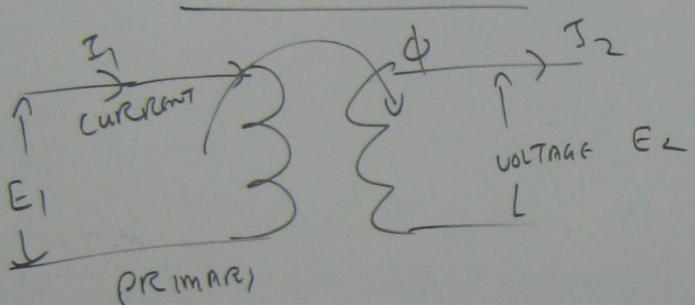


## TRANSFORMER

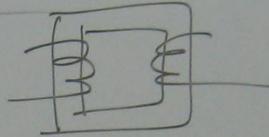


$$\frac{E_1}{E_2} = \frac{I_2}{I_1} = \frac{N_1}{N_2} = a$$

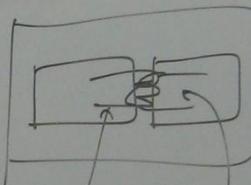
IRON CORE - LAMINATED CORE  
TO REDUCE EDDY CURRENT LOSS.

### CORE CONSTRUCTION

SHELL



CORE



PRIMARY      SECONDARY  
WINDING

TRANSFORMER VOLTAGE  
EQUATION

$$E = 4.44 f N \phi$$

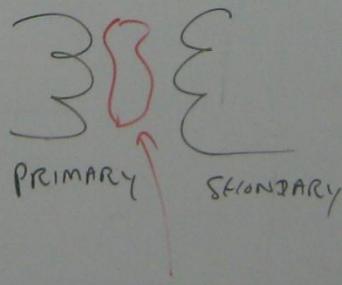
$f$  = frequency (Hz)

$N$  = No. of turns

$\phi$  = Flux (wb)

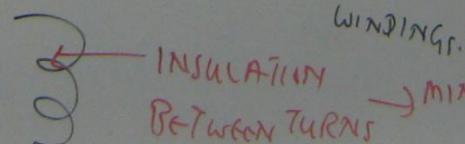
$$\phi = \text{flux density} \times \text{core C.S.A}$$

$$\phi = B \times A$$



### INSULATION

MAJOR INSULATION - INSULATION BETWEEN



INSULATION

BETWEEN TURNS

MINOR INSULATION

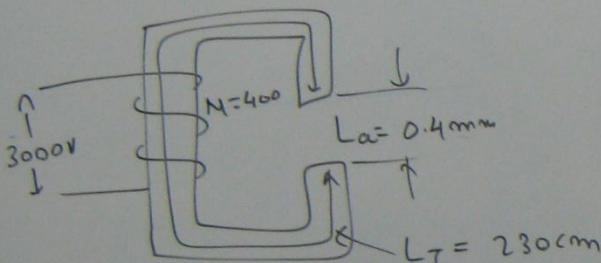
P)

CALCULATE IRON CORE FLUX DENSITY AND RMS

MAGNETIZING CURRENT FOR THE FOLLOWING 1φ

TRANSFORMER

$$N_p = 400 \quad E_p = 3000 \text{ V (Rms)}, \text{ CORE CSA} = 200 \text{ } \text{mm}^2$$
$$\text{CORE LENGTH} = 230 \text{ cm}, \text{ AIR GAP} = 0.4 \text{ mm} \quad \mu_\infty = 1900$$



$$H \times L = N \times I$$

MAGNETIZING

$$\text{FORCE} = \frac{\text{FLUX DENSITY}}{\text{PERMEABILITY}}$$
$$= \frac{B}{\mu}$$

$$H_a \times L_a + H_I \times L_I = N \times I$$
$$\frac{B}{\mu} \times L_a + \frac{B}{\mu} L_I = N \times I$$
$$\frac{\phi}{\mu_0} \times \frac{0.4}{1000} + \frac{\phi}{\mu_r \mu_0} \times \frac{230}{100} = 400 \times I$$

$$I = 4.8 \text{ A} \\ (\text{MAX})$$

$$I_{\text{rms}} = \frac{I_{\text{MAX}}}{\sqrt{2}}$$
$$= \frac{4.8}{\sqrt{2}}$$
$$= 3.42 \text{ Amp}$$

