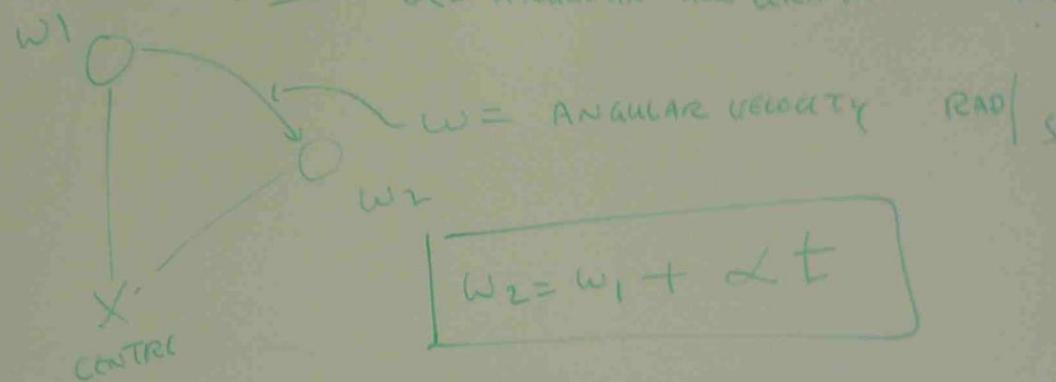


$$T = I \alpha$$

T = TORQUE N-m

I = MOMENT OF INERTIA N-m/s²

t sec α = ANGULAR ACCELERATION RAD/s²



$$w_2 = w_1 + \alpha t$$

Pb A MOTOR HAS A COMBINED MOMENT OF INERTIA OF 10 N-m/s^2 AND INITIAL VELOCITY OF 200 RAD/s . IF THE TORQUE PRODUCED BY THE MOTOR IS INCREASED BY 50 N-m CALCULATE (a) THE TIME FOR THE SPEED TO REACH 300 RAD/s

- (b) THE FINAL SPEED IF THE TORQUE WAS MAINTAINED FOR 10 sec
- (c) THE TORQUE INCREASE NECESSARY TO OBTAIN AN INCREASE OF 50 RAD/sec IN 2.5 SEC.

$$I = 10 \text{ N-m/s}^2 \quad \omega_1 = 200 \text{ rad/s}$$

$$T = 50 \text{ N-m} \quad \omega_2 = 300 \text{ rad/s}$$

$$t = ?$$

$$(a) \quad \omega_2 = \omega_1 + \alpha t \quad | \quad \omega_2 = \omega_1 + \alpha t \\ 300 = 200 + 5t$$

