

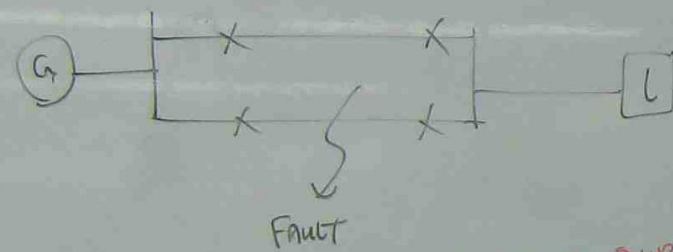
$$-P_0 \delta_2 + P_0 \delta_c$$



$\delta_0 =$  NORMAL LOADING ANGLE (RADIAN)

$$P_1 \cos \delta_0$$

$-\delta_2)$



$P_1 =$  POWER TRANSFERRED DURING FAULT

$\delta_2)$  THEN C.B & RELAY TRIP OFF THE LINE



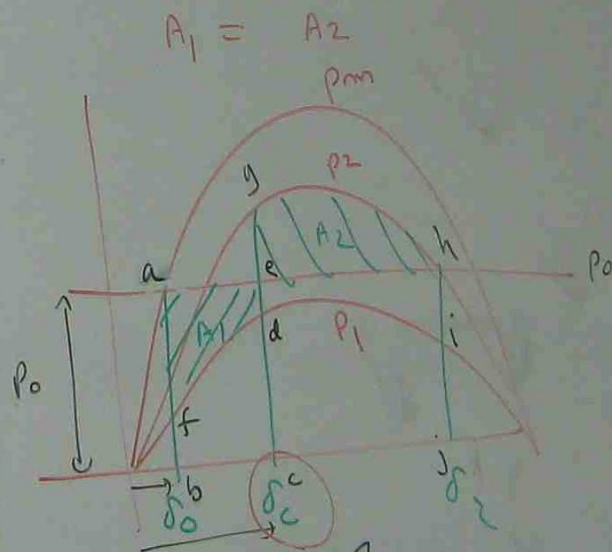
ONLY ONE LINE IS LEFT AFTER THE FAULT.

$P_2 =$  POWER TRANSFERRED AFTER THE FAULT

$A_1$  = ACCELERATED AREA (CHANGE IN ROTOR TOTAL MECHANICAL ENERGY DUE TO FAULT)

$A_2$  = DECELERATED AREA (RECOVERY)

TO MAINTAIN THE SYSTEM STABILITY,  $A_1$  MUST BE EQUAL TO  $A_2$



$$\begin{aligned}
 A_1 &= \square abce - \square bfdc \\
 &= ab \times bc - \int_{\delta_0}^{\delta_c} P_1 \sin \delta d\delta \\
 &= P_0(\delta_c - \delta_0) - \int_{\delta_0}^{\delta_c} P_1 \sin \delta d\delta - I
 \end{aligned}$$

$$A_2 = \square cghj - \square ehjo$$

$$A_2 = \int_{\delta_c}^{\delta_2} P_2 \sin \delta d\delta - \int_{\delta_c}^{\delta_2} P_0 d\delta$$

$$= \int_{\delta_c}^{\delta_2} P_2 \sin \delta d\delta - P_0(\delta_2 - \delta_c) - II$$

$$(I) A_1 = P_0 \delta_c - P_0 \delta_0 - P_1 \left[ -\cos \delta \right]_{\delta_0}^{\delta_c}$$

$$A_1 = P_0 \delta_c - P_0 \delta_0 + P_1 [\cos \delta_c - \cos \delta_0]$$

$$A_1 = P_0 \delta_c - P_0 \delta_0 + P_1 \cos \delta_c - P_1 \cos \delta_0 - I$$