$$E = 4.44 f \phi N$$
$$3000 = 4.44 \times 50 \times \phi \times 400$$

$$\phi = 0.028 \text{ wb}$$

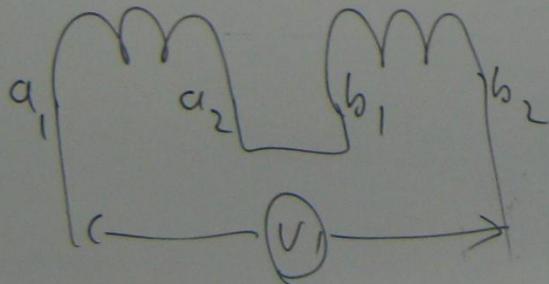
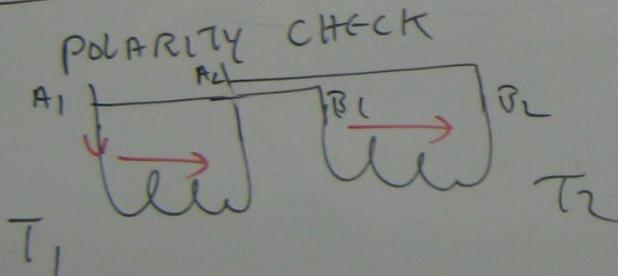
$$\frac{0.028 / 200 \times 10^{-4}}{4\pi \times 10^{-7}} \times \frac{0.4}{100} + \frac{0.028 / 200 \times 10^{-4}}{1900 \times 4\pi \times 10^{-7}} \times \frac{230}{100} = 400 \times I$$

Transformer cooling - AIR  
 FREE from moisture  
 SILICA GEL

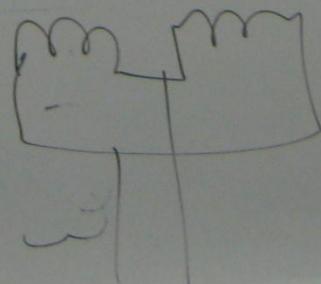
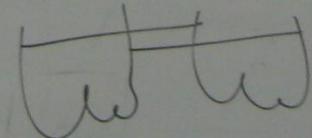
OIL  
 LOW VISCOSITY  
 HIGH FLASH POINT  
 LOW ACIDITY  
 LOW SLUDGE  
 HIGH INSULATION PROPERTIES

AS 1767, AS 1883 → TRANSFORMER OIL

PARALLEL CONNECTION



$V_1 \approx 0$   
 THEN CONNECT



$V \approx$  LINE VOLTAGE  
 CHANGE THE CONNECTION & TEST AGAIN

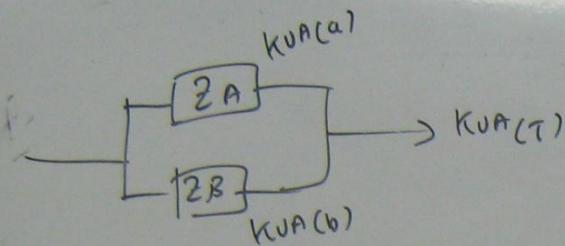
(b) Transformer (A) RATED 15 MVA  
 $\gamma_{2a} = 3 + j 6 \gamma$ .

