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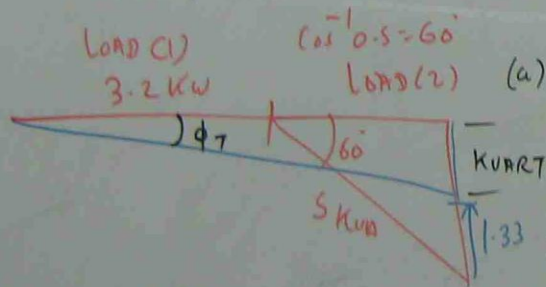
A 250 Vrms 50Hz source is supplying the following loads

Load 1 - 3.2 kW

Load 2 - 5 kVA 0.5 PF LAGGING

Load 3 - 1.33 kVAR LEADING (PURE CAPACITANCE)

CALCULATE (a) TOTAL LOAD (b) TOTAL POWER FACTOR (c) THE VALUE OF ADDITIONAL CONNECTED COMPONENT WHICH WILL IMPROVE POWER FACTOR TO 95%.



$$(a) \text{ kW}_T = 3.2 + 5 \cos 60^\circ$$

$$= 3.2 + 5 \times 0.5 = 3.2 + 2.5$$

$$= 5.7 \text{ kW}$$

$$(b) \text{ kVAR}_T = 5 \sin 60^\circ - 1.33$$

$$= 5 \times 0.866 - 1.33$$

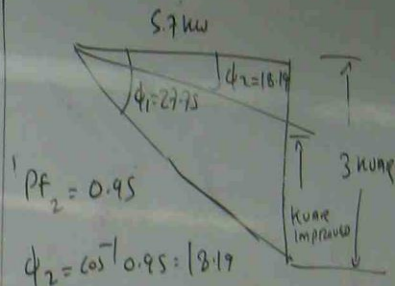
$$= 4.33 - 1.33 = 3 \text{ kVAR}$$

$$\tan \phi_T = \frac{\text{kVAR}_T}{\text{kW}_T} = \frac{3}{5.7} = 0.5263$$

$$\phi_T = \tan^{-1} 0.5263 = 27.75^\circ$$

$$\text{PF}_{\text{TOTAL}} = \cos 27.75^\circ = 0.884 \text{ LAGGING}$$

$$\phi_1 = 27.75^\circ$$



$$\text{kVAR}_{\text{improved}} = \text{kW} (\tan \phi_1 - \tan \phi_2)$$

$$= 5.7 (\tan 27.75^\circ - \tan 18.19^\circ)$$

$$= 5.7 (0.526 - 0.328)$$

$$= 1.128 \text{ kVAR}$$

$$\frac{E_{ph}}{X_c} = \text{kVAR}$$

$$\frac{G_{ph}^2}{2\pi f c} = \text{kVAR}$$

$$2\pi f c \times E_{ph}^2 = \text{kVAR}$$

$$c = \frac{\text{kVAR}}{2\pi f \times E_{ph}^2}$$

$$= \frac{1.128 \times 10^3}{2\pi \times 50 \times 250^2}$$

$$= 5.74 \times 10^{-5} \text{ F}$$

$$= 57.4 \text{ pF}$$

NEED TO CONNECT IN PARALLEL

- ① A STAR CONNECTED LOAD HAS THREE IMPEDANCES  
 $Z_A = 5\Omega$ ,  $Z_B = 27.5\text{ mH}$ ,  $Z_C = 5\Omega$  RESISTOR IN SERIES  
 WITH  $367\text{ }\mu\text{F}$  CAPACITOR. THREE PHASE 3 WIRES LINE  
 VOLTAGE =  $300\text{ V}$ . PHASE SEQUENCE A, B, C. USING  $E_{an}$   
 AS REFERENCE, CALCULATE (i) ALL LINE CURRENTS  
 (ii) VOLTAGE OF STAR POINT OF  
 LOAD WITH RESPECT TO NEUTRAL  
 POINT OF SUPPLY

- ② A STAR CONNECTED LOAD HAS  $Z_A = 5\Omega$ ,  $Z_B = 27.5\text{ mH}$   
 $Z_C = 5\Omega$  RESISTOR IN SERIES WITH  $367\text{ }\mu\text{F}$   
 CAPACITOR. PHASE SEQUENCE A, C, B  
 USE  $E_{an}$  AS REFERENCE, CALCULATE  
 (i) ALL LINE CURRENTS  
 (ii) VOLTAGE OF STAR POINT WITH  
 RESPECT TO NEUTRAL POINT OF SUPPLY.

①  $Z_A = 5\Omega$

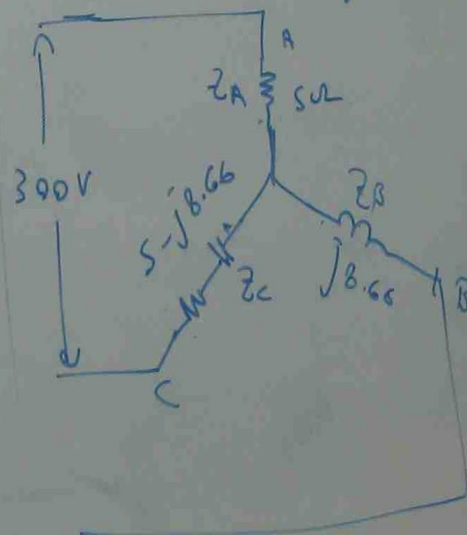
$$Z_B = 2\pi fL = 2 \times 3.1416 \times 50 \times 27.5 \times 10^{-3} = 8.66\Omega$$