$$T = I \alpha$$

$$S_0 = I \alpha$$

$$\alpha = \frac{50}{10} = 5 \text{ rad/s}^2$$

$$t = \frac{300 - 200}{5} \\ = \frac{100}{5} = 20 \text{ sec}$$

$$(b) t = 10 \text{ sec}$$

$$\omega_2 = ?$$

$$\omega_2 = \omega_1 + \alpha t$$

$$= 200 + 5 \times 10$$

$$= 250 \text{ RAD/s}$$

$$(c) \omega_2 - \omega_1 = 50 \text{ RAD/s}$$

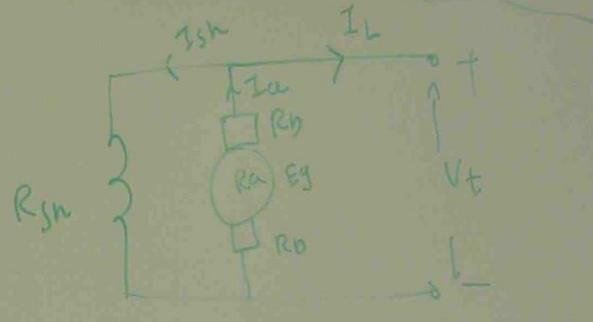
$$t = 2.5 \text{ sec}$$

$$\tau = ?$$

$$\alpha = \frac{\omega_2 - \omega_1}{t} = \frac{50}{2.5} = 20 \text{ RAD/s}^2$$

$$\tau = I \alpha = 10 \times 20 = 200 \text{ N-m}$$

CONFIGURATION OF DC MACHINE WINDINGS



SHUNT GENERATOR

R_{sh} = SHUNT FIELD RESISTANCE

R_a = ARMATURE RESISTANCE

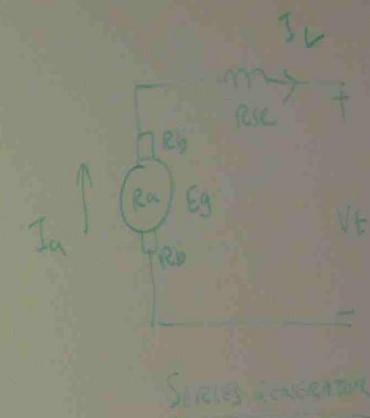
R_b = BRUSH RESISTANCE

E_g = GENERATED VOLTAGE

V_t = TERMINAL VOLTAGE

$$I_a = I_L + I_{sh} \quad E_g = V_t + I_a(R_a + R_b)$$

$$I_{sh} = \frac{V_t}{R_{sh}}$$



$$I_a = I_L$$

$$E_g = V_t + I_L(R_a + R_b)$$

$$I_L = \frac{V_t}{R_a + R_b}$$

$$(b) t = 10 \text{ sec}$$

$$\omega_2 = ?$$

$$\omega_2 = \omega_1 + \alpha t$$

$$= 200 + 5 \times 10$$

$$= 250 \text{ RAD/s}$$

$$(c) \omega_2 - \omega_1 = 50 \text{ RAD/s}$$

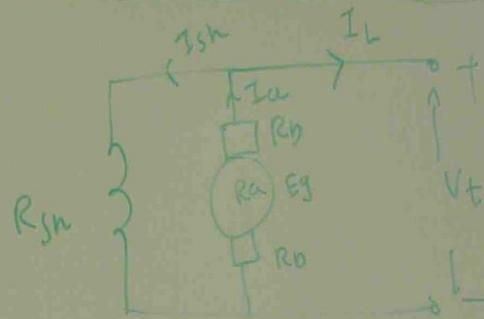
$$t = 2.5 \text{ sec}$$

$$\alpha = ?$$

$$\alpha = \frac{\omega_2 - \omega_1}{t} = \frac{50}{2.5} = 20 \text{ RAD/s}^2$$