Transformer (B) RATED 30 MVA

$$\gamma_{2b} = 4 + j 8 \gamma.$$

CALCULATE (a)  $\gamma_2$  of 30 MVA Transformer  
 BASED ON 15 MVA

(b) MVA supplied by  
 EACH TRANSFORMER WITH  
 THE COMBINATION OF  
 THEM ARE SUPPLYING  
 12 MVA UNITY P.F



$$KVA(a) = \frac{Z_B}{Z_A + Z_B} \times KVA(T)$$

$$KVA(b) = \frac{Z_A}{Z_A + Z_B} \times KVA(T)$$

$$\therefore X_2 = \frac{MVA(BASE)}{MVA_1} \times Y_1$$

$$(a) Z_2 = \frac{MVA(BASE)}{MVA_1} \times Z_1 \\ = \frac{15}{30} (4+j8)$$

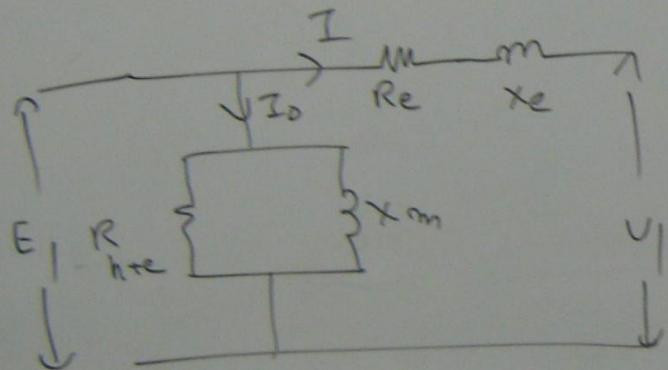
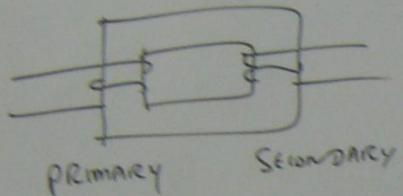
$$Z_B = 2+j4 \quad \text{Base on } 15 \text{ MVA}$$

$$Z_A = 3+j6 \quad \text{Base on } 15 \text{ MVA}$$

$$\begin{aligned} KVA(a) &= \frac{Z_B}{Z_A + Z_B} \times KVA(T) \\ &= \frac{2+j4}{3+j6+2+j4} \times 12 \\ &= \frac{\sqrt{2^2+4^2}}{\sqrt{3^2+6^2}} \times 12 \\ &= 4.79 \text{ MVA} \end{aligned}$$

$$\begin{aligned} KVA(b) &= \frac{Z_A}{Z_A + Z_B} \times 12 \\ &= \frac{3+j6}{3+j6+2+j4} \times 12 \\ &= \frac{\sqrt{3^2+6^2}}{\sqrt{5^2+10^2}} \times 12 = 7.19 \end{aligned}$$

## TRANSFORMER EQUIVALENT CIRCUIT



$$R_{eq} = R_1 + a^2 R_2$$

$R_1$  = PRIMARY WINDING RESISTANCE

$R_2$  = SECONDARY WINDING RESISTANCE

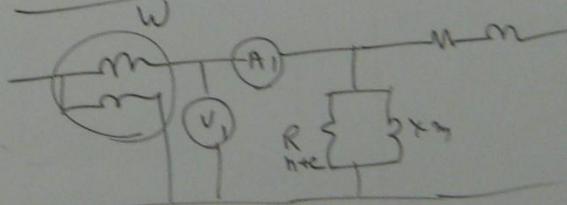
$a = \frac{N_1}{N_2} = \text{TURN RATIO}$