$$Z_C = R - jX_C = 5 - j \frac{1}{2\pi fC}$$

$$= 5 - j \frac{1}{2 \times 3.1416 \times 50 \times 367 \times 10^{-6}}$$

$$= 5 - j \frac{10^6}{2 \times 3.1416 \times 50 \times 367}$$

$$= 5 - j8.66\Omega = 10 \angle -60^\circ$$





$$27.5 \times 10^{-3} = 8.66 \angle 0^\circ$$

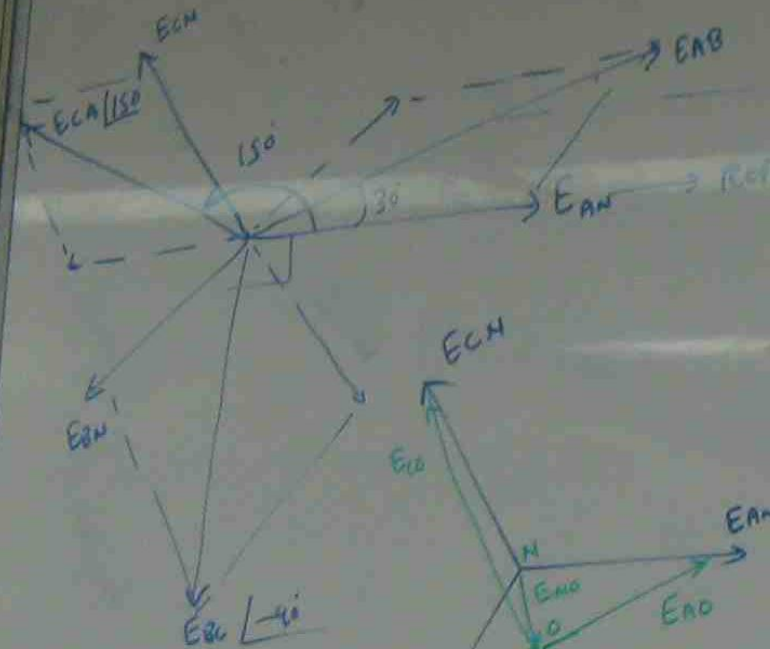
$$= 8.66 \angle 0^\circ$$

$$= 8.66 \angle 90^\circ$$

$$\times 367 \times 10^6$$

$$367$$

$$10 \angle -60^\circ$$



LINE VOLTAGE

$$E_{AB} = 300 \angle 30^\circ \text{ V}$$

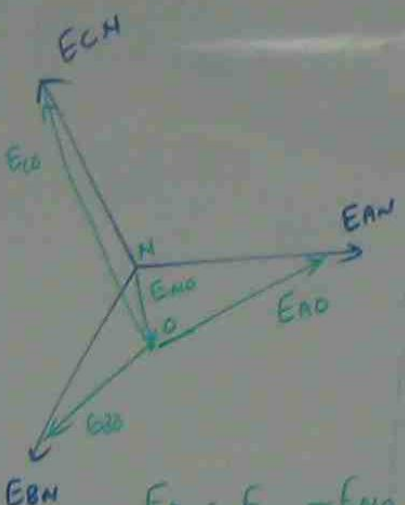
$$E_{BC} = 300 \angle -90^\circ \text{ V}$$

$$E_{CA} = 300 \angle +150^\circ \text{ V}$$

$$E_{AN} = \frac{300}{\sqrt{3}} \angle 0^\circ = 173.2 \angle 0^\circ$$

$$E_{BN} = 173.2 \angle -120^\circ$$

$$E_{CN} = 173.2 \angle +120^\circ$$



$$E_{NO} = E_{AN} - E_{AO}$$

$$E_{BO} = E_{BN} - E_{BO}$$

$$E_{CO} = E_{CN} - E_{CO}$$

$$E_{NO} = ?$$

$$E_{NO} = \frac{E_{AN} \times Y_A + E_{BN} \times Y_B + E_{CN} \times Y_C}{Y_A + Y_B + Y_C} = \frac{173.2 \angle 0^\circ \times \frac{1}{Z_A} + 173.2 \angle -120^\circ \times \frac{1}{Z_B} + 173.2 \angle 120^\circ \times \frac{1}{Z_C}}{\frac{1}{Z_A} + \frac{1}{Z_B} + \frac{1}{Z_C}}$$

$$= \frac{173.2 \angle 0^\circ \times \frac{1}{5} + 173.2 \angle -120^\circ \times \frac{1}{8.66 \angle 90^\circ} + 173.2 \angle 120^\circ \times \frac{1}{10 \angle -60^\circ}}{\frac{1}{5} + \frac{1}{8.66 \angle 90^\circ} + \frac{1}{10 \angle -60^\circ}}$$

$$= \frac{34.6 \angle 0^\circ + 19.9 \angle -210^\circ + 17.3 \angle 180^\circ}{0.2 + 0.115 \angle -90^\circ + 0.1 \angle 60^\circ}$$

$$= \frac{34.6 + 19.9(\cos 210^\circ - j \sin 210^\circ) + 17.3(\cos 180^\circ + j \sin 180^\circ)}{0.2 + 0.115(\cos 90^\circ - j \sin 90^\circ) + 0.1(\cos 60^\circ + j \sin 60^\circ)}$$

$$= \frac{34.6 + 19.9(-0.866 + j0.5) + 17.3(-1 + j0)}{0.2 + 0 - j0.115 + 0.05 + j0.0866}$$

$$= \frac{34.6 - 17.14 + j9.95 - 17.3}{0.25 - j0.028}$$

$$\sqrt{0.25^2 + 0.028^2} \angle -\tan^{-1} \frac{0.028}{0.25}$$

$$= \frac{0.16 + j9.95}{0.25 \angle -6.4^\circ} = \frac{9.98 \angle 89^\circ}{0.25 \angle -6.4^\circ}$$