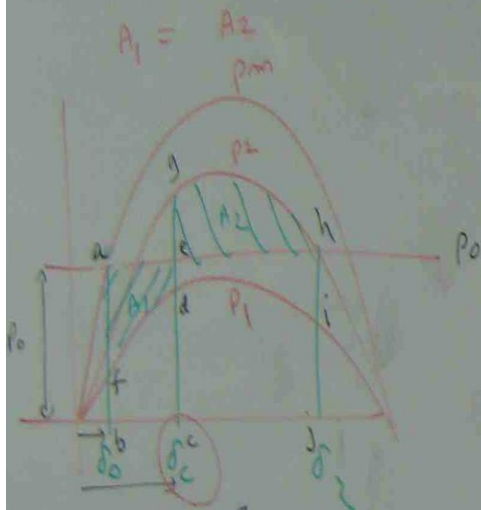
$$A_2 = -P_2 \left[ \cos \delta \right]_{\delta_c}^{\delta_2}$$

$$A_2 = -P_2 [\cos \delta_2 - \cos \delta_c]$$

$$= -P_2 \cos \delta_2 + P_2 \cos \delta_c$$

$$A_2 = P_2 \cos \delta_c - P_2 \cos \delta_2$$

$A_1$  - ACCELERATED AREA (CHANGE IN ROTOR TORQUE / SPEED / ENERGY DUE TO FAULT)  
 $A_2$  - DECELERATED AREA (RECOVERY)  
 TO MAINTAIN THE SYSTEM STABILITY,  $A_1$  MUST BE EQUAL TO  $A_2$



$$\begin{aligned}
 A_1 &= \square abce - \square bfdc \\
 &= ab \times bc - \int_{\delta_0}^{\delta_c} P_1 \sin \delta d\delta \\
 &= P_0(\delta_c - \delta_0) - \int_{\delta_0}^{\delta_c} P_1 \sin \delta d\delta - I
 \end{aligned}$$

$$A_2 = \square cghj - \square ehjo$$

$$\begin{aligned}
 A_2 &= \int_{\delta_c}^{\delta_2} P_2 \sin \delta d\delta - \hat{n} \times eh \\
 &= \int_{\delta_c}^{\delta_2} P_2 \sin \delta d\delta - P_0(\delta_2 - \delta_c) - II
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{I} \quad A_1 &= P_0 \delta_c - P_0 \delta_0 - P_1 \left[ -\cos \delta \right]_{\delta_0}^{\delta_c} \\
 A_1 &= P_0 \delta_c - P_0 \delta_0 + P_1 [\cos \delta_c - \cos \delta_0] \\
 A_1 &= P_0 \delta_c - P_0 \delta_0 + P_1 \cos \delta_c - P_1 \cos \delta_0 - \textcircled{3}
 \end{aligned}$$

$$\begin{aligned}
 A_2 &= -P_2 \left[ \cos \delta \right]_{\delta_c}^{\delta_2} - P_0 \delta_2 + P_0 \delta_c \\
 A_2 &= -P_2 [\cos \delta_2 - \cos \delta_c] - P_0 \delta_2 + P_0 \delta_c
 \end{aligned}$$

$$\begin{aligned}
 &= -P_2 \cos \delta_2 + P_2 \cos \delta_c \\
 &\quad - P_0 \delta_2 + P_0 \delta_c \quad \textcircled{4}
 \end{aligned}$$

$$A_1 = A_2$$

$$\cancel{P_0 \delta_c} - P_0 \delta_0 + \underline{P_1 \cos \delta_c} - P_1 \cos \delta_0 = -P_2 \cos \delta_2 + \underline{P_2 \cos \delta_c} - P_0 \delta_2 + \cancel{P_0 \delta_c}$$

$\delta_0 = \text{normal}$

$$P_1 \cos \delta_c - P_2 \cos \delta_c = -P_2 \cos \delta_2 - P_0 \delta_2 + P_0 \delta_0 + P_1 \cos \delta_0$$

$$\cos \delta_c (P_1 - P_2) = P_1 \cos \delta_0 - P_2 \cos \delta_2 + P_0 (\delta_0 - \delta_2)$$

$$\cos \delta_c = \frac{P_1 \cos \delta_0 - P_2 \cos \delta_2 + P_0 (\delta_0 - \delta_2)}{(P_1 - P_2)}$$

$$\delta_c = \cos^{-1} \frac{P_1 \cos \delta_0 - P_2 \cos \delta_2 + P_0 (\delta_0 - \delta_2)}{(P_1 - P_2)} \quad \text{THEN C.B.}$$