$$X_e = X_1 + a^2 X_2$$

$R_{h+e}$  = CORE RESISTANCE

$X_m$  = CORE INDUCTIVE REACTANCE

OPEN CIRCUIT TEST



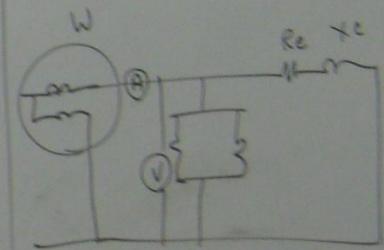
$$R_{h+e} = \frac{V^2}{W}$$

$$\text{VAR} = \sqrt{(V^2) - (W)^2}$$

$$X_m = \frac{V^2}{\text{VAR}}$$

SHORT CIRCUIT TEST

L.V WINDING SIDE IS  
SHORT CIRCUTED

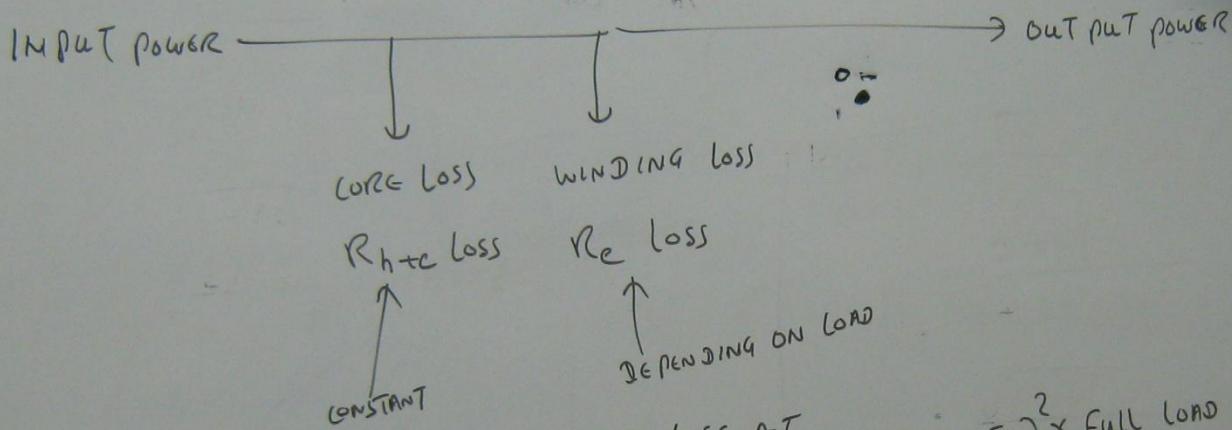


$$I^2 R_e = W$$

$$R_e = \frac{W}{I^2}$$

$$Z_e = \frac{V}{I}$$

$$X_e = \sqrt{Z_e^2 - R_e^2}$$



WINDING LOSS AT ANY LOAD =  $(\text{LOAD RATIO})^2 \times \text{Full load copper loss}$

(COPPER LOSS)

$$\frac{1}{2} \text{ LOAD copper loss} = \left(\frac{1}{2}\right)^2 \times \text{Full load copper loss}$$

TRANSFORMER MAXIMUM EFFICIENCY

CONSTANT LOSS = VARIABLE LOSS  
 (CORE LOSS)                  (COPPER LOSS)

$\times 12 = 19$

Pb THE FOLLOWINGS ARE TEST RESULTS OF 3 $\phi$  66/11kV 30 mVA

$Y/Y$  TRANSFORMER

NO LOAD TEST

$$\text{L.V SIDE} = 11\text{kV}, \text{L.V SIDE CURRENT} = 50 \text{ Amp}$$

VOLTAGE POWER = 25 kW

SHORT CIRCUIT TEST

$$\text{LINE VOLTAGE} = 1650\text{V}, \text{LINE TO LINE CURRENT} = \text{RATED CURRENT}$$

POWER = 20 kW.

$$R_{h+c} = \frac{U_{ph}^2}{14 \text{ NO LOAD POWER}} = \frac{(11000/\sqrt{3})^2}{25000} = 4840\Omega$$

$$I_m = \sqrt{I^2 - I_{h+c}^2} = \sqrt{50^2 - \left(\frac{U_{ph}}{R_{h+c}}\right)^2} = \sqrt{50^2 - \left(\frac{11000/\sqrt{3}}{4840}\right)^2}$$

$$I_m = 49.98 \text{ Amp}$$

$$X_m = \frac{U_{ph}}{I_m} = \frac{11000/\sqrt{3}}{49.98} = 127.05 \Omega$$

SHORT CIRCUIT TEST

$$I^2 \times R_{eq} = 14 \text{ SHORT CIRCUIT POWER}$$

$$\left( \frac{30 \times 10^6}{\sqrt{3} \times 66 \times 10^3} \right)^2 \times R_{eq} = \frac{20 \times 10^3}{3}$$

$$R_{eq} = 0.097 \Omega$$

$$Z_{eq} = \frac{U_{ph}}{I} = \frac{1650/\sqrt{3}}{\frac{30 \times 10^6}{\sqrt{3} \times 66 \times 10^3}}$$

$$= 3.63 \Omega$$

$$X'_{eq} = \sqrt{Z_{eq}'^2 - (R_{eq}')^2}$$

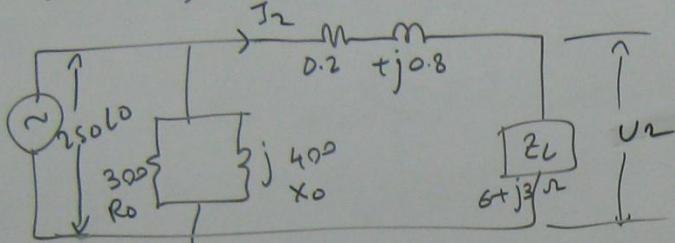
$$= \sqrt{3.63^2 - 0.097^2}$$

$$= 3.62 \Omega$$

$$R_{h+c}' = q^2 (R_{h+c}''') = \left( \frac{66}{11} \right)^2 \times 4840$$

(ph)

