Reinforcement Details

Units: spacing & distance (in).

Span Size Stirrups (2 legs each unless otherwise noted)

| | |
|---|---------------------------------------|
| 1 | #5 --- None --- |
| 2 | #4 8 @ 8.0 + <-- 44.4 --> + 10 @ 8.6 |
| 3 | #4 10 @ 8.6 + <-- 22.2 --> + 10 @ 8.6 |
| 4 | #4 10 @ 8.6 + <-- 44.4 --> + 8 @ 8.0 |
| 5 | #5 --- None --- |

Beam Transverse Reinforcement Capacity

Units: Start, End, Xu (ft), Vu, PhiVn (kip), Av/s (in²/in), Av (in²), Sp (in)

| Span | Start | End | Required | | | Provided | | | | |
|--------|--------|--------|----------|--------------|---------|----------|-------|-------|--------|----------|
| | | | Xu | Vu Comb/Patt | Av/s | Av | Sp | Av/s | PhiVn | |
| 1 | 0.000 | 0.750 | 0.000 | 0.00 | U1/All | ----- | ----- | ----- | ----- | ----- |
| 2 | 0.000 | 1.000 | 2.270 | 32.32 | U1/All | ----- | ----- | ----- | ----- | ----- |
| | 1.000 | 5.973 | 2.270 | 32.32 | U1/All | 0.0099 | 0.40 | 8.0 | 0.0503 | 65.50 *8 |
| | 5.973 | 9.676 | 5.973 | 11.37 | U1/Even | 0.0000 | ----- | ----- | ----- | 12.11 |
| | 9.676 | 16.500 | 15.230 | 42.14 | U1/All | 0.0218 | 0.40 | 8.6 | 0.0464 | 62.32 |
| 16.500 | 17.500 | 15.230 | 42.14 | U1/All | ----- | ----- | ----- | ----- | ----- | |
| 3 | 0.000 | 1.000 | 2.270 | 37.23 | U1/All | ----- | ----- | ----- | ----- | ----- |
| | 1.000 | 7.824 | 2.270 | 37.23 | U1/All | 0.0158 | 0.40 | 8.6 | 0.0464 | 62.32 |
| | 7.824 | 9.676 | 9.676 | 6.78 | U1/S3 | 0.0000 | ----- | ----- | ----- | 12.11 |
| | 9.676 | 16.500 | 15.230 | 37.23 | U1/All | 0.0158 | 0.40 | 8.6 | 0.0464 | 62.32 |
| 16.500 | 17.500 | 15.230 | 37.23 | U1/All | ----- | ----- | ----- | ----- | ----- | |
| 4 | 0.000 | 1.000 | 2.270 | 42.14 | U1/All | ----- | ----- | ----- | ----- | ----- |
| | 1.000 | 7.824 | 2.270 | 42.14 | U1/All | 0.0218 | 0.40 | 8.6 | 0.0464 | 62.32 |
| | 7.824 | 11.527 | 11.527 | 11.37 | U1/Even | 0.0000 | ----- | ----- | ----- | 12.11 |
| | 11.527 | 16.500 | 15.230 | 32.32 | U1/All | 0.0099 | 0.40 | 8.0 | 0.0503 | 65.50 *8 |
| 16.500 | 17.500 | 15.230 | 32.32 | U1/All | ----- | ----- | ----- | ----- | ----- | |
| 5 | 0.000 | 0.750 | 0.750 | 0.00 | U1/All | ----- | ----- | ----- | ----- | ----- |

NOTES:

*8 - Minimum transverse (stirrup) reinforcement governs.

Slab Shear Capacity

=====

Units: b, d (in), Xu (ft), PhiVc, Vu(kip)

| Span | b | d | Vratio | PhiVc | Vu | Xu |
|------|--------|------|--------|--------|------|-------|
| 1 | 250.00 | 5.00 | 0.000 | 118.59 | 0.00 | 0.00 |
| 2 | 250.00 | 5.00 | 0.000 | 118.59 | 0.00 | 16.33 |
| 3 | 250.00 | 5.00 | 0.000 | 118.59 | 0.00 | 16.33 |
| 4 | 250.00 | 5.00 | 0.000 | 118.59 | 0.00 | 1.17 |
| 5 | 250.00 | 5.00 | 0.000 | 118.59 | 0.00 | 0.00 |