$$T = I \alpha = 10 \times 20 = 200 \text{ N-m}$$

CONFIGURATION OF DC MACHINE WINDINGS



SHUNT GENERATOR

R_{sh} = SHUNT FIELD RESISTANCE

R_a = ARMATURE RESISTANCE

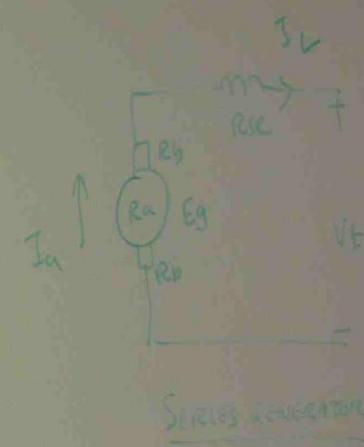
R_b = BRUSH RESISTANCE

E_g = GENERATED VOLTAGE

V_t = TERMINAL VOLTAGE

$$I_a = I_L + I_{sh} \quad E_g = V_t + I_a(R_a + R_b)$$

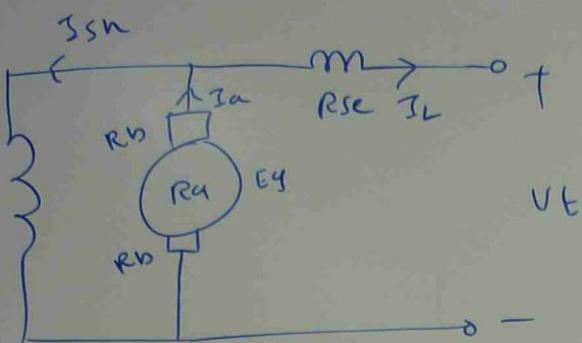
$$I_{sh} = \frac{V_t}{R_{sh}}$$



$$I_a = I_L$$

$$E_g = V_t + I_L(R_a + R_b)$$

$$I_L = \text{load power} / V_t$$

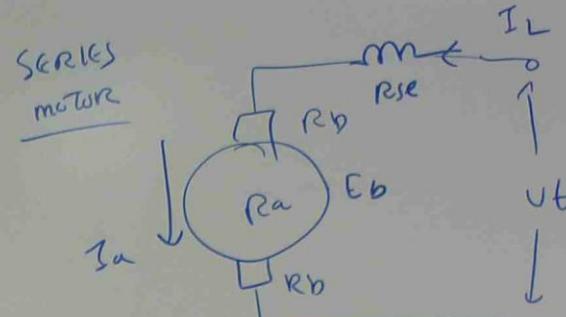


SHORT SHUNT Compound

$$I_a = I_L + I_{sh}$$

$$I_{sh} = \frac{Vt + I_L R_{se}}{R_{sh}}$$

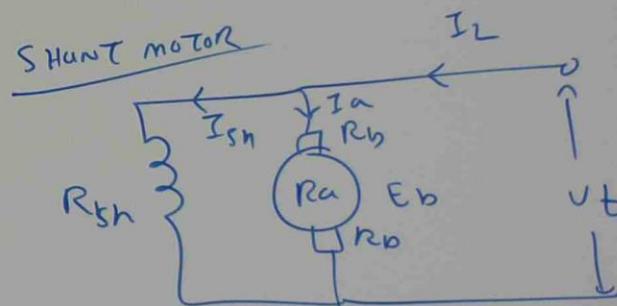
$$E_g = Vt + I_a (R_a + 2R_b)$$



$$E_b = \text{BACK E mF}$$

$$I_v = I_a$$

$$E_b = Vt - I_a (R_a + 2R_b)$$



$$I_{sh} = \frac{Vt}{R_{sh}}, \quad E_b = Vt - I_a (R_a + 2R_b)$$

$$I_a = I_L - I_{sh}$$

GENERATED VOLTAGE + BACK EMF

$$E_g = \frac{\phi Z N}{60} \times \frac{P}{a} \quad (\text{GENERATOR})$$

E_g = GENERATED VOLTAGE

Z = NO. OF CONDUCTORS

N = RPM

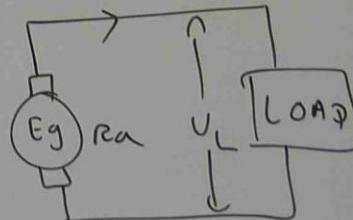
P = NO. OF POLES

a = NO. OF ARMATURE PARALLEL PATHS

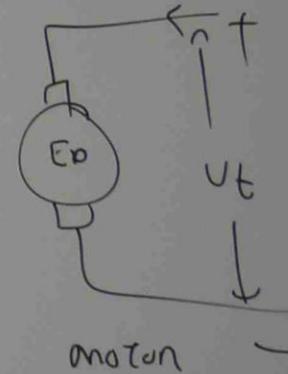
$a = m \times p$ (LAP)

$a = m \times 2$ (WAVE)