$$E_{NO} = 39.8 \angle 45.4^\circ V$$

$$E_{AO} = E_{AN} - E_{NO}$$

$$= 173.2 \angle 0^\circ - 39.8 \angle 45.4^\circ$$

$$= 173.2 - 39.8(-0.094 + j0.945)$$

$$= 173.21 + 3.74 - j39.6$$

$$= 176.95 - j39.6$$

$$= 181.32 \angle -12.57^\circ V$$

$$\leftrightarrow 0.25 - j0.028$$

$$I_A = E_{AO} \times Y_A$$

$$= \frac{181.32 \angle -12.57^\circ}{5 \angle 0^\circ}$$

$$= 36.26 \angle -12.57^\circ A$$



$$E_{B0} = E_{BN} - E_{N0} = 173.2 \angle -120 - (-3.74 + j39.6)$$

$$= 173.2 (\cos 120 - j \sin 120) + 3.74 - j39.6$$

$$= 173.2 (-0.5 - j0.866) + 3.74 - j39.6$$

$$= -86.6 - j150 + 3.74 - j39.6 = -82.86 - j189.6$$

$$= \sqrt{82.86^2 + 189.6^2} \angle -180 - \tan^{-1} \frac{189.6}{82.86}$$

$$= 206.9 \angle - (180 - 66.39) = 206.9 \angle -113.61 \text{ V}$$

$$I_B = E_{B0} \times Y_B = 206.9 \angle -113.61 \times 0.115 \angle -90$$

$$= 23.79 \angle -203 \text{ A}$$

$$E_{C0} = E_{CN} - E_{N0} = 173.2 \angle 120 - (-3.74 + j39.6)$$

$$= 173.2 (-0.5 + j0.866) - (-3.74 + j39.6)$$

$$= -86.6 + j150 + 3.74 - j39.6$$

$$= -82.86 + j110.4 = \sqrt{82.86^2 + 110.4^2} \angle (180 - \tan^{-1} \frac{110.4}{82.86})$$

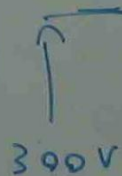
$$= 138 \angle - (180 - 53.1) = 138 \angle -126.9 \text{ V}$$

$$I_C = E_{C0} \times Y_C = 138 \angle -126.9 \times 0.1 \angle 60 = 13.8 \angle -66.9 \text{ Amp}$$

$$\textcircled{1} Z_A = 5 \Omega$$

$$Z_B = 2 \Omega$$

$$Z_C = R$$



S

$$\textcircled{2} \quad Z_A = 5 \Omega$$

$$Z_b = 2\pi fL = 2 \times 3.1416 \times 50 \times 27.5 \times 10^{-3} = 8.66 \Omega$$