Flexural Transfer of Negative Unbalanced Moment at Supports

=====

Units: Width (in), Munb (k-ft), As (in^2)

| Supp | Width | Width-c | d | Munb | Comb | Pat | GammaF | AsReq | AsProv | Add Bars |
|------|-------|---------|------|-------|------|------|--------|-------|--------|----------|
| 1 | 36.00 | 36.00 | 5.00 | 93.21 | U1 | All | 0.687 | 3.421 | 1.187 | 12-#4 |
| 2 | 36.00 | 36.00 | 5.00 | 46.73 | U1 | Even | 0.600 | 1.333 | 1.387 | --- |
| 3 | 36.00 | 36.00 | 5.00 | 46.73 | U1 | Even | 0.600 | 1.333 | 1.387 | --- |
| 4 | 36.00 | 36.00 | 5.00 | 93.21 | U1 | All | 0.687 | 3.421 | 1.187 | 12-#4 |

Punching Shear Around Columns

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Critical Section Properties

Units: b1, b2, b0, davg, CG, c(left), c(right) (in), Ac (in^2), Jc (in^4)

| Supp | Type | b1 | b2 | b0 | davg | CG | c(left) | c(right) | Ac | Jc |
|------|------|-------|-------|-------|-------|-------|---------|----------|------|-------------|
| 1 | Rect | 20.50 | 44.00 | 64.00 | 17.25 | 2.41 | 11.41 | 9.09 | 1104 | 95338 |
| 2 | Rect | 23.00 | 23.00 | 92.00 | 13.52 | 0.00 | 11.50 | 11.50 | 1244 | 1.1499e+005 |
| 3 | Rect | 23.00 | 23.00 | 92.00 | 13.52 | 0.00 | 11.50 | 11.50 | 1244 | 1.1499e+005 |
| 4 | Rect | 20.50 | 44.00 | 64.00 | 17.25 | -2.41 | 9.09 | 11.41 | 1104 | 95338 |

Punching Shear Results

Units: Vu (kip), Munb (k-ft), vu (psi), Phi*vc (psi)

| Supp | Vu | vu | Munb | Comb | Pat | GammaV | vu | Phi*vc |
|------|--------|------|--------|------|-----|--------|------|--------|
| 1 | 48.47 | 43.9 | 83.49 | U1 | All | 0.313 | 73.8 | 189.7 |
| 2 | 104.50 | 84.0 | -16.77 | U1 | All | 0.400 | 92.1 | 189.7 |
| 3 | 104.50 | 84.0 | 16.77 | U1 | All | 0.400 | 92.1 | 189.7 |
| 4 | 48.47 | 43.9 | -83.49 | U1 | All | 0.313 | 73.8 | 189.7 |