$$E_b = \frac{\phi Z N}{60} \times \frac{P}{a} \quad (\text{motor})$$

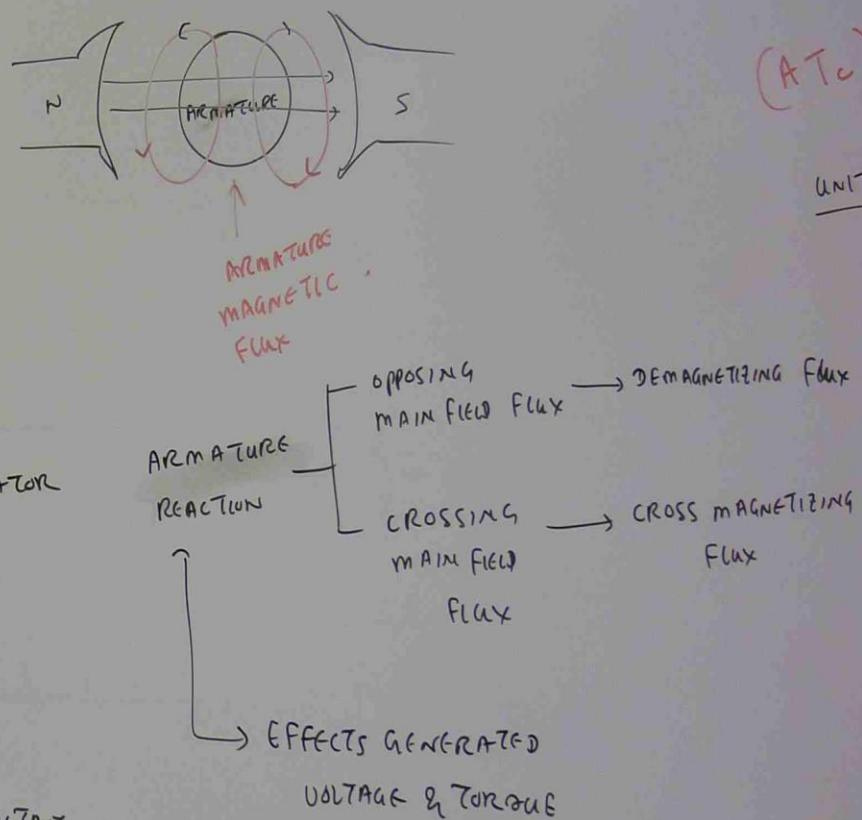
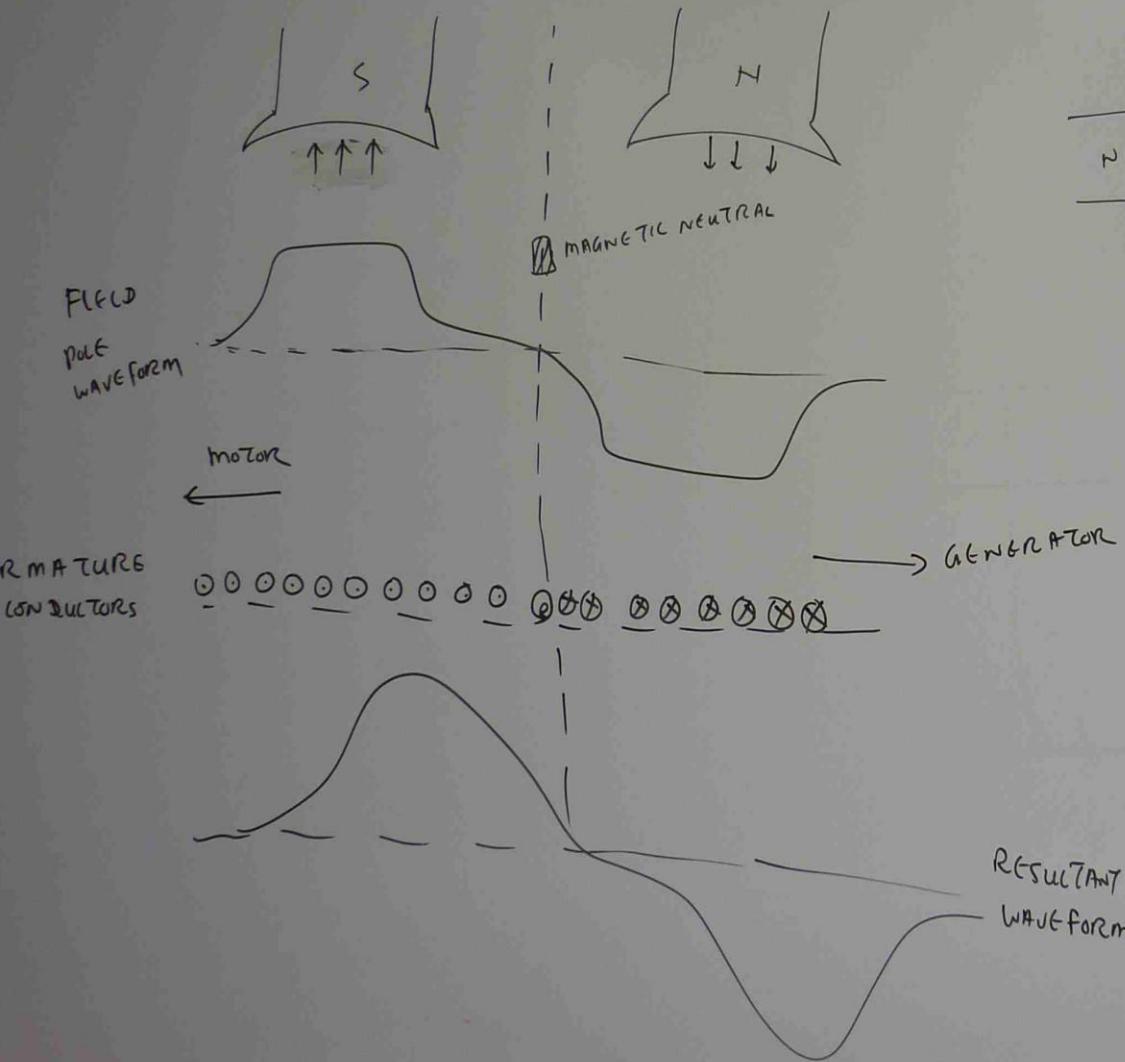