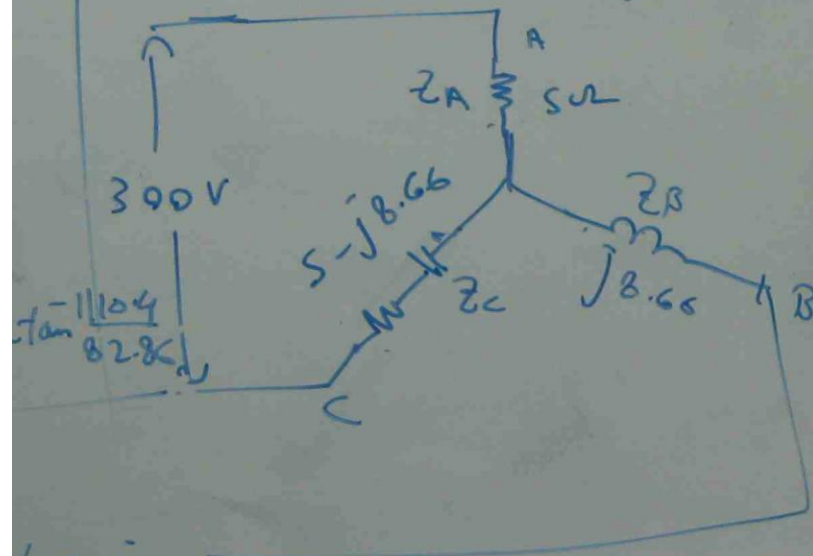
$$= j 8.66 \Omega$$

$$Z_c = R - jX_c = 5 - j \frac{1}{2\pi fC}$$

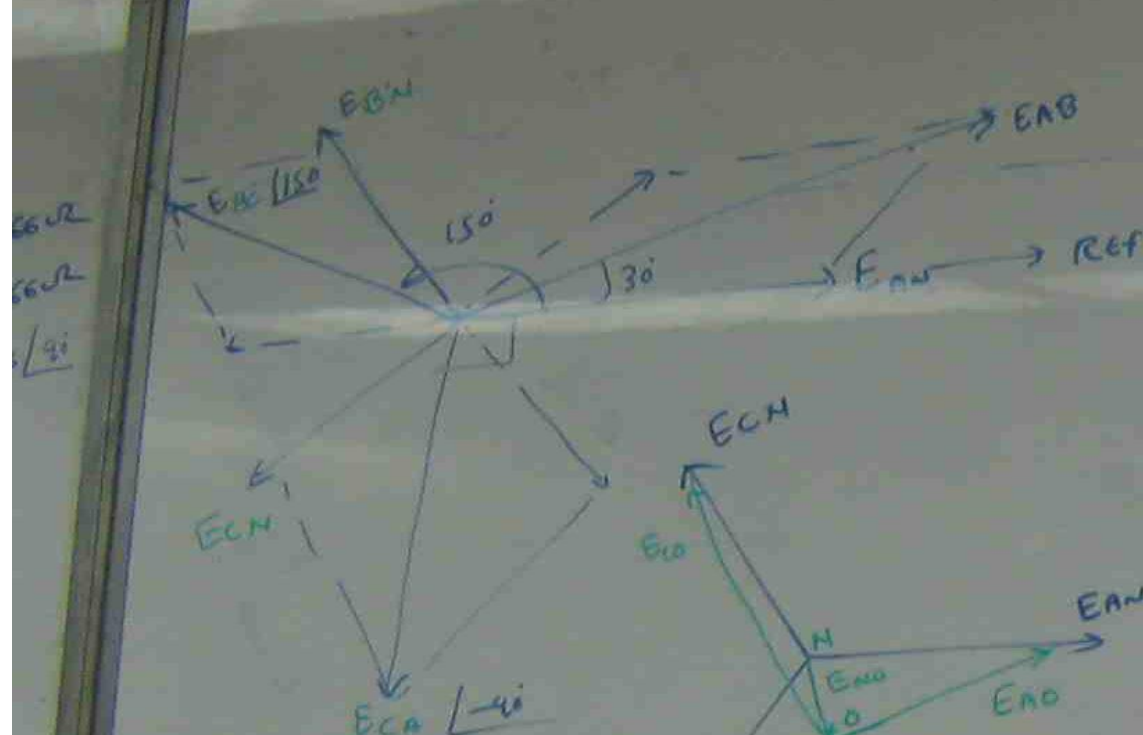
$$= 5 - j \frac{1}{2 \times 3.1416 \times 50 \times 367 \times 10^{-6}}$$

$$= 5 - j \frac{10^6}{2 \times 3.1416 \times 50 \times 367}$$

$$= 5 - j 8.66 \Omega = 10 \angle -60^\circ$$



$$-66.9 \text{ Amp}$$



LINE VOLTAGE

$$E_{AB} = 300 \angle 30^\circ \text{ V}$$

$$E_{CA} = 300 \angle -90^\circ \text{ V}$$

$$E_{BC} = 300 \angle +150^\circ \text{ V}$$

$$E_{AN} = \frac{300}{\sqrt{3}} \angle 0^\circ = 173.2 \angle 0^\circ$$

$$E_{BN} = 173.2 \angle -120^\circ$$

$$E_{CN} = 173.2 \angle +120^\circ$$

$$E_{NO} = E_{AN} - E_{AO}$$

$$E_{BO} = E_{BN} - E_{AO}$$

$$E_{CO} = E_{CN} - E_{AO}$$

$$E_{NO} = ?$$



$$E_{NO} = \frac{V_{AN} Y_A + V_{BN} Y_B + V_{CN} Y_C}{Y_A + Y_B + Y_C}$$

$$= \frac{173.2 \angle 0^\circ \times 0.2 \angle 0^\circ + 173.2 \angle 120^\circ \times 0.115 \angle -90^\circ + 173.2 \angle -120^\circ \times 0.1 \angle 60^\circ}{0.2 \angle 0^\circ + 0.115 \angle -90^\circ + 0.1 \angle 60^\circ}$$

$$= \frac{34.6 \angle 0^\circ + 19.9 \angle 30^\circ + 17.3 \angle -60^\circ}{0.25 - j0.028}$$

$$= \frac{60.66 \angle -4.7^\circ}{0.25 \angle -6.4^\circ} = 242.6 \angle 1.7^\circ = 242.5 + j7.2 \quad \checkmark$$

$$E_{AO} = E_{AN} - E_{NO} = 173.2 \angle 0^\circ - (242.5 + j7.2) = 173.2 - 242.5 - j7.2 = -69.3 - j7.2 = 69.9 \angle -174^\circ \quad \checkmark$$

$$E_{BO} = E_{BN} - E_{NO} = 173.2 \angle 120^\circ - (242.5 + j7.2) = (-86.5 + j149.8) - (242.5 + j7.2) = -329 + j142.6 = 358.6 \angle 156.6^\circ \quad \checkmark$$

$$E_{CO} = E_{CN} - E_{NO} = 173.2 \angle -120^\circ - (242.5 + j7.2) = (-86.5 - j149.8) - (242.5 + j7.2) = -329 - j157 = 364.5 \angle -154.5^\circ \quad \checkmark$$

$$I_A = E_{AO} Y_A = 69.9 \angle -174^\circ \times 0.2 = 14 \angle -174^\circ \text{ Amp}$$

$$I_B = E_{BO} Y_B = 358.6 \angle 156.6^\circ \times 0.115 \angle -90^\circ = 41.2 \angle 67^\circ \text{ Amp}$$

$$I_C = E_{CO} Y_C = 364.5 \angle -154.5^\circ \times 0.1 \angle 60^\circ = 36.5 \angle -94^\circ \text{ Amp}$$

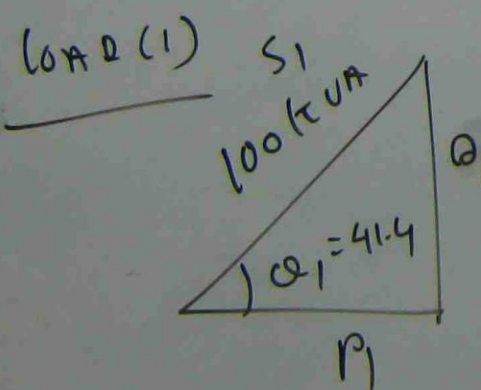


A 415V RMS 50Hz source supplies the following parallel loads

- LOAD 1 - 100 kVA 0.75 PF LAGGING
- LOAD 2 - 50 kW 0.8 PF LAGGING
- LOAD 3 - 20 kVAR 90 DEG LEAD
- LOAD 4 - 60 kW, 90 kVAR LEADING.