Q. A GENERATOR OPERATING AT 50 HZ DELIVERS  $P_0$  POWER TO INFINITE BUSBAR THROUGH NETWORK IN WHICH RESISTANCE MAY BE NEGLECTED. A FAULT OCCURS WHICH REDUCES THE MAXIMUM POWER TRANSFERABLE TO  $P_1$  WHEREAS BEFORE THE FAULT THIS POWER WAS  $1.8 \text{ pu}$  AND AFTER THE CLEARANCE OF THE FAULT, IT IS  $1.3 \text{ pu}$ . BY USE OF EQUAL AREA CRITERION, DETERMINE THE CRITICAL CLEARING ANGLE.

$$P_2 \quad \delta_c = ?$$

$$\delta_c = \cos^{-1} \frac{P_1 \cos \delta_0 - P_2 \cos \delta_2 + P_0 (\delta_0 - \delta_2)}{P_1 - P_2}$$

$$P_1 = 0.4 \quad P_2 = 1.3, \quad P_0 = 1, \quad P_{\max} = 1.8$$

$$\delta_0 = \sin^{-1} \frac{P_0}{P_{\max}}$$

$$\delta_2 = 180 - \sin^{-1} \left( \frac{P_0}{P_2} \right)$$

$$\delta_0 = \sin^{-1} \frac{1}{1.8} = 33.8^\circ$$

$$\delta_2 = 180 - \sin^{-1} \frac{1}{1.3} = 129.72^\circ$$

FL

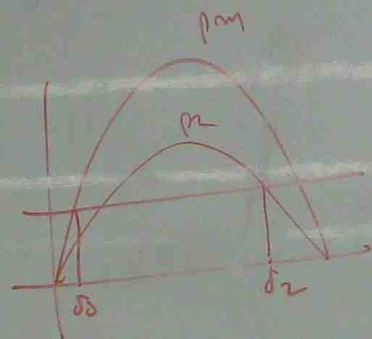
$$180 \rightarrow \pi \text{ Radian}$$

$$33.8 \rightarrow ? = \frac{\pi \times 33.8}{180}$$

$$= \frac{3.1416 \times 33.8}{180}$$

$$= 0.58$$

$$129.72 \rightarrow ? = \frac{\pi \times 129.72}{180} = 2.26$$



$$\delta_c = \cos^{-1} \frac{0.4 \cos 33.8 - 1.3 \cos 129.72 + 1 (2.26 - 0.58)}{0.4 - 1.3}$$

$$= \cos^{-1} 0.515$$

$$= 58.9^\circ$$

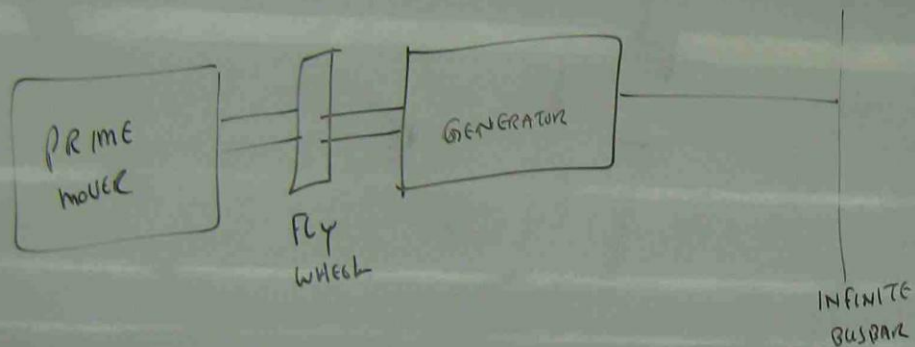
FIND RELAY SETTING TIME, IF THE MACHINE HAS 4 POLES.

$$N = \frac{120f}{p} = \frac{120 \times 50}{4} = 1500 \text{ rpm.}$$

$$1500 \times 360 = 60 \text{ sec}$$

$$58.9^\circ \rightarrow ? = \frac{60 \times 58.9}{1500 \times 360} = 0.006 \text{ sec}$$

$$1500 \times 360 = 60 \text{ ms}$$



$$M_c \frac{d^2 \delta}{dt^2} = P_0 - P_m \sin \delta$$

Moment of Inertia  $\rightarrow M_c$   
 Angular Acceleration  $\rightarrow \frac{d^2 \delta}{dt^2}$   
 Electrical Energy Out Put by Generator  $\rightarrow P_m \sin \delta$