GENERATOR



MOTOR

MAGNETIC ACTION OF ARMATURE FIELD DISTORTION

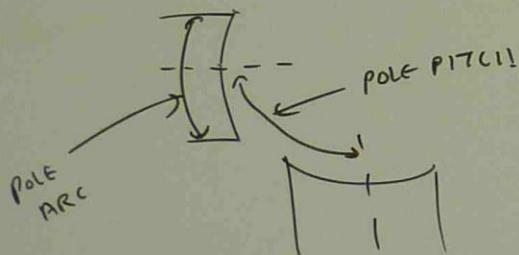


(AT_c)

$$\text{CROSS MAGNETIZING FLUX} = \frac{\alpha z I_a}{2a P}$$

UNIT → (Amp-TURNS/pole)

$$\alpha = \frac{\text{POLE ARC}}{\text{POLE PITCH}}$$



NO. OF
z = ARMATURE CONDUCTORS

a = NO. OF ARMATURE
PARALLEL PATHS

P = NO. OF POLES.

p_b

AN ARMATURE 0.5m DIAMETER OF 6 POLES LAP WOUND GENERATOR HAS 378 CONDUCTORS CARRIES 800 AMP AND HAS A POLE ARC 0.17m. CALCULATE CROSS MAGNETIZING ARMATURE REACTION AMPERE TURN.

SIMPLIFIED (AT_c)

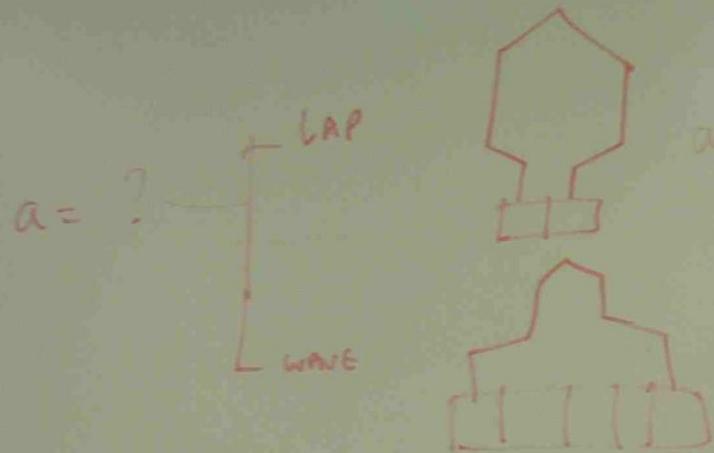
$$AT_c = \frac{\alpha z I_a}{2a P}$$

$$\alpha = \frac{\text{POLE ARC}}{\text{POLE PITCH}}$$

$$= \frac{0.17}{\frac{\pi D}{\text{No. of poles}}}$$

$$= \frac{0.17}{\frac{3.1416 \times 0.5}{6}} = 0.65$$





$$a = m \times p$$

$n = 1$ Simplex
 $m = 2$ Duplex

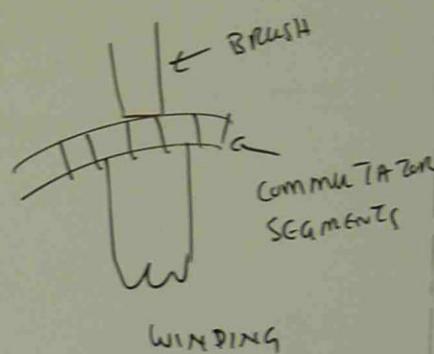
$$a = 2m$$

$m = 1$ Simplex
 $m = 2$ Duplex

$$a = m \times p = 1 \times 6 = 6$$

$$AT_c = \frac{0.65 \times 378 \times 800}{2 \times 6 \times 6}$$

$$= 2740 \text{ AT/pole}$$

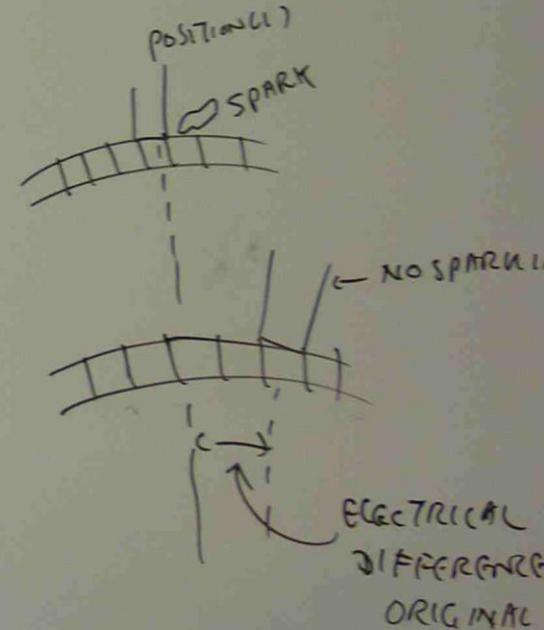


METHODS TO REDUCE ARMATURE

(1) INTER POLE



(2) SHIFT THE BRUSH POSITION (U)