Material Takeoff

=====

Reinforcement in the Direction of Analysis

| | | | | | |
|--------------|------------|-----|---------------|-----|-----------------|
| Top Bars: | 673.5 lb | <=> | 12.47 lb/ft | <=> | 0.567 lb/ft^2 |
| Bottom Bars: | 876.8 lb | <=> | 16.24 lb/ft | <=> | 0.738 lb/ft^2 |
| Stirrups: | 183.9 lb | <=> | 3.41 lb/ft | <=> | 0.155 lb/ft^2 |
| Total Steel: | 1734.2 lb | <=> | 32.11 lb/ft | <=> | 1.460 lb/ft^2 |
| Concrete: | 817.2 ft^3 | <=> | 15.13 ft^3/ft | <=> | 0.688 ft^3/ft^2 |

```

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    oooooo  oo  oooooo  ooo  oooooo  o  oooooo  (TM)
    
```

```

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[3] DEFLECTION RESULTS

Section Properties

Frame Section Properties

Units: Ig, Icr (in^4), Mcr (k-ft)

| Span Zone | M+ve | | | M-ve | | |
|-----------|--------|------|---------|--------|-------|----------|
| | Ig | Icr | Mcr | Ig | Icr | Mcr |
| 1 Left | 25395 | 0 | 63.14 | 9333 | 6766 | -36.89 |
| Midspan | 25395 | 0 | 63.14 | 9333 | 7147 | -36.89 |
| Right | 433026 | 0 | 1267.91 | 433026 | 23081 | -1267.91 |
| 2 Left | 25395 | 1552 | 63.14 | 9333 | 7147 | -36.89 |
| Midspan | 25395 | 2280 | 63.14 | 9333 | 0 | -36.89 |
| Right | 25395 | 1552 | 63.14 | 9333 | 7331 | -36.89 |
| 3 Left | 25395 | 1552 | 63.14 | 9333 | 7331 | -36.89 |
| Midspan | 25395 | 1552 | 63.14 | 9333 | 6766 | -36.89 |
| Right | 25395 | 1552 | 63.14 | 9333 | 7331 | -36.89 |
| 4 Left | 25395 | 1552 | 63.14 | 9333 | 7331 | -36.89 |
| Midspan | 25395 | 2280 | 63.14 | 9333 | 0 | -36.89 |
| Right | 25395 | 1552 | 63.14 | 9333 | 7147 | -36.89 |
| 5 Left | 433026 | 0 | 1267.91 | 433026 | 23081 | -1267.91 |
| Midspan | 25395 | 0 | 63.14 | 9333 | 7147 | -36.89 |
| Right | 25395 | 0 | 63.14 | 9333 | 6766 | -36.89 |

NOTES: M+ve values are for positive moments (tension at bottom face).
 M-ve values are for negative moments (tension at top face).

Frame Effective Section Properties

Units: Ie, Ie,avg (in^4), Mmax (k-ft)

| Span Zone | Weight | Load Level | | | | | |
|-----------|--------|------------|--------|-----------|--------|-----------|--------|
| | | Dead | | Sustained | | Dead+Live | |
| | | Mmax | Ie | Mmax | Ie | Mmax | Ie |
| 1 Right | 1.000 | -0.52 | 433026 | -0.52 | 433026 | -1.14 | 433026 |
| Span Avg | ---- | ---- | 433026 | ---- | 433026 | ---- | 433026 |
| 2 Middle | 0.850 | 27.19 | 25395 | 27.19 | 25395 | 59.43 | 25395 |
| Right | 0.150 | -58.35 | 7837 | -58.35 | 7837 | -127.56 | 7380 |
| Span Avg | ---- | ---- | 22761 | ---- | 22761 | ---- | 22693 |
| 3 Left | 0.150 | -52.93 | 8009 | -52.93 | 8009 | -115.73 | 7396 |
| Middle | 0.700 | 18.06 | 25395 | 18.06 | 25395 | 39.49 | 25395 |
| Right | 0.150 | -52.93 | 8009 | -52.93 | 8009 | -115.73 | 7396 |
| Span Avg | ---- | ---- | 20179 | ---- | 20179 | ---- | 19995 |
| 4 Left | 0.150 | -58.35 | 7837 | -58.35 | 7837 | -127.56 | 7380 |
| Middle | 0.850 | 27.19 | 25395 | 27.19 | 25395 | 59.43 | 25395 |
| Span Avg | ---- | ---- | 22761 | ---- | 22761 | ---- | 22693 |
| 5 Left | 1.000 | -0.52 | 433026 | -0.52 | 433026 | -1.14 | 433026 |
| Span Avg | ---- | ---- | 433026 | ---- | 433026 | ---- | 433026 |

Strip Section Properties at Midspan

Units: Ig (in⁴)

| Span | Column Strip | | | Middle Strip | | |
|------|--------------|-------|-------|--------------|-------|-------|
| | Ig | LDf | Ratio | Ig | LDf | Ratio |
| 1 | 20040.5 | 0.781 | 0.990 | 2862 | 0.219 | 1.943 |
| 2 | 20040.5 | 0.693 | 0.878 | 2862 | 0.307 | 2.723 |
| 3 | 20040.5 | 0.673 | 0.853 | 2862 | 0.327 | 2.903 |
| 4 | 20040.5 | 0.693 | 0.878 | 2862 | 0.307 | 2.723 |
| 5 | 20040.5 | 0.781 | 0.990 | 2862 | 0.219 | 1.943 |

NOTES: Load distribution factor, LDL, averages moment distribution factors listed in [2] Design Results.
 Ratio refers to proportion of strip to frame deflections under fix-end conditions.

Instantaneous Deflections

Extreme Instantaneous Frame Deflections and Corresponding Locations

Units: Def (in), Loc (ft)

| Span | Direction | Value | Dead | Live | | Total | Total | |
|------|-----------|-------|--------|-----------|-------------|--------|-----------|-----------|
