

## BALANCED 3 $\phi$

ALL PHASE / LINE VOLTAGE EQUAL

CURRENT EQUAL

PHASE DISPLACEMENT 120°

## UNBALANCED 3 $\phi$

UNBALANCED LOADING

SHORT CIRCUIT

PARTIAL SHORT

OPEN PHASE

PHASE TO GROUND

→ UNEQUAL PHASE / LINE  
VOLTAGE

UNEQUAL PHASE / LINE  
CURRENT

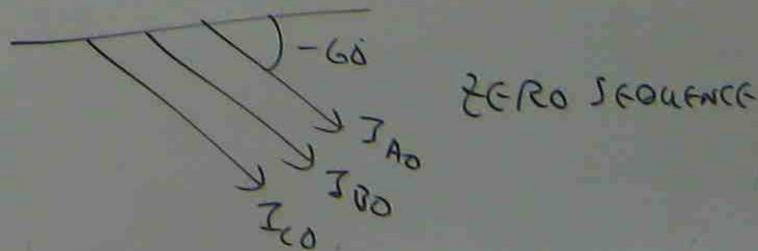
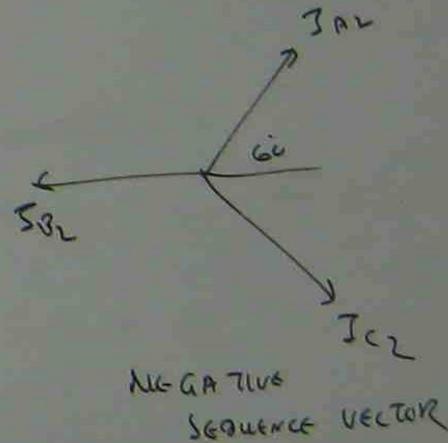
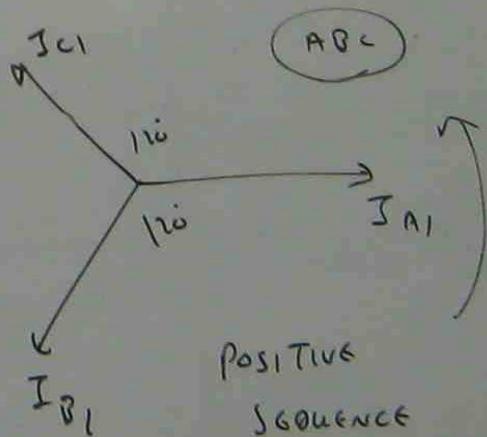
PHASE DISPLACEMENT  
MAY NOT BE 120°

$$j = 1 \angle 90^\circ, \quad j^2 = 1 \angle 180^\circ, \quad j^3 = 1 \angle 270^\circ$$

$$(j = \sqrt{-1})$$

$$a = \text{PHASE DISPLACEMENT} = 1 \angle 120^\circ$$

$$a^2 = 1 \angle 240^\circ$$



$$I_A = I_{A1}^+ + I_{A2}^- + I_{A0}^0$$

$$I_B = I_{B1}^+ + I_{B2}^- + I_{B0}^0$$

$$I_C = I_{C1}^+ + I_{C2}^- + I_{C0}^0$$

$$I_{A1}^+ = \frac{1}{3} (I_A + a I_B + a^2 I_C)$$

$$I_{A2}^- = \frac{1}{3} (I_A + a^2 I_B + a I_C)$$

$$I_{A0}^0 = \frac{1}{3} (I_A + I_B + I_C)$$

$I_{B1}^+$  SAME MAGNITUDE AS  $I_{A1}^+$ , BUT  $-120^\circ$  DIFFERENCE

$I_{C1}^+$  SAME MAGNITUDE AS  $I_{A1}^+$ , BUT  $+120^\circ$  DIFFERENCE

$I_{B2}$  SAME MAGNITUDE AS  $I_{A2}$  BUT  $+ 120^\circ$  DIFFERENCE  
 $I_{C2}$  SAME MAGNITUDE AS  $I_{A2}$  BUT  $- 120^\circ$  DIFFERENCE

$I_{B0} = I_{C0} = I_{A0}$  THERE IS  $- 60^\circ$  PHASE ANGLE

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$$I_A = I_{A1} + I_{A2} + I_{A0}$$

$$I_B = I_{B1} + I_{B2} + I_{B0}$$

$$I_C = I_{C1} + I_{C2} + I_{C0}$$

$$I_{B2}$$

$$I_{C2}$$

SAME MAGNITUDE AS  $I_{A2}$  BUT  $+120^\circ$  DIFFERENCE

SAME MAGNITUDE AS  $I_{A2}$  BUT  $-120^\circ$  DIFFERENCE

$$I_{B0} = I_{C0} = I_{A0} \quad \text{THEIR } \angle \text{ IS } -60^\circ \text{ PHASE ANGLE}$$

$$I_{A1} = \frac{1}{3} (I_A + a I_B + a^2 I_C)$$

$$I_{A2} = \frac{1}{3} (I_A + a^2 I_B + a I_C)$$

$$I_{A0} = \frac{1}{3} (I_A + I_B + I_C)$$

$I_{B1}$  SAME MAGNITUDE AS  $I_{A1}$ , BUT  $-120^\circ$  DIFFERENCE

$I_{C1}$  SAME MAGNITUDE AS  $I_{A1}$ , BUT  $+120^\circ$  DIFFERENCE

$I_{B2}$

SAME MAGNITUDE AS  $I_{A2}$  BUT  $+120^\circ$  DIFFERENCE

$I_{C2}$

SAME MAGNITUDE AS  $I_{A1}$  BUT  $-120^\circ$  DIFFERENCE

$I_{B0} = I_{C0} = I_{A0}$

THERE IS  $-60^\circ$  PHASE ANGLE

$I_{A1} = I \angle 0^\circ$       $I_{B1} = I \angle 0 - 120^\circ$       $I_{C1} = I \angle 0 + 120^\circ$

$I_{A2} = I_1 \angle 0^\circ$       $I_{B2} = I_1 \angle 0^\circ + 120^\circ$       $I_{C2} = I_1 \angle 0^\circ - 120^\circ$