MECHANICAL ENERGY BY PRIME MOVER  $\rightarrow P_0$

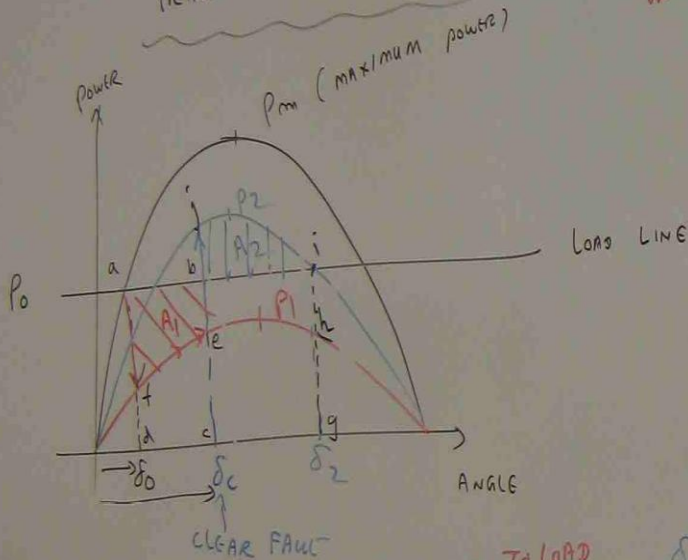
$$M_c \frac{d^2 \delta}{dt^2} + K_d \frac{d\delta}{dt} = (P_0 - \Delta P_0) -$$

Prime mover Power  $\rightarrow M_c \frac{d^2 \delta}{dt^2}$   
 Damping Function to Limit Oscillation  $\rightarrow K_d \frac{d\delta}{dt}$   
 Change of Output Power  $\rightarrow \Delta P_0$

MECH PROS  
ELEC PRO

T<sub>1</sub> - NEXT WEEK  
REVISION AFTER THE BREAK

# TRANSIENT STABILITY FAULT CLEARANCE



P<sub>m</sub> = MAXIMUM POWER

P<sub>0</sub> = NORMAL OUTPUT POWER

δ<sub>0</sub> = NORMAL LOAD ANGLE

P<sub>1</sub> = POWER TO LOAD DURING FAULT

P<sub>2</sub> = POWER TO LOAD AFTER FAULT.

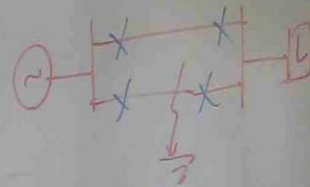
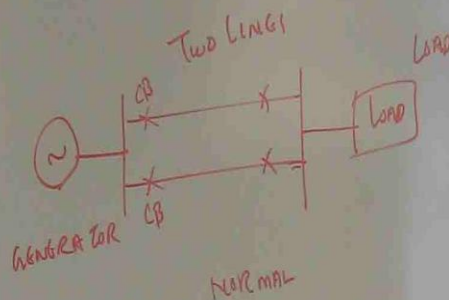
δ<sub>2</sub> = FINAL ANGLE

TO MAINTAIN STABILITY  $A_1 = A_2$

1800 rpm

1800 rpm → 60 sec

δ<sub>c</sub> — ?



RELAY

CB OPERATES TO CLEAR THE FAULT AT δ<sub>c</sub>

AFTER FAULT



A<sub>1</sub> = ACCELERATED AREA (DUE TO FAULT)

A<sub>2</sub> = CONTROLLED AREA (RELAY OPERATION)

$$\begin{aligned}
 A_1 &= abcd - dcef \int_{\delta_0}^{\delta_c} \delta_c \\
 &= ad \times dc - \int_{\delta_0}^{\delta_c} P_1 \sin \delta d\delta \\
 &= P_0(\delta_c - \delta_0) - \left[ -P_1 \cos \delta \right]_{\delta_0}^{\delta_c} \\
 &= P_0(\delta_c - \delta_0) + P_1 (\cos \delta_0 - \cos \delta_c) \\
 &= P_0 \delta_c - P_0 \delta_0 + P_1 [\cos \delta_c - \cos \delta_0] \\
 A_1 &= P_0 \delta_c - P_0 \delta_0 + P_1 \cos \delta_c - P_1 \cos \delta_0 \quad \text{--- (1)}
 \end{aligned}$$