| | | | | Sustained | Unsustained | | Sustained | Dead+Live |
| 1 | Down | Def | --- | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- | --- |
| | Up | Def | -0.001 | --- | -0.001 | -0.001 | -0.001 | -0.003 |
| | | Loc | 0.000 | --- | 0.000 | 0.000 | 0.000 | 0.000 |
| 2 | Down | Def | 0.011 | --- | 0.013 | 0.013 | 0.011 | 0.024 |
| | | Loc | 8.000 | --- | 8.000 | 8.000 | 8.000 | 8.000 |
| | Up | Def | --- | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- | --- |
| 3 | Down | Def | 0.006 | --- | 0.007 | 0.007 | 0.006 | 0.013 |
| | | Loc | 8.750 | --- | 8.750 | 8.750 | 8.750 | 8.750 |
| | Up | Def | -0.000 | --- | -0.000 | -0.000 | -0.000 | -0.001 |
| | | Loc | 1.000 | --- | 1.000 | 1.000 | 1.000 | 1.000 |
| 4 | Down | Def | 0.011 | --- | 0.013 | 0.013 | 0.011 | 0.024 |
| | | Loc | 9.500 | --- | 9.500 | 9.500 | 9.500 | 9.500 |
| | Up | Def | --- | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- | --- |
| 5 | Down | Def | --- | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- | --- |
| | Up | Def | -0.001 | --- | -0.001 | -0.001 | -0.001 | -0.003 |
| | | Loc | 0.750 | --- | 0.750 | 0.750 | 0.750 | 0.750 |

Extreme Instantaneous Column Strip Deflections and Corresponding Locations

Units: Def (in), Loc (ft)

| Span | Direction | Value | Dead | Live | | Total | Total | |
|------|-----------|-------|--------|-----------|-------------|--------|-----------|-----------|
| | | | | Sustained | Unsustained | | Sustained | Dead+Live |
| 1 | Down | Def | --- | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- | --- |
| | Up | Def | -0.001 | --- | -0.001 | -0.001 | -0.001 | -0.003 |
| | | Loc | 0.000 | --- | 0.000 | 0.000 | 0.000 | 0.000 |
| 2 | Down | Def | 0.010 | --- | 0.012 | 0.012 | 0.010 | 0.023 |
| | | Loc | 8.000 | --- | 8.000 | 8.000 | 8.000 | 8.000 |
| | Up | Def | --- | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- | --- |
| 3 | Down | Def | 0.005 | --- | 0.006 | 0.006 | 0.005 | 0.011 |
| | | Loc | 8.750 | --- | 8.750 | 8.750 | 8.750 | 8.750 |
| | Up | Def | -0.000 | --- | -0.000 | -0.000 | -0.000 | -0.001 |
| | | Loc | 1.000 | --- | 1.000 | 1.000 | 1.000 | 1.000 |
| 4 | Down | Def | 0.010 | --- | 0.012 | 0.012 | 0.010 | 0.023 |
| | | Loc | 9.500 | --- | 9.500 | 9.500 | 9.500 | 9.500 |
| | Up | Def | --- | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- | --- |
| 5 | Down | Def | --- | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- | --- |
| | Up | Def | -0.001 | --- | -0.001 | -0.001 | -0.001 | -0.003 |
| | | Loc | 0.750 | --- | 0.750 | 0.750 | 0.750 | 0.750 |

Extreme Instantaneous Middle Strip Deflections and Corresponding Locations

Units: Def (in), Loc (ft)

| Span | Direction | Value | Dead | Live | | Total | Total | |
|------|-----------|-------|--------|-----------|-------------|--------|-----------|-----------|
| | | | | Sustained | Unsustained | | Sustained | Dead+Live |
| 1 | Down | Def | --- | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- | --- |
| | Up | Def | -0.001 | --- | -0.001 | -0.001 | -0.001 | -0.003 |
| | | Loc | 0.000 | --- | 0.000 | 0.000 | 0.000 | 0.000 |
| 2 | Down | Def | 0.022 | --- | 0.026 | 0.026 | 0.022 | 0.049 |
| | | Loc | 8.500 | --- | 8.500 | 8.500 | 8.500 | 8.500 |
| | Up | Def | --- | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- | --- |
| 3 | Down | Def | 0.020 | --- | 0.024 | 0.024 | 0.020 | 0.044 |
| | | Loc | 8.750 | --- | 8.750 | 8.750 | 8.750 | 8.750 |
| | Up | Def | -0.000 | --- | -0.000 | -0.000 | -0.000 | -0.000 |
| | | Loc | 0.750 | --- | 0.750 | 0.750 | 0.750 | 0.750 |

| | | | | | | | | |
|---|------|-----|--------|-----|--------|--------|--------|--------|
| 4 | Down | Def | 0.022 | --- | 0.026 | 0.026 | 0.022 | 0.049 |
| | | Loc | 9.000 | --- | 9.000 | 9.000 | 9.000 | 9.000 |
| | Up | Def | --- | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- | --- |
| 5 | Down | Def | --- | --- | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- | --- | --- |
| | Up | Def | -0.001 | --- | -0.001 | -0.001 | -0.001 | -0.003 |