DETERMINE (a) TOTAL REAL POWER (b) REACTIVE POWER  
(c) APPARENT POWER (d) POWER FACTOR.

ALSO DETERMINE THE CAPACITANCE REQUIRED PER PHASE TO RAISE POWER FACTOR TO 0.95

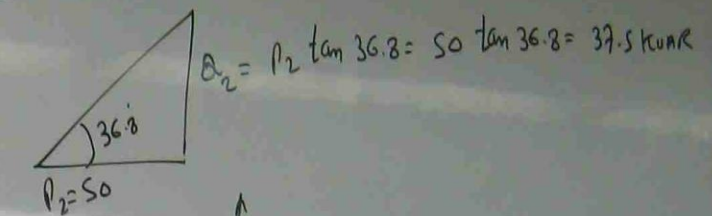


$$\theta_1 = \cos^{-1} 0.75 = 41.4^\circ$$

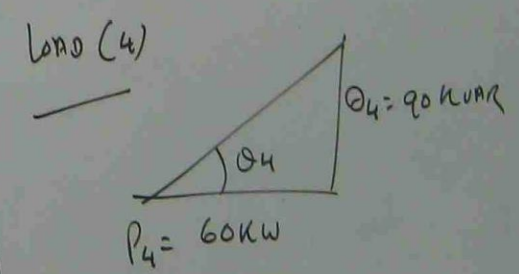
$$P_1 = 100 \cos 41.4 = 75 \text{ kW}$$

$$Q_1 = 100 \sin 41.4 = 66.1 \text{ kVAR}$$

LOAD (2)  $\theta_2 = \cos^{-1} 0.8 = 36.8^\circ$



LOAD (3)



$$P_T = P_1 + P_2 + P_3 + P_4 = 75 + 50 + 0 + 60 = 185 \text{ kW}$$

$$Q_T = Q_1 + Q_2 + Q_3 + Q_4 = 66.1 + 37.5 + 20 + 90 = 213.6 \text{ kVAR}$$

$$\tan \theta_T = \frac{K_{\text{VAR}}}{K_{\text{WT}}} = \frac{2134}{185} = 11.54$$

$$\theta_T = \tan^{-1} 11.54 = 49^\circ \quad \text{PF}_T = \cos \theta_T = \cos 49^\circ = 0.656$$

$$\theta_{T_1} = 49^\circ$$

$$\text{PF}_{T_2} = 0.95 \quad \cos \theta_{T_2} = 0.95, \quad \theta_{T_2} = \cos^{-1} 0.95 = 18.2^\circ$$

$$\begin{aligned} K_{\text{VAR}} (\text{required}) &= K_{\text{WT}} (\tan \theta_{T_1} - \tan \theta_{T_2}) \\ &= 185 (\tan 49^\circ - \tan 18.2^\circ) \\ &= 185 (11.54 - 0.328) = 152.81 \end{aligned}$$

$$\frac{K_{\text{VAR}} (\text{required})}{3} = \frac{E_{\text{ph}}^2}{\frac{1}{2\pi f_c}} \quad K_{\text{VAR}}$$



$$\frac{(52.81 \times 10^3)^3}{3} = E_{ph}^2 \times 2\pi f c$$

$$50.93 \times 10^3 = \left(\frac{415}{\sqrt{3}}\right)^2 \times 2 \times 3.1416 \times 50 \times c$$