$$\begin{aligned}
 A_2 &= jcgj - bcgi \\
 &= \int_{\delta_c}^{\delta_2} P_2 \sin \delta d\delta - P_0(\delta_2 - \delta_c) \\
 &= -P_2 [\cos \delta]_{\delta_c}^{\delta_2} - P_0 \delta_2 + P_0 \delta_c \\
 &= -P_2 [\cos \delta_2 - \cos \delta_c] - P_0 \delta_2 + P_0 \delta_c \quad \text{--- (2)}
 \end{aligned}$$

$$A_2 = -P_2 [\cos \delta_2 - \cos \delta_c] - P_0 \delta_2 + P_0 \delta_c \quad \text{--- (2)}$$

$$\begin{aligned}
 A_1 &= A_2 \\
 P_0 \delta_c - P_0 \delta_0 + P_1 \cos \delta_c - P_1 \cos \delta_0 &= -P_2 [\cos \delta_2 - \cos \delta_c] - P_0 \delta_2 + P_0 \delta_c \\
 -P_0 \delta_0 + P_1 \cos \delta_c - P_1 \cos \delta_0 &= -P_2 \cos \delta_2 + P_2 \cos \delta_c - P_0 \delta_2
 \end{aligned}$$

$$\begin{aligned}
 P_1 \cos \delta_c - P_2 \cos \delta_c &= -P_2 \cos \delta_2 - P_0 \delta_2 + P_0 \delta_0 + P_1 \cos \delta_0 \\
 \cos \delta_c [P_1 - P_2] &= P_1 \cos \delta_0 - P_2 \cos \delta_2 + P_0 (\delta_0 - \delta_2)
 \end{aligned}$$

$$\cos \delta_c = \frac{P_1 \cos \delta_0 - P_2 \cos \delta_2 + P_0 (\delta_0 - \delta_2)}{P_1 - P_2}$$

$$\begin{aligned}
 \delta_c &= \text{FAULT CLEARING ANGLE TO MAINTAIN STABILITY} \\
 &= \cos^{-1} \left[ \frac{P_1 \cos \delta_0 - P_2 \cos \delta_2 + P_0 (\delta_0 - \delta_2)}{P_1 - P_2} \right]
 \end{aligned}$$

$$\delta_c = \cos^{-1} \left[ \frac{P_1 \cos \delta_0 - P_2 \cos \delta_2 + P_0 (\delta_0 - \delta_2)}{P_1 - P_2} \right]$$

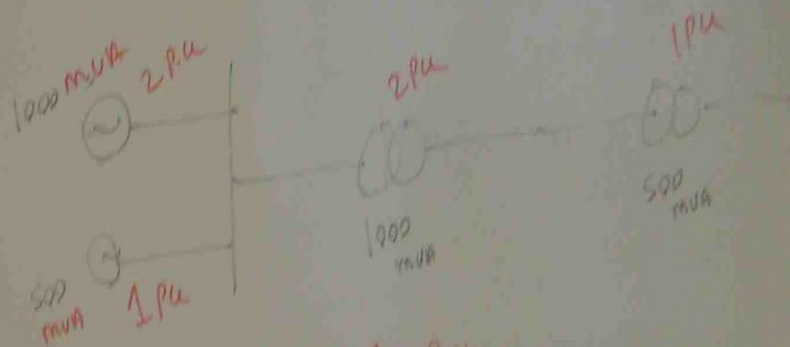
$$\delta_0 = \sin^{-1} \frac{P_0}{P_{max}}$$