| | | Loc | 0.750 | --- | 0.750 | 0.750 | 0.750 | 0.750 |

Long-term Deflections

=====

Long-term Column Strip Deflection Factors

Time dependant factor for sustained loads = 2.000

Units: Astop, Asbot (in^2), b, d (in), Rho' (%), Lambda (-)

| Span | Zone | M+ve | | | | M-ve | | | |
|------|---------|-------|------|------|-------------|-------|------|------|-------------|
| | | Astop | b | d | Rho' Lambda | Asbot | b | d | Rho' Lambda |
| 1 | Right | ---- | ---- | ---- | 0.000 2.000 | ---- | ---- | ---- | 0.000 2.000 |
| 2 | Midspan | ---- | ---- | ---- | 0.000 2.000 | ---- | ---- | ---- | 0.000 2.000 |
| 3 | Midspan | ---- | ---- | ---- | 0.000 2.000 | ---- | ---- | ---- | 0.000 2.000 |
| 4 | Midspan | ---- | ---- | ---- | 0.000 2.000 | ---- | ---- | ---- | 0.000 2.000 |
| 5 | Left | ---- | ---- | ---- | 0.000 2.000 | ---- | ---- | ---- | 0.000 2.000 |

NOTES: Deflection multiplier, Lambda, depends on moment sign at sustained load level and Rho' in given zone.
 Rho' is assumed zero because Compression Reinforcement option is NOT selected in Solve Options.

Long-term Middle Strip Deflection Factors

Time dependant factor for sustained loads = 2.000

Units: Astop, Asbot (in^2), b, d (in), Rho' (%), Lambda (-)

| Span | Zone | M+ve | | | | M-ve | | | |
|------|---------|-------|------|------|-------------|-------|------|------|-------------|
| | | Astop | b | d | Rho' Lambda | Asbot | b | d | Rho' Lambda |
| 1 | Right | ---- | ---- | ---- | 0.000 2.000 | ---- | ---- | ---- | 0.000 2.000 |
| 2 | Midspan | ---- | ---- | ---- | 0.000 2.000 | ---- | ---- | ---- | 0.000 2.000 |
| 3 | Midspan | ---- | ---- | ---- | 0.000 2.000 | ---- | ---- | ---- | 0.000 2.000 |
| 4 | Midspan | ---- | ---- | ---- | 0.000 2.000 | ---- | ---- | ---- | 0.000 2.000 |
| 5 | Left | ---- | ---- | ---- | 0.000 2.000 | ---- | ---- | ---- | 0.000 2.000 |

NOTES: Deflection multiplier, Lambda, depends on moment sign at sustained load level and Rho' in given zone.
 Rho' is assumed zero because Compression Reinforcement option is NOT selected in Solve Options.

Extreme Long-term Column Strip Deflections and Corresponding Locations

Units: D (in), x (ft)

| Span | Direction | Value | cs | cs+lu | cs+l | Total |
|------|-----------|-------|--------|--------|--------|--------|
| 1 | Down | Def | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- |
| | Up | Def | -0.002 | -0.004 | -0.004 | -0.005 |
| | | Loc | 0.000 | 0.000 | 0.000 | 0.000 |
| 2 | Down | Def | 0.021 | 0.033 | 0.033 | 0.043 |
| | | Loc | 8.000 | 8.000 | 8.000 | 8.000 |
| | Up | Def | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- |
| 3 | Down | Def | 0.010 | 0.015 | 0.015 | 0.020 |
| | | Loc | 8.750 | 8.750 | 8.750 | 8.750 |
| | Up | Def | -0.001 | -0.001 | -0.001 | -0.001 |
| | | Loc | 1.000 | 1.000 | 1.000 | 1.000 |
| 4 | Down | Def | 0.021 | 0.033 | 0.033 | 0.043 |
| | | Loc | 9.500 | 9.500 | 9.500 | 9.500 |
| | Up | Def | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- |
| 5 | Down | Def | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- |
| | Up | Def | -0.002 | -0.004 | -0.004 | -0.005 |
| | | Loc | 0.750 | 0.750 | 0.750 | 0.750 |

NOTES: Incremental deflections due to creep and shrinkage (cs) based on sustained load level values.
 Incremental deflections after partitions are installed can be estimated by deflections due to:
 - creep and shrinkage plus unsustained live load (cs+lu), if live load applied before partitions,
 - creep and shrinkage plus live load (cs+l), if live load applied after partitions.
 Total deflections consist of dead, live, and creep and shrinkage deflections.

Extreme Long-term Middle Strip Deflections and Corresponding Locations

Units: D (in), x (ft)

| Span | Direction | Value | cs | cs+lu | cs+l | Total |
|------|-----------|-------|--------|--------|--------|--------|
| 1 | Down | Def | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- |
| | Up | Def | -0.002 | -0.004 | -0.004 | -0.005 |
| | | Loc | 0.000 | 0.000 | 0.000 | 0.000 |
| 2 | Down | Def | 0.044 | 0.071 | 0.071 | 0.093 |
| | | Loc | 8.500 | 8.500 | 8.500 | 8.500 |