$$c = \frac{50.93 \times 10^3}{(240) \times 314.16}$$

$$= 2.814 \times 10^{-3}$$

$$f = 2.814 \times 10^{-3} \times 10^6 \text{ PF}$$

$$= 2.814 \times 10^3$$

$$= 2814 \text{ PF}$$



$$Z_a = 50 + j0 \Omega$$

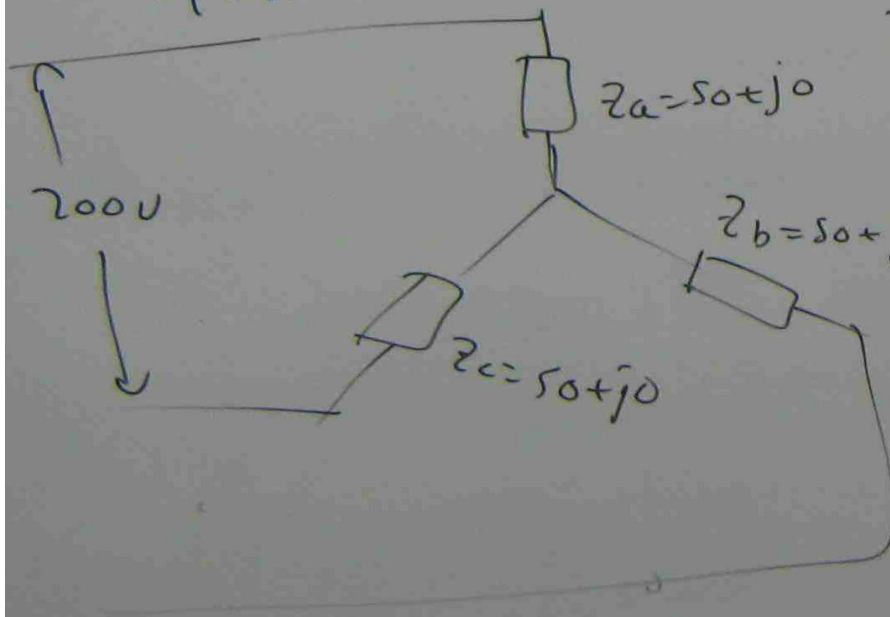
$$Z_b = 50 + j150 \Omega$$

$$Z_c = 50 + j0 \Omega$$

SEQUENCE A, B, C STAR CONNECTION

3 PHASE 3 WIRE . LINE VOLTAGE = 200V

CALCULATE POWER CONSUMED BY LOAD  
BY USING DELTA EQUIVALENT



$$Z_a = 50 \angle 0^\circ$$

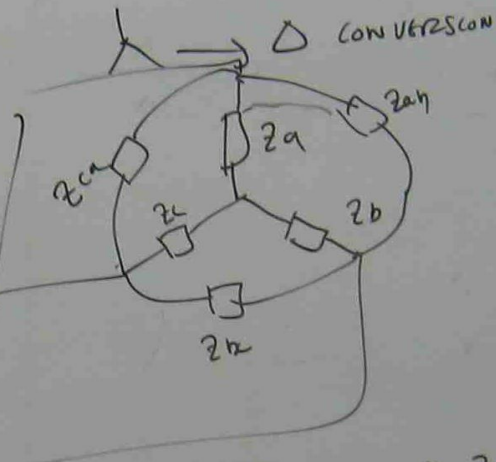
$$Z_b = \sqrt{50^2 + 150^2}$$

$$\angle \tan^{-1} \frac{150}{50}$$

$$= 158.1 \angle 71.56^\circ$$

$$Z_c = 50 \angle 0^\circ$$





$$Z_{ab} = \frac{Z_a Z_b + Z_b Z_c + Z_c Z_a}{Z_c}$$

$$Z_{bc} = \frac{Z_a Z_b + Z_b Z_c + Z_c Z_a}{Z_a}$$

$$Z_{ca} = \frac{Z_a Z_b + Z_b Z_c + Z_c Z_a}{Z_b}$$

$$Z_{ab} = \frac{50 \angle 0^\circ \times 158.1 \angle 71.56^\circ + 158.1 \angle 71.56^\circ \times 50 \angle 0^\circ + 50 \angle 0^\circ \times 50 \angle 0^\circ}{50 \angle 0^\circ}$$

$$= \frac{17905 \angle 71.56^\circ + 17905 \angle 71.56^\circ + 2500}{50 \angle 0^\circ}$$

$$Z_{ab} = \frac{2 \times 17905 (\cos 71.56^\circ + j \sin 71.56^\circ) + 2500}{50 \angle 0^\circ}$$

$$= \frac{15810 (0.316 + j 0.948) + 2500}{50 \angle 0^\circ}$$

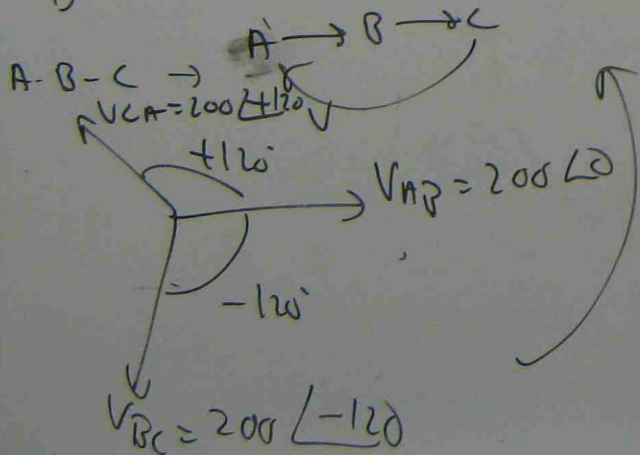
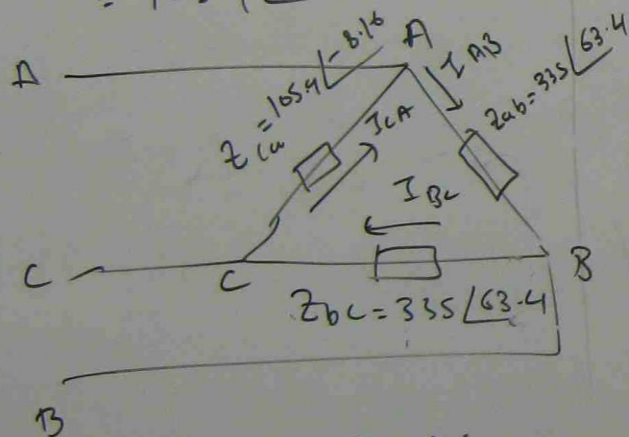
$$= \frac{4995 + j 14987 + 2500}{50 \angle 0^\circ}$$

$$= \frac{7495 + j 14987}{50 \angle 0^\circ}$$

$$Z_{ab} = \frac{16756 \angle 63.4^\circ}{50 \angle 0^\circ} = 335 \angle 63.4^\circ$$

$$Z_{bc} = \frac{16756 \angle 63.4}{50 \angle 0} = 335 \angle 63.4 \Omega$$

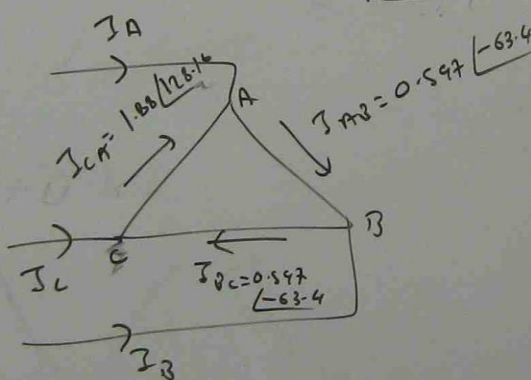
$$Z_{ca} = \frac{16756 \angle 63.4}{158.1 \angle 71.56} = 105.9 \angle -8.16 \Omega$$



$$I_{AB} = \frac{V_{AB}}{Z_{AB}} = \frac{200 \angle 0}{335 \angle 63.4} = 0.597 \angle -63.4 \text{ Amp.}$$