POWER BEFORE FAULT,  $P_1$  = POWER DURING FAULT,  $P_2$  = POWER AFTER FAULT

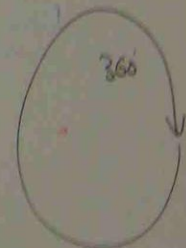
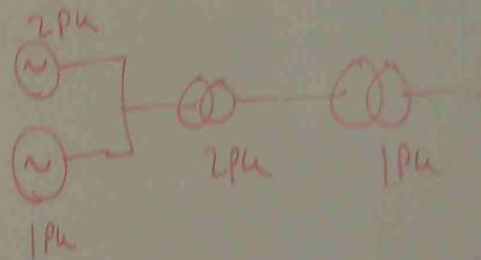
Q. A GENERATOR OPERATING AT 50 HZ DELIVERS 1 P.U. POWER TO INFINITE BUSBAR THROUGH NETWORK WHICH RESISTANCE MAY BE NEGLECTED. A FAULT OCCURS WHICH REDUCES THE MAXIMUM POWER TRANSFERABLE TO 0.4 P.U. WHEREAS BEFORE THE FAULT THIS POWER WAS 1.8 P.U. AND AFTER THE CLEARANCE OF THE FAULT, IT IS 1.3 P.U. BY USE OF EQUAL AREA CRITERION CALCULATE CRITICAL FAULT CLEARING ANGLE

$$\delta_c = \cos^{-1} \frac{P_0 (\delta_0 - \delta_c) + P_1 \cos \delta_0 - P_2 \cos \delta_2}{P_1 - P_2}$$

IF THE GENERATOR IS RUNNING AT 1500 RPM, CALCULATE RELAY SETTING TIME



LET 500 MVA = 1 P.U.



$$\delta_0 = \sin^{-1} \frac{P_0}{P_{max}} = \sin^{-1} \frac{1}{1.8} = 33.8^\circ$$

$$\delta_2 = 180 - \sin^{-1} \frac{P_0}{P_2} = 180 - \sin^{-1} \frac{1}{1.3} = 129.72^\circ$$

$$\delta_c = \cos^{-1} \left( \frac{1}{0.4 - 1.3} \right) + 0.4 \cos 33.8 - 1.3 \cos 129.72$$

$$180^\circ = \pi \text{ radian} = 3.1416$$

$$33.8^\circ = \frac{3.1416 \times 33.8}{180} = 0.58$$

$$129.72^\circ = \frac{3.1416 \times 129.72}{180} = 2.26$$

$$\delta_c = \cos^{-1} \frac{-1(0.58 - 2.26) + 0.4 \cos 33.8 - 1.3 \cos 129.72}{-0.9}$$

$$\delta_c = 58.9$$

$$1500 \text{ rpm} \quad (1 \text{ rpm} = 360^\circ)$$

$$1500 \times 360 \rightarrow 1 \text{ min} \rightarrow 60 \text{ sec}$$

$$58.9^\circ \rightarrow \frac{60 \times 58.9}{1500 \times 360} = 0.005 \text{ sec}$$

$$= 5 \text{ ms}$$

RELAY SETTING TIME

$$A_1 = A_2$$

$$P_0 \delta_c - P_0 \delta_0 + P_1 \cos \delta_c - P_1 \cos \delta_0 = -P_2 [\cos \delta_2 - \cos \delta_c] - P_0 \delta_2 + P_0 \delta_c$$

$$-P_0 \delta_0 + P_1 \cos \delta_c - P_1 \cos \delta_0 = -P_2 \cos \delta_2 + P_2 \cos \delta_c - P_0 \delta_2$$

$$P_1 \cos \delta_c - P_2 \cos \delta_c = -P_2 \cos \delta_2 - P_0 \delta_2 + P_0 \delta_0 + P_1 \cos \delta_0$$

$$\cos \delta_c [P_1 - P_2] = P_1 \cos \delta_0 - P_2 \cos \delta_2 + P_0 (\delta_0 - \delta_2)$$

$$\delta_2 = 180^\circ - \delta_0$$

$$\cos \delta_c = \frac{P_1 \cos \delta_0 - P_2 \cos \delta_2 + P_0 (\delta_0 - \delta_2)}{P_1 - P_2}$$

Power

$P_0$  = Before Fault

$P_1$  = During Fault

$P_2$  = After Fault

$$\delta_c = \text{FAULT CLEARING ANGLE TO MAINTAIN STABILITY}$$

$$= \cos^{-1} \left[ \frac{P_1 \cos \delta_0 - P_2 \cos \delta_2 + P_0 (\delta_0 - \delta_2)}{P_1 - P_2} \right]$$