| | Up | Def | --- | --- | --- | --- |

| | | | | | | |
|---|------|-----|--------|--------|--------|--------|
| | | Loc | --- | --- | --- | --- |
| 3 | Down | Def | 0.040 | 0.064 | 0.064 | 0.084 |
| | | Loc | 8.750 | 8.750 | 8.750 | 8.750 |
| | Up | Def | -0.000 | -0.001 | -0.001 | -0.001 |
| | | Loc | 0.750 | 0.750 | 0.750 | 0.750 |
| 4 | Down | Def | 0.044 | 0.071 | 0.071 | 0.093 |
| | | Loc | 9.000 | 9.000 | 9.000 | 9.000 |
| | Up | Def | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- |
| 5 | Down | Def | --- | --- | --- | --- |
| | | Loc | --- | --- | --- | --- |
| | Up | Def | -0.002 | -0.004 | -0.004 | -0.005 |
| | | Loc | 0.750 | 0.750 | 0.750 | 0.750 |

NOTES: Incremental deflections due to creep and shrinkage (cs) based on sustained load level values.
Incremental deflections after partitions are installed can be estimated by deflections due to:
- creep and shrinkage plus unsustained live load (cs+lu), if live load applied before partitions,
- creep and shrinkage plus live load (cs+l), if live load applied after partitions.
Total deflections consist of dead, live, and creep and shrinkage deflections.

7. Summary and Comparison of Design Results

| Table 9 - Comparison of Moments obtained from Hand (EFM) and spSlab Solution (ft-kip) | | | |
|--|---------------------|-------------------|---------------|
| | | Hand (EFM) | spSlab |
| Exterior Span | | | |
| Beam Strip | Exterior Negative * | 38.4 | 40 |
| | Positive | 50.9 | 48.17 |
| | Interior Negative * | 73.1 | 80.63 |
| Column Strip | Exterior Negative * | 6.8 | 7.06 |
| | Positive | 9 | 8.5 |
| | Interior Negative * | 12.9 | 14.23 |
| Middle Strip | Exterior Negative * | 15 | 15.36 |
| | Positive | 29.5 | 27.55 |
| | Interior Negative * | 42.4 | 46.12 |
| Interior Span | | | |
| Beam Strip | Interior Negative * | 67 | 73.15 |
| | Positive | 40.6 | 36.65 |
| Column Strip | Interior Negative * | 11.8 | 12.91 |
| | Positive | 7.2 | 6.47 |
| Middle Strip | Interior Negative * | 38.8 | 41.84 |
| | Positive | 23.5 | 20.96 |
| * negative moments are taken at the faces of supports | | | |

| Table 10 - Comparison of Reinforcement Results | | | | | | | |
|---|-------------------|---|---------------|--|---------------|-------------------------------------|---------------|
| Span Location | | Reinforcement Provided for Flexure | | Additional Reinforcement Provided for Unbalanced Moment Transfer* | | Total Reinforcement Provided | |
| | | Hand | spSlab | Hand | spSlab | Hand | spSlab |
| Exterior Span | | | | | | | |
| Beam Strip | Exterior Negative | 4 - #4 | 4 - #4 | n/a | n/a | 4 - #4 | 4 - #4 |
| | Positive | 5 - #4 | 4 - #4 | n/a | n/a | 5 - #4 | 4 - #4 |
| | Interior Negative | 5 - #4 | 5 - #4 | --- | --- | 5 - #4 | 5 - #4 |
| Column Strip | Exterior Negative | 8 - #4 | 8 - #4 | 10 - #4 | 12 - #4 | 18 - #4 | 20 - #4 |
| | Positive | 8 - #4 | 8 - #4 | n/a | n/a | 8 - #4 | 8 - #4 |
| | Interior Negative | 8 - #4 | 8 - #4 | --- | --- | 8 - #4 | 8 - #4 |
| Middle Strip | Exterior Negative | 14 - #4 | 14 - #4 | n/a | n/a | 14 - #4 | 14 - #4 |
| | Positive | 14 - #4 | 14 - #4 | n/a | n/a | 14 - #4 | 14 - #4 |
| | Interior Negative | 14 - #4 | 14 - #4 | n/a | n/a | 14 - #4 | 14 - #4 |
| Interior Span | | | | | | | |
| Beam Strip | Positive | 4 - #4 | 4 - #4 | n/a | n/a | 4 - #4 | 4 - #4 |
| Column Strip | Positive | 8 - #4 | 8 - #4 | n/a | n/a | 8 - #4 | 8 - #4 |
| Middle Strip | Positive | 14 - #4 | 14 - #4 | n/a | n/a | 14 - #4 | 14 - #4 |

| Table 11 - Comparison of Beam Shear Reinforcement Results | | |
|--|-------------------------------|------------------|
| Span Location | Reinforcement Provided | |
| | Hand | spSlab |
| End Span | | |
| Exterior | 8 - #4 @ 8 in | 8 - #4 @ 8 in |
| Interior | 10 - #4 @ 8.6 in | 10 - #4 @ 8.6 in |
| Interior Span | | |
| Interior | 9 - #4 @ 8.6 in | 10 - #4 @ 8.6 in |

| Table 12 - Comparison of Two-Way (Punching) Shear Check Results (around Columns Faces) | | | | | | | | | | |
|---|--------------------------|--------|-------------|--------|---------------------|--------|--------------|--------|------------------|--------|