$$I_{BC} = \frac{V_{BC}}{Z_{BC}} = \frac{200 \angle -120}{335 \angle 63.4} = 0.597 \angle -183.4 \text{ Amp}$$

$$I_{CA} = \frac{V_{CA}}{Z_{CA}} = \frac{200 \angle +120}{105.9 \angle -8.16} = 1.88 \angle 128.16 \text{ Amp.}$$



$$P_T = \sum I_{AB}^2 Z_{AB} \cos$$

$$\begin{aligned} & 0.597(0.447 - j0.894) - 1.88(-0.617 + j0.786) \\ & 0.266 - j0.531 + 1.159 - j1.477 \\ & 1.425 - j2 = 2.455 \angle -54.5^\circ \text{ Amp} \\ & I_A = 2.455 \angle -54.5^\circ \text{ Amp} \end{aligned}$$

AT (B)  $I_B + I_{AB} = I_{BC}$   
 $I_B = I_{BC} - I_{AB}$

AT (C)  $I_C + I_{BC} = I_{CA}$   
 $I_C = I_{CA} - I_{BC}$

AT A POINT

Flow IN = Flow out

$$I_A + I_{CA} = I_{AB}$$

$$I_A = I_{AB} - I_{CA}$$

$$= 0.597 \angle -63.4 - 1.88 \angle 128.16$$

$$= 0.597(\cos 63.4 - j \sin 63.4)$$

$$- 1.88(\cos 128.16 + j \sin 128.16)$$



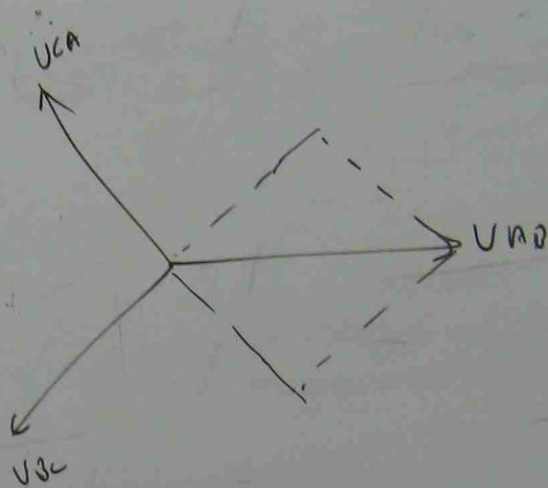
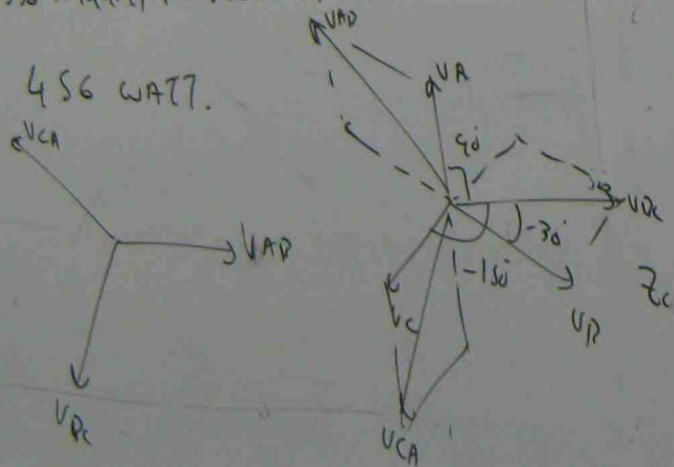
$$P_T = I_{AB}^2 R_{AB} + I_{BC}^2 R_{BC} + I_{CA}^2 R_{CA}$$

$$= (0.597)^2 [200 \cos 0] + (0.597)^2 [200 \cos 0] + (1.88)^2 [200 \cos 0]$$

$$= (0.597)^2 [335 \cos 63.4] + (0.597)^2 [335 \cos 63.4] + (1.88)^2 [105.4 \cos(-8.16)]$$

$$= 0.356 \times 149.99 + 0.356 \times 149.99 + 353 \times 0.9898$$

$$= 456 \text{ WATT.}$$



$$V_{\text{ph}} = \frac{\text{LINE VOLTAGE}}{\sqrt{3}} = \frac{200}{\sqrt{3}} = 115.4 \text{ V}$$

$$V_{BC} = 0 \quad V_A \angle 90^\circ \quad V_B \angle -30^\circ, V_C \angle -150^\circ$$

$$V_{BC} = \angle -120^\circ \rightarrow V_A \angle 90-120 \quad V_B \angle -30-120 \quad V_C \angle -150-120$$

$$V_A \angle -30^\circ \quad V_B \angle -150^\circ \quad V_C \angle -270^\circ$$

$$115.4 \angle -30^\circ \quad 115.4 \angle -150^\circ \quad 115.4 \angle -270^\circ$$

$$(V_A) \quad (V_B) \quad (V_C)$$

ph

A STAR CONNECTED LOAD HAS 3 IMPEDANCES

$$Z_a = 100\Omega \text{ RESISTOR WITH } 400 \text{ mH INDUCTOR}$$

$$Z_b = 120\Omega \text{ RESISTOR WITH } 10 \mu\text{F CAPACITOR}$$

$$Z_c = 250\Omega \text{ RESISTOR.}$$

$$\text{LINE VOLTAGE} = 75 \text{ V, } 60 \text{ Hz}$$

PHASE SEQUENCE ABC.

USE  $E_{AB}$  AS REFERENCE, CALCULATE

(i) ALL CURRENTS IN POLAR FORM

(ii) VOLTAGE OF STAR POINT WITH RESPECT TO NEUTRAL POINT.