IN THE FOLLOWING PROBLEM, FIND (a) IRON LOSS, (b) SECONDARY LOAD  
CURRENT (c) COPPER LOSS (d) LOAD POWER (e) EFFICIENCY



$$(a) \text{IRON LOSS} = \frac{U^2}{R_o} = \frac{250^2}{300} = 208.1 \text{ WATT}$$

$$\begin{aligned}(b) I_2 &= \frac{V}{Z_c + Z_L} \\&= \frac{250}{0.2 + j0.8 + 6 + j3} \\&= \frac{250}{6.2 + j3.8} \\&= \frac{250}{\sqrt{6.2^2 + 3.8^2}} = 34.38 \text{ Amp}\end{aligned}$$

;

$$\begin{aligned}(c) \text{COPPER LOSS} &= I^2 R_e \\&= (34.38)^2 \times 0.2 \\&= 236.39 \text{ WATT}\end{aligned}$$

$$\begin{aligned}(d) \text{LOAD POWER} &= I^2 L \times R_L = 34.38^2 \times 6 \\&= 7075 \text{ WATT}\end{aligned}$$

$$\text{INPUT} = \text{LOAD POWER} + \text{COPPER LOSS} + \text{IRON LOSS}$$

$$\begin{aligned}&= 7075 + 236.39 + 208.1 \\&\approx 7536 \text{ WATT}\end{aligned}$$

$$\% \text{EFFICIENCY} = \frac{\text{OUTPUT}}{\text{INPUT}} \times 100$$

$$= \frac{7075}{7536} \times 100 = 94.1\%$$

uit

4840

Transformer at load

% Regulation (Voltage Drop)

Efficiency  $\longleftrightarrow$  Full Day Efficiency

$$\% \text{ Voltage Regulation} = \% R_{cos\theta} \pm \% X \sin\theta$$

+ LAGGING  
- LEADING

$$\% R = \frac{IR}{V_{ph}} \times 100$$

$$1.8 = \frac{75.76 \times R}{66 \times 10^3} \times 100$$

$$R = 1.57 \Omega$$

$$\% X = \frac{IX}{V_{ph}} \times 100$$

$$5 = \frac{75.76 \times X}{66 \times 10^3} \times 100$$

$$X = 4.36 \Omega$$

$$\begin{aligned} \text{Full Load Loss} &= 3 I_{FL}^2 \times R \\ \text{Copper Loss} &= 3(75.76)^2 \times 1.57 \end{aligned}$$

$\frac{1}{4}$  Load  $\rightarrow$  Maximum Efficiency

$$\text{Iron Loss} = \frac{1}{4} \text{ Load Copper Loss}$$

$$\begin{aligned} \text{Iron Loss} &= \left(\frac{1}{4}\right)^2 \times 3(75.76)^2 \times 1.57 \\ &= 1689 \text{ W} \end{aligned}$$

Pb A 1500 kVA 6600/415V 3 $\phi$   $\Delta/\lambda$  Transformer

$$\% R = 1.8, \% X = 5$$

MAXIMUM EFFICIENCY OCCURS AT  $\frac{1}{4}$  LOAD  
CALCULATE (a) IRON LOSS (b), MAX. EFFICIENCY AT 0.9 PF LAGGING

(c) FULL LOAD % REGULATION AT 0.8 PF LEADING.

$$I_{LINE} = \frac{KVA \times 10^3}{\sqrt{3} V} = \frac{1500 \times 10^3}{1.732 \times 6600} = 131.2 \text{ Amp}$$

$$I_{ph} = \frac{I_{LINE}}{\sqrt{3}} = \frac{131.2}{1.732} = 75.76 \text{ Amp}$$

$$O/P \text{ at } 0.9 \text{ P.F lagging} = 1500 \text{ kW} \times \text{P.F}$$

$$= 1500 \times 0.9$$

$$\text{MAX EFFICIENCY} = \frac{1}{4} \text{ LOAD} = \frac{1}{4} \times 1500 \times 0.9$$

$$\text{MAX EFFICIENCY COPPER LOSS} = (1/4)^2 \gamma_3 (75.76)^2 \times 1.57 = 1689$$

$$\text{MAX EFFICIENCY IRON LOSS} = 1689$$

$$\begin{aligned}\text{EFFICIENCY} &= \frac{\text{OUT PUT}}{\text{OUT PUT} + \text{IRON LOSS} + \text{COPPER LOSS}} \times 100 \\ &= \frac{1/4 \times 1500 \times 10^3 \times 0.9}{1/4 \times 1500 \times 10^3 \times 0.9 + 1689 + 1689} \times 100 \\ &= 99\%.\end{aligned}$$