| Support | b_1 , in. | | b_2 , in. | | b_o , in. | | V_u , kips | | c_{AB} , in. | |
| | Hand | spSlab | Hand | spSlab | Hand | spSlab | Hand | spSlab | Hand | spSlab |
| Exterior | 20.5 | 20.5 | 23.0 | 44.0 | 64 | 64 | 43.56 | 48.47 | 9.09 | 9.09 |
| Interior | 23.0 | 23.0 | 23.0 | 23.0 | 92 | 92 | 104.76 | 104.50 | 11.50 | 11.50 |
| Support | J_c , in. ⁴ | | γ_v | | M_{unb} , ft-kips | | v_u , psi | | ϕv_c , psi | |
| | Hand | spSlab | Hand | spSlab | Hand | spSlab | Hand | spSlab | Hand | spSlab |
| Exterior | 95338 | 95338 | 0.386 | 0.313 | 84.37 | 83.49 | 76.8 | 73.8 | 189.7 | 189.7 |
| Interior | 114993 | 114990 | 0.400 | 0.400 | 14.10 | 16.77 | 91.0 | 92.1 | 189.7 | 189.7 |

| Table 13 - Comparison of Immediate Deflection Results (in.) | | | | | | | | | |
|--|-------|--------|---------------------|--------|----------------------|--------|-------|--------|--|
| Column Strip | | | | | | | | | |
| Span | D | | D+LL _{sus} | | D+LL _{full} | | LL | | |
| | Hand | spSlab | Hand | spSlab | Hand | spSlab | Hand | spSlab | |
| Exterior | 0.009 | 0.010 | 0.009 | 0.010 | 0.021 | 0.023 | 0.011 | 0.012 | |
| Interior | 0.004 | 0.005 | 0.004 | 0.005 | 0.010 | 0.011 | 0.005 | 0.006 | |
| Middle Strip | | | | | | | | | |
| Span | D | | D+LL _{sus} | | D+LL _{full} | | LL | | |
| | Hand | spSlab | Hand | spSlab | Hand | spSlab | Hand | spSlab | |
| Exterior | 0.021 | 0.022 | 0.021 | 0.022 | 0.047 | 0.049 | 0.025 | 0.026 | |
| Interior | 0.019 | 0.020 | 0.019 | 0.020 | 0.042 | 0.044 | 0.023 | 0.024 | |

| Table 14 - Comparison of Time-Dependent Deflection Results | | | | | | | |
|---|------------------|--------|---------------------|--------|------------------------|--------|--|
| Column Strip | | | | | | | |
| Span | λ_Δ | | Δ_{cs} , in. | | Δ_{total} , in. | | |
| | Hand | spSlab | Hand | spSlab | Hand | spSlab | |
| Exterior | 2.0 | 2.0 | 0.019 | 0.021 | 0.040 | 0.043 | |
| Interior | 2.0 | 2.0 | 0.009 | 0.010 | 0.018 | 0.020 | |
| Middle Strip | | | | | | | |
| Span | λ_Δ | | Δ_{cs} , in. | | Δ_{total} , in. | | |
| | Hand | spSlab | Hand | spSlab | Hand | spSlab | |
| Exterior | 2.0 | 2.0 | 0.043 | 0.044 | 0.089 | 0.093 | |
| Interior | 2.0 | 2.0 | 0.038 | 0.040 | 0.080 | 0.084 | |

In all of the hand calculations illustrated above, the results are in close or exact agreement with the automated analysis and design results obtained from the spSlab model. Excerpts of spSlab graphical and text output are given below for illustration.

8. Conclusions & Observations

A slab system can be analyzed and designed by any procedure satisfying equilibrium and geometric compatibility. Three established methods are widely used. The requirements for two of them are described in detail in ACI 318-14 Chapter 8 (8.2.1).

Direct Design Method (DDM) is an approximate method and is applicable to two-way slab concrete floor systems that meet the stringent requirements of ACI 318-14 (8.10.2). In many projects, however, these requirements limit the usability of the Direct Design Method significantly.

The Equivalent Frame Method (EFM) does not have the limitations of Direct Design Method. It requires more accurate analysis methods that, depending on the size and geometry can prove to be long, tedious, and time-consuming.

StructurePoint's [spSlab](#) software program solution utilizes the Equivalent Frame Method to automate the process providing considerable time-savings in the analysis and design of two-way slab systems as compared to hand solutions using DDM or EFM.

Finite Element Method (FEM) is another method for analyzing reinforced concrete slabs, particularly useful for irregular slab systems with variable thicknesses, openings, and other features not permissible in DDM or EFM. Many reputable commercial FEM analysis software packages are available on the market today such as [spMats](#). Using FEM requires critical understanding of the relationship between the actual behavior of the structure and the numerical simulation since this method is an approximate numerical method. The method is based on several assumptions and the operator has a great deal of decisions to make while setting up the model and applying loads and boundary conditions. The results obtained from FEM models should be verified to confirm their suitability for design and detailing of concrete structures.