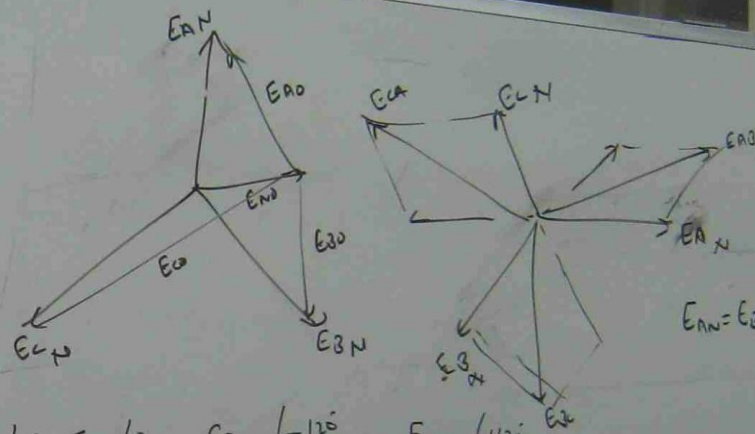
$$Z_a = 100 + j2\pi fL = 100 + j2 \times 3.1416 \times 60 \times 400 \times 10^{-3}$$

$$= 100 + j150 = 180 \angle 56.3^\circ \Omega$$

$$Z_b = 120 - j \frac{1}{2\pi fC} = 120 - j \frac{1}{2 \times 3.1416 \times 60 \times 10 \times 10^{-6}}$$

$$= 120 - j265.25 = 291 \angle -65.6^\circ \Omega$$

$$Z_c = 250 \angle 0^\circ \Omega$$



$$E_{AN} = E_{BN} = E_{CN} = \frac{75}{\sqrt{3}} = 43.3 \text{ V}$$

$$E_{AB} \angle 30^\circ, E_{AN} \angle 0^\circ, E_{BN} \angle -120^\circ, E_{CN} \angle 120^\circ$$

$E_{AB}$  REFERENCE  $\rightarrow E_{AB} \angle 0^\circ$

$$E_{AB} \angle 30-30, E_{AN} \angle 0-30, E_{BN} \angle -120-30, E_{CN} \angle 120-30$$

$$E_{AB} \angle 0, E_{AN} \angle -30, E_{BN} \angle -150, E_{CN} \angle 90$$

$$43.3 \angle -30, 43.3 \angle -150, 43.3 \angle 90$$

$$E_{NO} = \frac{E_{AN} Y_A + E_{BN} Y_B + E_{CN} Y_C}{Y_A + Y_B + Y_C}$$

$$= \frac{\frac{E_{AN}}{Z_A} + \frac{E_{BN}}{Z_B} + \frac{E_{CN}}{Z_C}}{\frac{1}{Z_A} + \frac{1}{Z_B} + \frac{1}{Z_C}}$$

$$Y_A = \frac{1}{Z_A} = \frac{1}{180 \angle 56.3^\circ}$$

$$= 0.0055 \angle -56.3^\circ$$

$$Y_B = \frac{1}{Z_B} = \frac{1}{291 \angle -65.6^\circ}$$

$$= 0.0034 \angle 65.6^\circ$$

$$Y_C = \frac{1}{Z_C} = \frac{1}{250}$$

$$= 0.004$$



$$\begin{aligned}
 E_{No} &= \frac{43.3 \angle -30 \times 0.0055 \angle -56.3 + 43.3 \angle -150 \times 0.0034 \angle 65.6 + 43.3 \angle 40 \times 0.004}{0.0055 \angle -56.3 + 0.0034 \angle 65.6 + 0.004} \\
 &= \frac{0.238 \angle -86.3 + 0.147 \angle -84.4 + 0.1732 \angle 90}{0.0055 (\cos 56.3 - j \sin 56.3) + 0.0034 (\cos 65.6 + j \sin 65.6) + 0.004} \\
 &= \frac{0.238 (\cos 86.3 - j \sin 86.3) + 0.147 (\cos 84.4 - j \sin 84.4) + 0.1732 (\cos 90 + j \sin 90)}{0.132 - j0.0929 + 0.0029 + j0.0031 + 0.004} \\
 &= \frac{0.0153 - j0.237 + 0.0143 - j0.0146 + j0.1732}{0.1389 - j0.089} \\
 &= \frac{0.0296 - j0.0784}{0.1389 - j0.089} \\
 &= \frac{0.0838 \angle -69.3}{0.16496 \angle -32.6} \\
 &= 0.51 \angle -26.3 \checkmark
 \end{aligned}$$

$$\begin{aligned}
 E_{No} &= E_{AN} - E_{No} \\
 &= 43.3 \angle 30 - 0.51 \angle -26.3 \\
 &= 43.3 (\cos 30 - j \sin 30) - 0.51 (\cos 26.3 - j \sin 26.3) \\
 &= 37.5 - j21.65 - 0.457 + j0.225 \\
 &= 37 - j21.425 \\
 &= 42.75 \angle -30
 \end{aligned}$$

$$\begin{aligned}
 I_A &= \frac{E_{AO}}{Z_A} = \frac{42.75 \angle -30}{180 \angle 56.3} \\
 &= 0.226 \angle -86.3 \text{ A}
 \end{aligned}$$

$$\begin{aligned}
 E_{Bo} &= E_{BN} - E_{No} \\
 &= 43.3 \angle -150 - 0.51 \angle -26.3
 \end{aligned}$$

$$I_B = \frac{E_{Bo}}{Z_B}$$

$$\begin{aligned}
 E_{Co} &= E_{CN} - E_{No} \\
 &= 43.3 \angle 40 - 0.51 \angle -26.3
 \end{aligned}$$

$$I_C = \frac{E_{Co}}{Z_C}$$