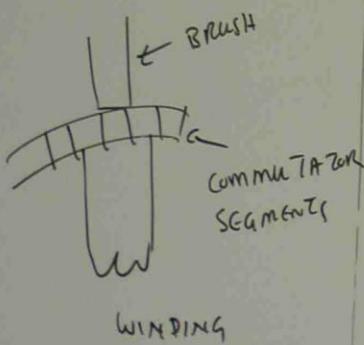


$$a = m \times p$$

$m = 1$ SIMPLEX
 $m = 2$ DUPLEX

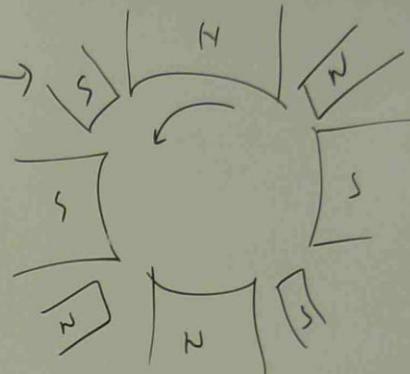
$$a = 2m$$

$m = 1$ SIMPLEX
 $m = 2$ DUPLEX

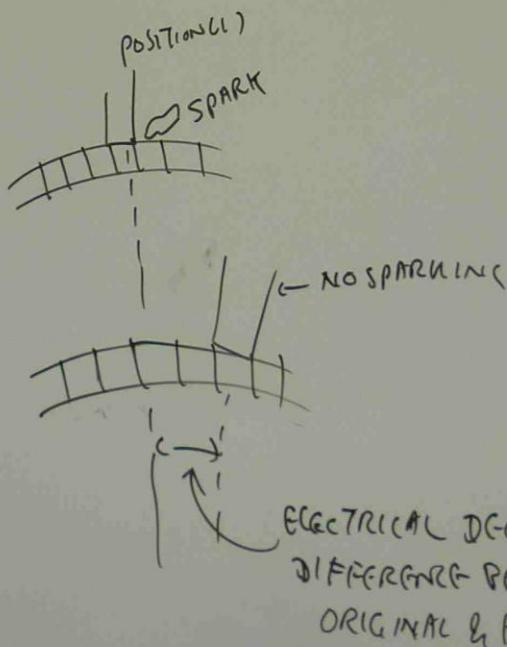


METHODS TO REDUCE ARMATURE REACTION

(1) INTER POLE



(2) SHIFT THE BRUSH



$$AT_d = \text{DEMAGNETIZING AMP-TURNS / POLE} = B$$

$$AT_c = \text{CROSS MAGNETIZING AMP-TURNS / POLE} = \frac{Z I}{2 P}$$

pb THE BRUSHES ON A ROCKED 0.03 m 6 POLES, LAP WOUND ARMATURE CURRENT AND DEMAGNETIZING

$$AT_d = \text{DEMAGNETIZING AMP-TURNS / POLE} = \frac{\beta Z I_a}{360 a} \quad \begin{aligned} Z &= \text{NO. OF CONDUCTORS} \\ I_a &= \text{ARMATURE CURRENT} \\ a &= \text{ARMATURE PARALLEL PATH} \end{aligned}$$

$$AT_c = \text{CROSS MAGNETIZING AMP-TURNS / POLE} = \frac{Z I_a}{2 P} \left(\frac{360 - 2 P \beta}{720} \right) \quad p = \text{NO. OF POLES.}$$

Pb THE BRUSHES ON A 0.4 m DIAMETER COMMUTATOR ARE ROCKED 0.03 m CIRCUMFERENTIALLY. THE MACHINE HAS 6 POLES, LAP WOUND (SIMPLEX), 378 CONDUCTORS, 800 AMP ARMATURE CURRENT. CALCULATE CROSS MAGNETIZING AND DEMAGNETIZING AMP-TURNS / POLE.