The following table shows a general comparison between the DDM, EFM and FEM. This table covers general limitations, drawbacks, advantages, and cost-time efficiency of each method where it helps the engineer in deciding which method to use based on the project complexity, schedule, and budget.

| Applicable ACI 318-14 Provision | Limitations/Applicability | Concrete Slab Analysis Method | | |
|--|--|---|---|--|
| | | DDM (Hand) | EFM (Hand//spSlab) | FEM (spMats) |
| 8.10.2.1 | Minimum of three continuous spans in each direction | <input checked="" type="checkbox"/> | | |
| 8.10.2.2 | Successive span lengths measured center-to-center of supports in each direction shall not differ by more than one-third the longer span | <input checked="" type="checkbox"/> | | |
| 8.10.2.3 | Panels shall be rectangular, with ratio of longer to shorter panel dimensions, measured center-to-center supports, not exceed 2. | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> | |
| 8.10.2.4 | Column offset shall not exceed 10% of the span in direction of offset from either axis between centerlines of successive columns | <input checked="" type="checkbox"/> | | |
| 8.10.2.5 | All loads shall be due to gravity only | <input checked="" type="checkbox"/> | | |
| 8.10.2.5 | All loads shall be uniformly distributed over an entire panel (q_u) | <input checked="" type="checkbox"/> | | |
| 8.10.2.6 | Unfactored live load shall not exceed two times the unfactored dead load | <input checked="" type="checkbox"/> | | |
| 8.10.2.7 | For a panel with beams between supports on all sides, slab-to-beam stiffness ratio shall be satisfied for beams in the two perpendicular directions. | <input checked="" type="checkbox"/> | | |
| 8.7.4.2 | Structural integrity steel detailing | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> |
| 8.5.4 | Openings in slab systems | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> |
| 8.2.2 | Concentrated loads | Not permitted | <input checked="" type="checkbox"/> | <input checked="" type="checkbox"/> |
| 8.11.1.2 | Live load arrangement (Load Patterning) | Not required | Required | Engineering judgment required based on modeling technique |
| R8.10.4.5 ^e | Reinforcement for unbalanced slab moment transfer to column (M_{sc}) | Moments @ support face | Moments @ support centerline | Engineering judgment required based on modeling technique |
| | Irregularities (i.e. variable thickness, non-prismatic, partial bands, mixed systems, support arrangement, etc.) | Not permitted | Engineering judgment required | Engineering judgment required |
| Complexity | | Low | Average | Complex to very complex |
| Design time/costs | | Fast | Limited | Unpredictable/Costly |
| Design Economy | | Conservative (see detailed comparison with spSlab output) | Somewhat conservative | Unknown - highly dependent on modeling assumptions: 1. Linear vs. non-linear 2. Isotropic vs non-isotropic 3. Plate element choice 4. Mesh size and aspect ratio 5. Design & detailing features |
| General (Drawbacks) | | Very limited applications | Limited geometry | Limited guidance non-standard application (user dependent). Required significant engineering judgment |
| General (Advantages) | | Very limited analysis is required | Detailed analysis is required or via software (e.g. spSlab) | Unlimited applicability to handle complex situations permissible by the features of the software used (e.g. spMats) |

^e The unbalanced slab moment transferred to the column M_{sc} (M_{unb}) is the difference in slab moment on either side of a column at a specific joint. In DDM only moments at the face of the support are calculated and are also used to obtain M_{sc} (M_{unb}). In EFM where a frame analysis is used, moments at the column center line are used to obtain M_{sc} (M_{unb}).