$$\% \text{ REGULATION} = \% \text{ REGLOSS} \pm \% \text{ X SIN} \theta$$

FOR LEADING PF

$$\% \text{ REG} = \% \text{ REGLOSS} - \% \text{ X SIN} \theta$$

$$\text{COS} \theta = 0.8$$

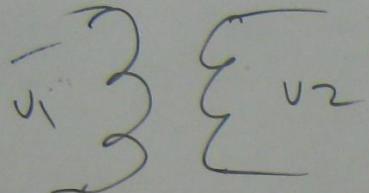
$$\theta = \cos^{-1} 0.8 = 36.8^\circ$$

$$\text{SIN} \theta = \sin 36.8^\circ = 0.6$$

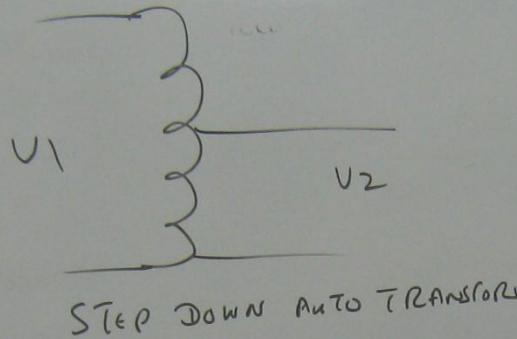
$$\% \text{ REG} = [0.8 \times 0.8 - 5 \times 0.6]$$

=

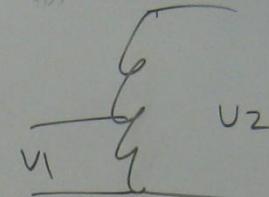
6



2 WINDING  
TRANSFORMER



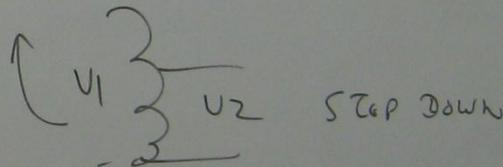
STEP DOWN AUTO TRANSFORMER



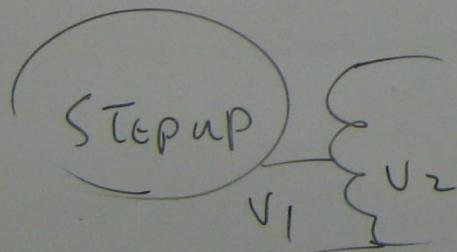
STEP UP AUTO TRANSFORMER

$$\text{Auto Transformer Power} = \left(1 - \frac{1}{k}\right) \times \text{2 WINDING TRANSFORMER U.A}$$

RATING (U.A)



STEP DOWN



$$\text{Auto U.A} = (1 - k) \times \text{2 WINDING TR. U.A}$$

$$k = \frac{V_1}{V_2}$$

= 160 + w

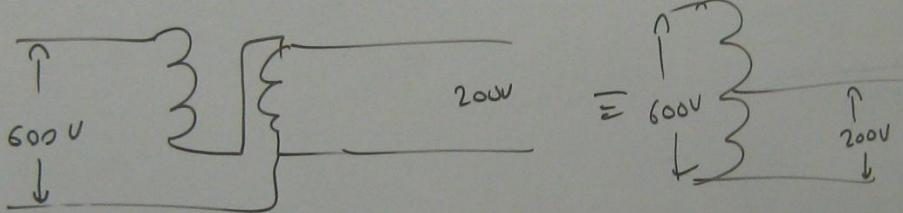
Ph 400 / 200 V 2 WINDING TRANSFORMER

14 RATED 5 KVA. THE TRANSFORMER IS TO SUPPLY 600 / 200 V

DRAW THE CIRCUIT DIAGRAM HOW TO SUPPLY THE LOAD.

ALSO FIND IT'S RATING WHILE SUPPLYING 600 / 200 V.

400 } { 200  
2 WINDINGS



$$\text{Auto T.R U.A} = \left(1 - \frac{1}{k}\right) \times \text{2 WINDING T.R U.A}$$

$$k = \frac{U_1}{U_2} = \frac{600}{200} = 3$$
$$\text{Auto U.A} = \left(1 - \frac{1}{3}\right) \times 5$$
$$\Rightarrow \frac{2}{3} \times 5 = 3.33 \text{ KVA}$$